

Obrazové Transformácie
Cvičenia z Počítačového Videnia

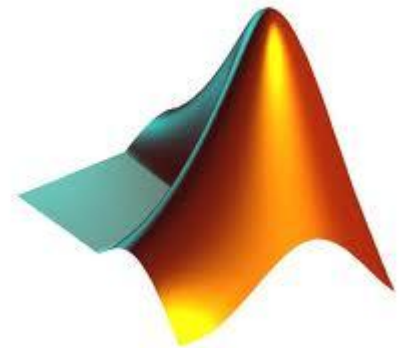
Zuzana Haladová
Júlia Kučerová

Obrazové transformácie

Zovšeobecnená Houghova transformácia

Rýchla Fourierova transformácia

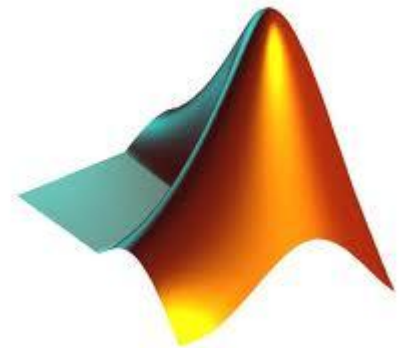
Diskrétna kosínusová transformácia



Hough

Houghova transformácia- ak chceme detekovať oblasti zo známym tvarom hranice

- Vieme detekovať priamky aj krivky, ak je známe ich analytické vyjadrenie
- Metóda je robustná aj pre zašumené objekty



Hough

Houghova transformácia pre priamky

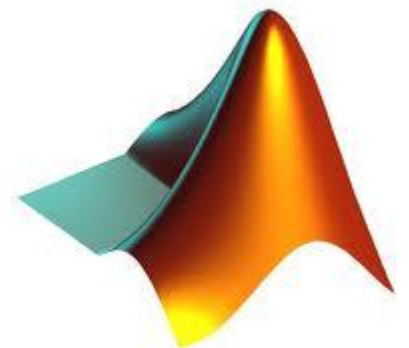
- Priamku vieme vyjadriť

$$y = mx + b$$

- Houghova trans. reprezentuje priamku pomocou b , m resp. r , θ pričom

- r je najmenšia vzdialenosť od počiatku k priamke

- θ je uhol medzi x a priamkou



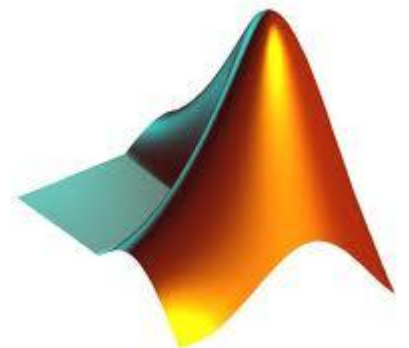
Hough

Vyjadrenie priamky pomocou r a θ je:

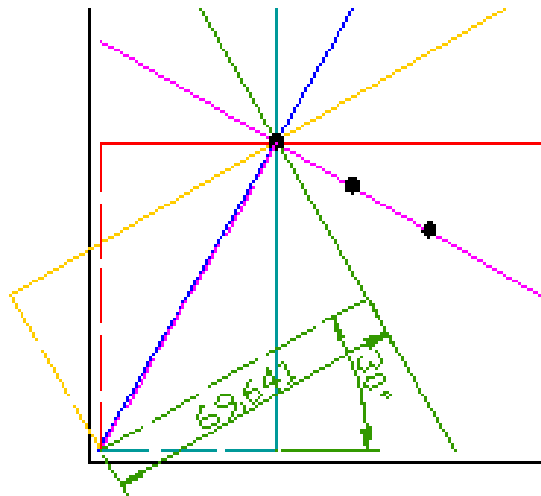
- HT pracuje na bin. obrázku nasledovne:

$$y = \left(-\frac{\cos \Theta}{\sin \Theta}\right)x + \left(\frac{r}{\sin \Theta}\right)$$

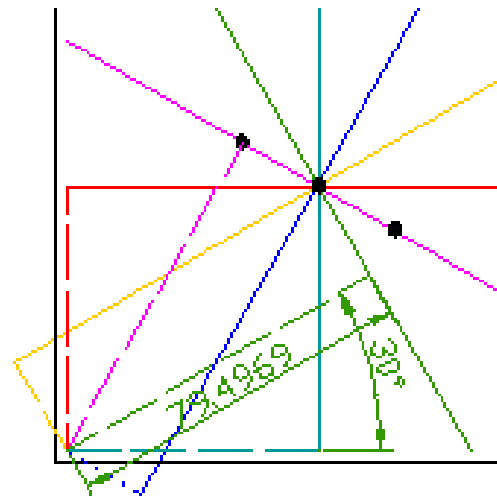
- Pre každý bod obrázku a pre každú priamku ním prechádzajúcu vypočíta r a θ tejto priamky.



