## 2-AIN-108: Labs #4 DL Conceptualization

**Exercise 1.** Given  $N_{\mathsf{C}} = \mathsf{Person}$ , Female and  $N_{\mathsf{R}} = \mathsf{hasChild}$  define complex concepts:

- Male
- Parent
- Father
- Mother
- GrandParent
- GrandMother
- GrandFather
- MotherHavingOnlyDaughters

Exercise 2. Formalize following sentences as composite concepts:

- A man that is married to a doctor, and all of whose children are either doctors or professors.
- A man that likes only married women.
- A parent that has a child whose children are all maried.

Exercise 3. Formalize following sentences as TBox axioms:

- Car engine is either diesel engine, petrol engine, electric engine, hybrid engine or steam engine.
- Vegetarians eat only vegetable.
- Vegan does not eat any animal product.
- Only humans can have human children.

**Exercise 4.** Proove following equivalences<sup>1</sup>:

1. 
$$\models C \sqcap \neg C \equiv \bot$$

$$2. \models C \sqcup \neg C \equiv \top$$

3. 
$$\models \neg \neg C \equiv C$$

$$4. \models \neg(C \sqcup D) \equiv \neg C \sqcap \neg D$$

5. 
$$\models \neg (C \sqcap D) \equiv \neg C \sqcup \neg D$$

<sup>&</sup>lt;sup>1</sup>Hint: realize what does  $\models C \equiv D$  mean, apply interpretation rules for concept constructors and proove resulting set identities.