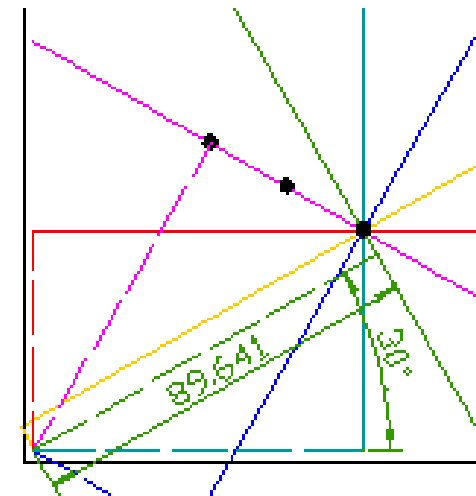
Hough



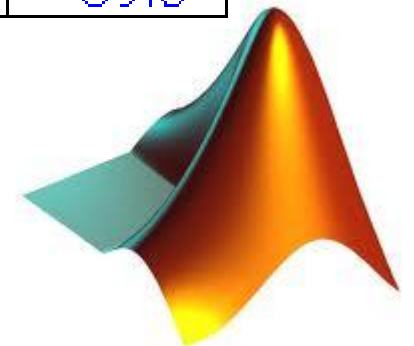
Angle	Dist.
0	40
30	69.6
60	81.2
90	70
120	40.6
150	0.4



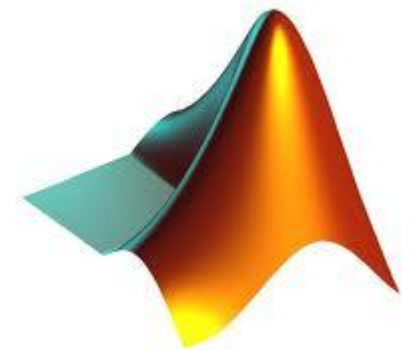
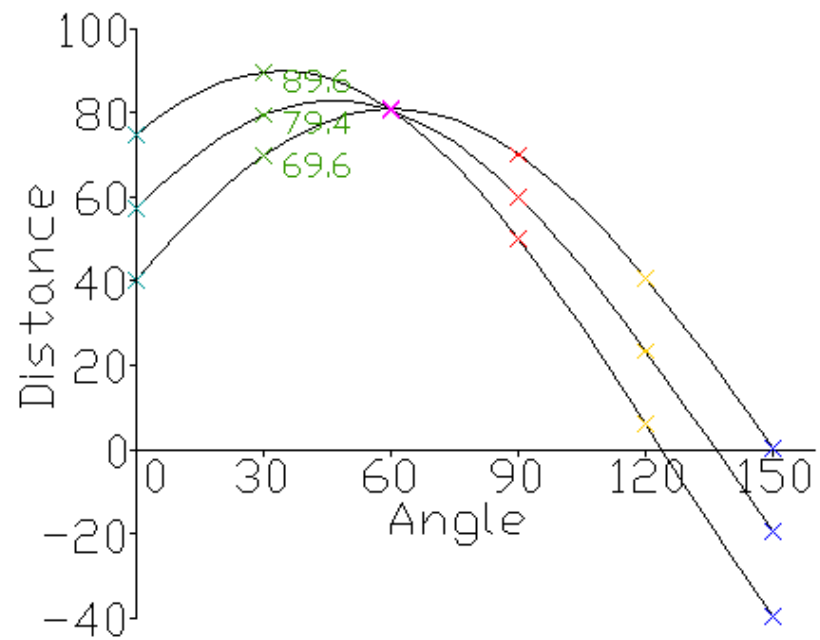
Angle	Dist.
0	57.1
30	79.5
60	80.5
90	60
120	23.4
150	-19.5



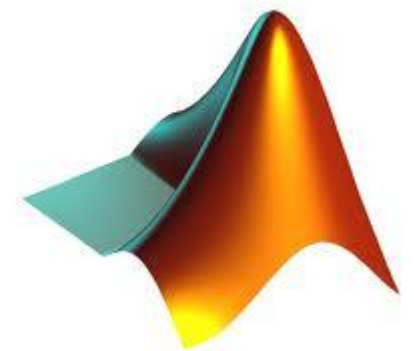
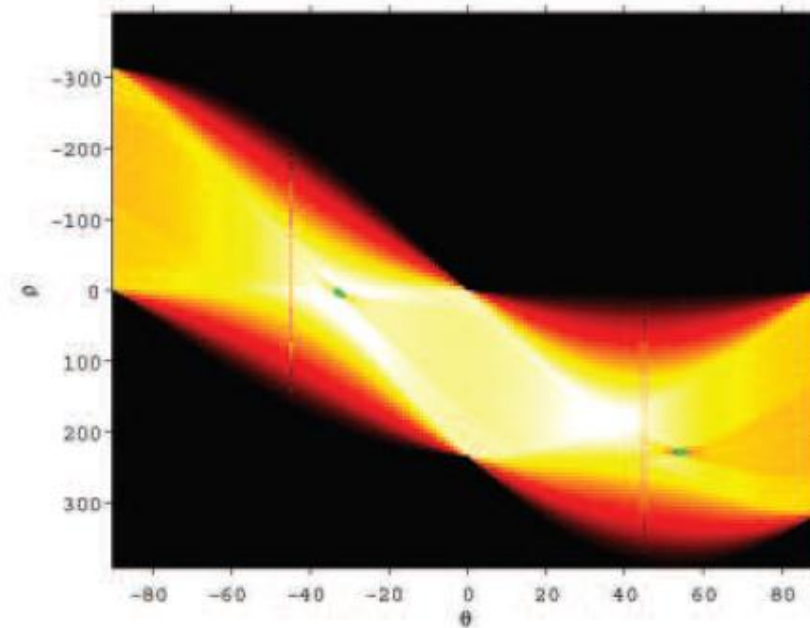
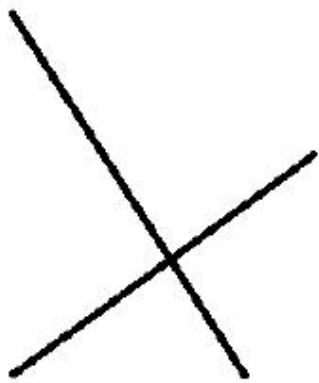
Angle	Dist.
0	74.6
30	89.6
60	80.6
90	50
120	6.0
150	-39.6



Hough



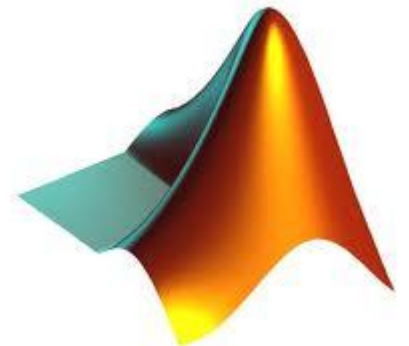
Hough



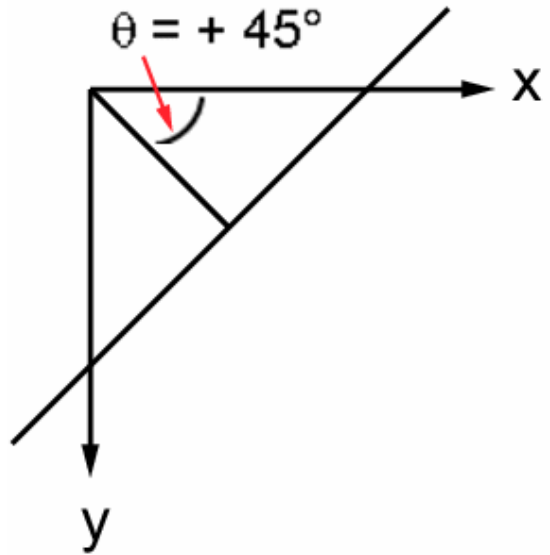
Hough

V MATLAB (Image Processing Toolbox)

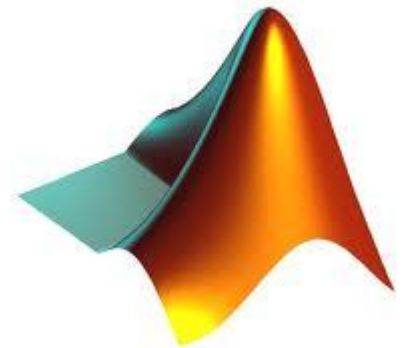
```
I=imread('1.jpg'); IG =rgb2gray(I);  
IE=edge(IG,'Canny');  
[H,T,R]=hough(IE);  
imshow(imadjust(mat2gray(H)), 'XData',T, 'YData',  
R); colormap(hot);
```



Hough



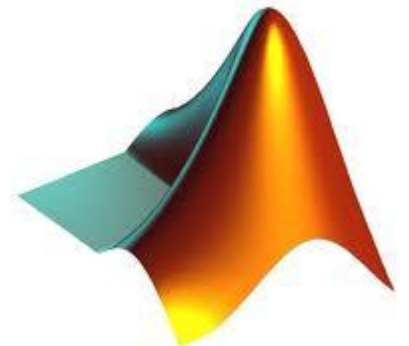
$$\rho = x \cdot \cos(\theta) + y \cdot \sin(\theta)$$



Hough

$[H, T, R] = \text{hough}(IE);$

- H – matica Houghovej transformácie
- T je pole hodnôt θ a R je pole r nad ktorými je vyjadrená H
- Riadky a stĺpce H zodpovedajú r a θ
- hodnota na pozícii (1,2) zodpovedá počtu bodov ležiacich na priamke z 1. r a 2. θ z polí R a T



Hough

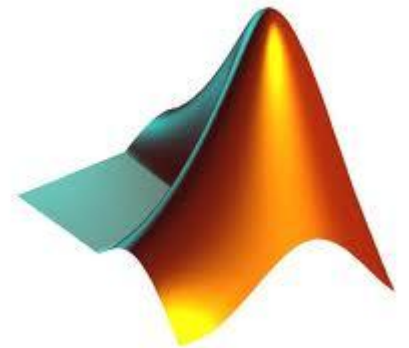
`[H,T,R]=hough(IE);`

- `peaks = houghpeaks(H, numpeaks)`

- `peaks` je pole $Q \times 2$ kde Q

`<0,numpeaks>`

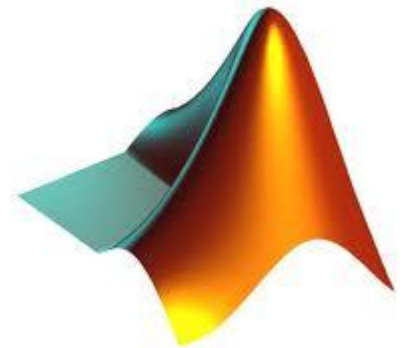
a obsahuje x,y hodnoty pre `peaks` v `H`



Hough

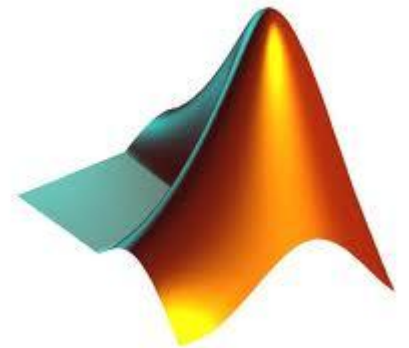
`lines = houghlines(BW, theta, rho, peaks)`

- lines je štruktúrované pole ktoré pre každú nájdenú úsečku obsahuje:
 - point1 x,y hodnoty konca úsečky
 - point2 x,y hodnoty konca úsečky
 - theta uhol v stupňoch (z matice H)
 - rho hodnota(z matice H)



Hough

```
lines = houghlines(IE, theta, rho, peaks)
- figure, imshow(IE), hold on
- for k = 1:length(lines)
- xy = [lines(k).point1; lines(k).point2];
- plot(xy(:,1),xy(:,2),'Color','green');
- end
```

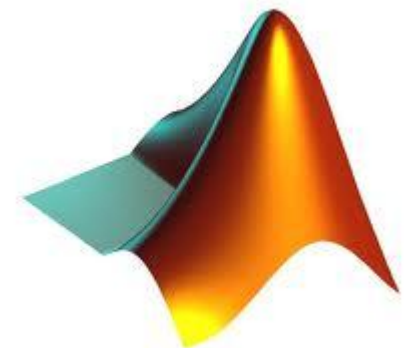
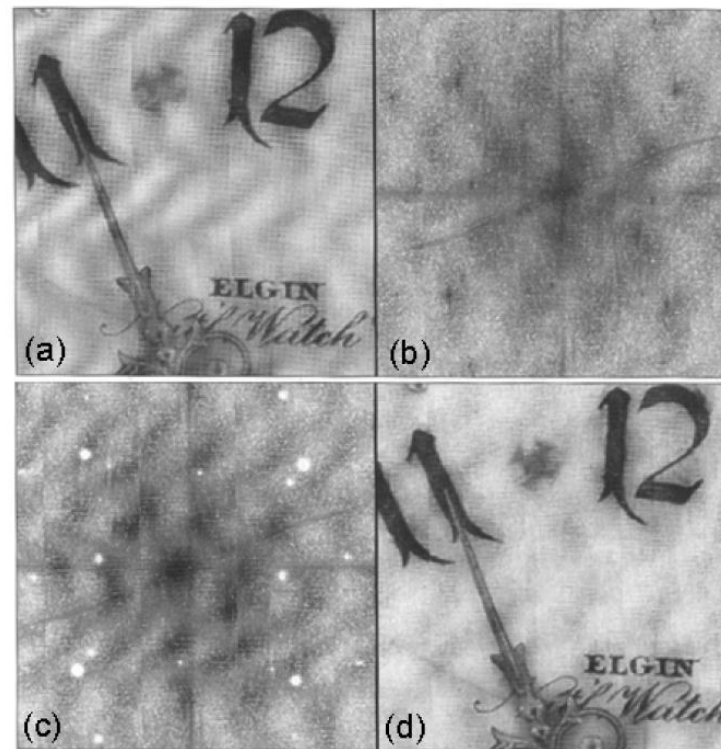


FFT

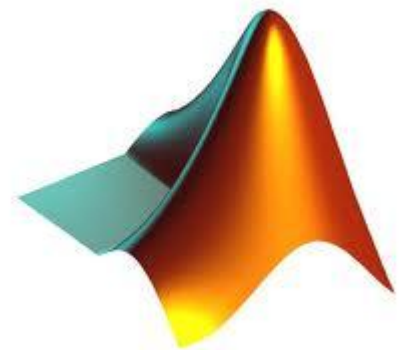
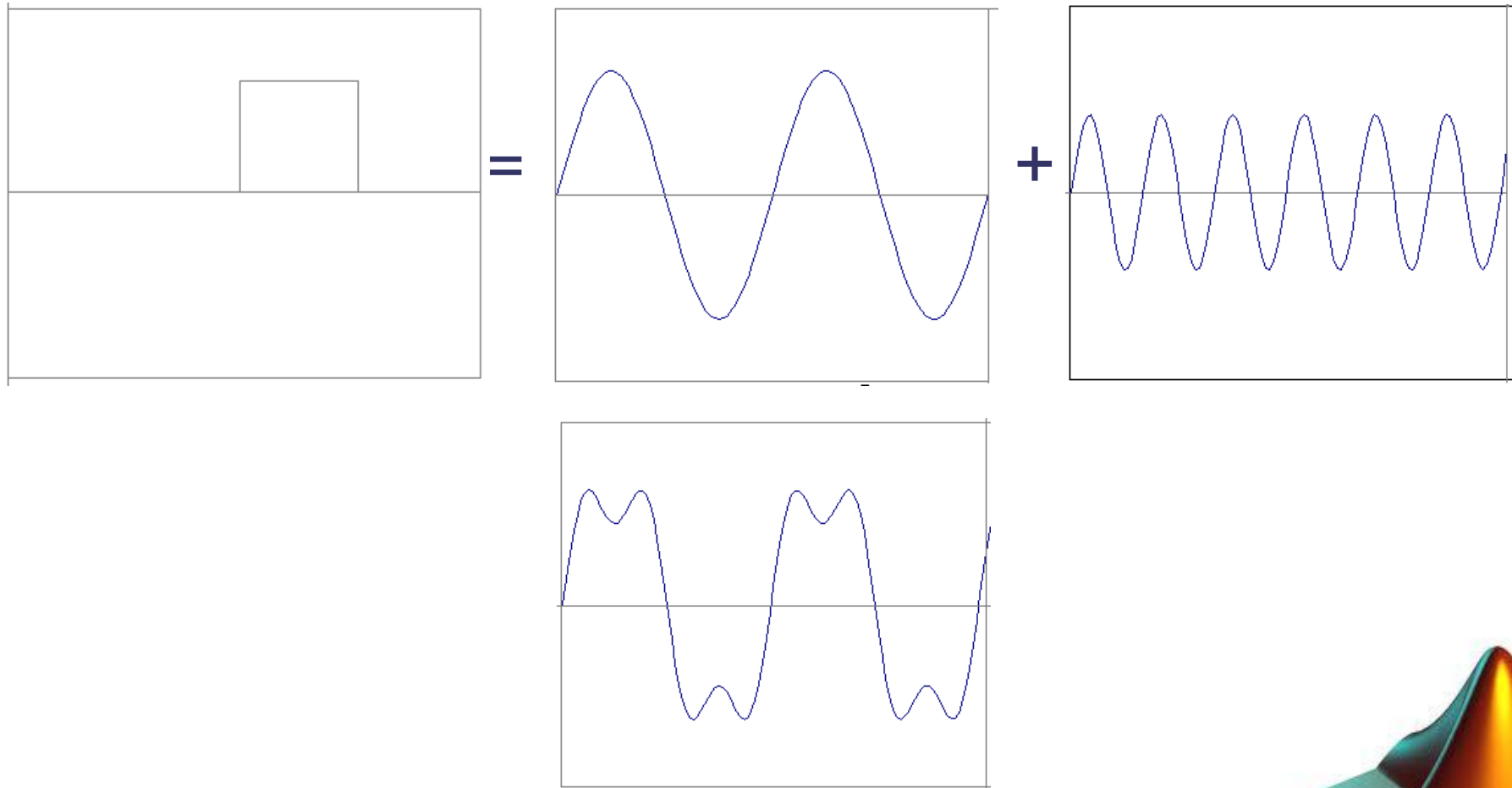
Akákoľvek funkcia $f(x)$ môže byť vyjadrená ako vážený súčet sínusov a kosínusov

Využitie:

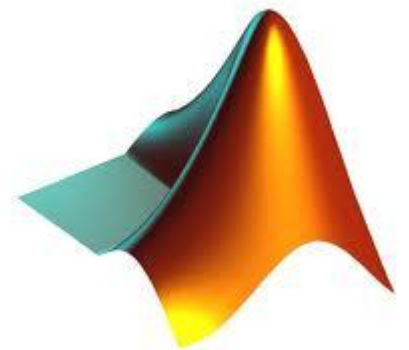
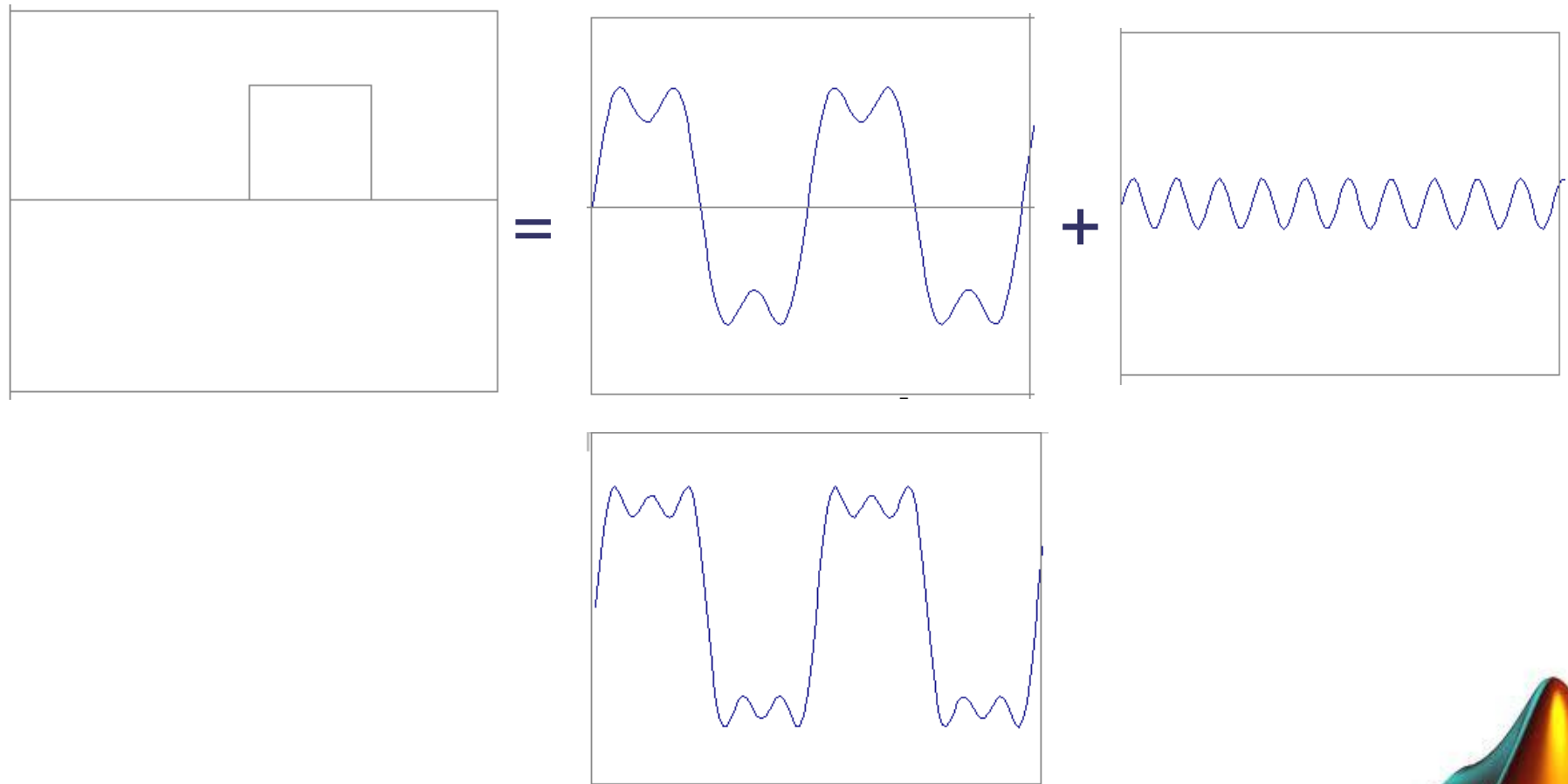
- lowpass filter
- highpass filter
- odstraňovanie artefaktov z obrazu



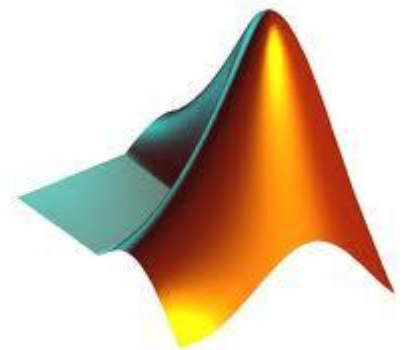
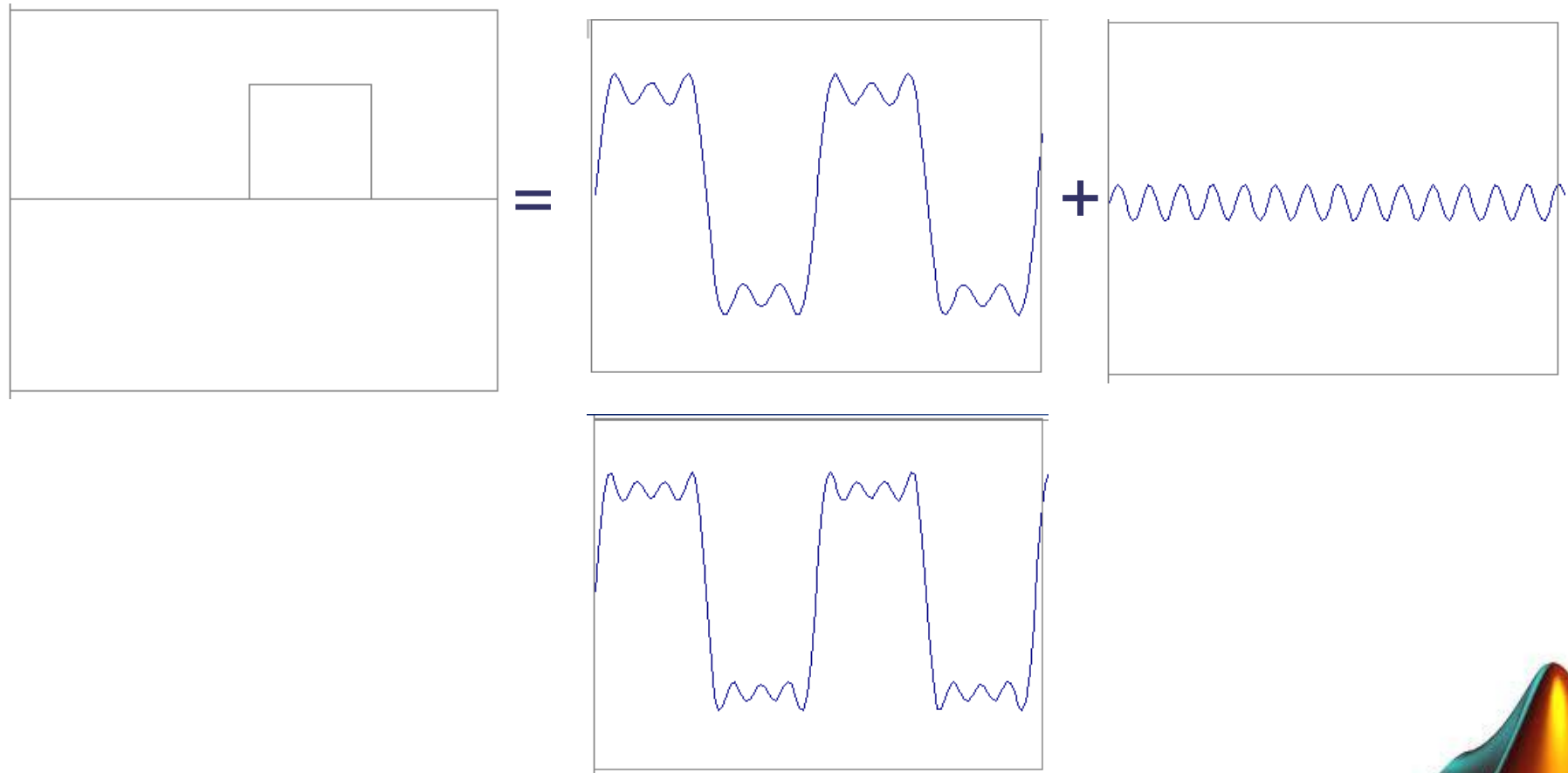
FFT



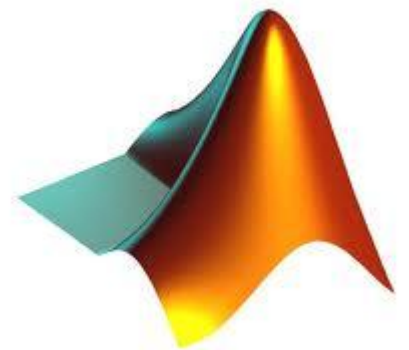
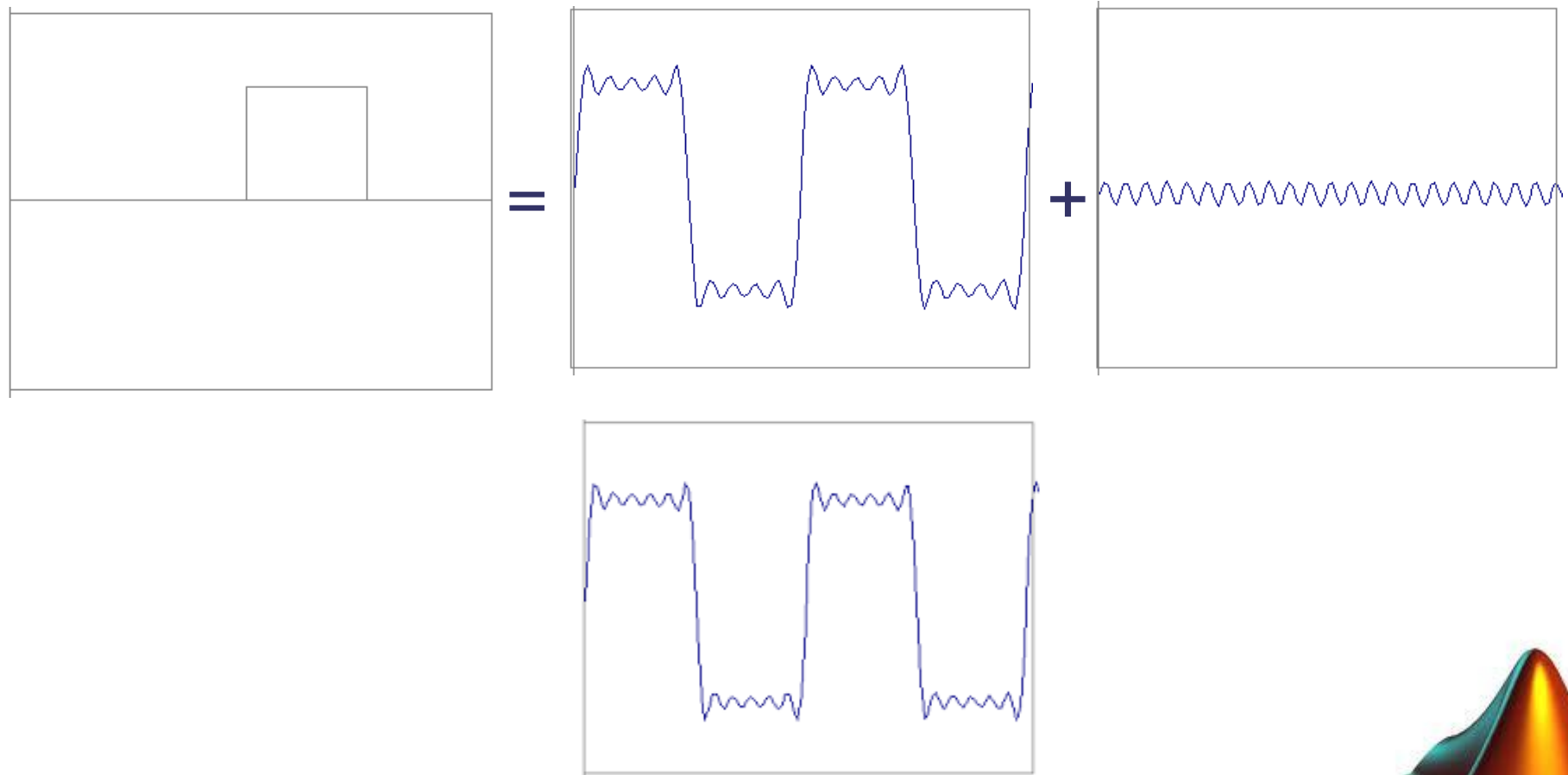
FFT



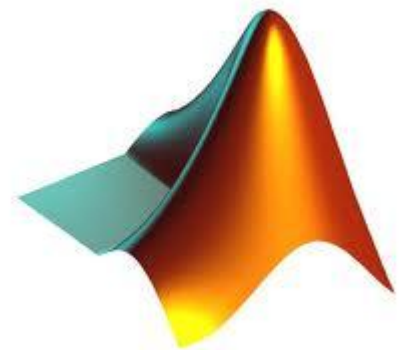
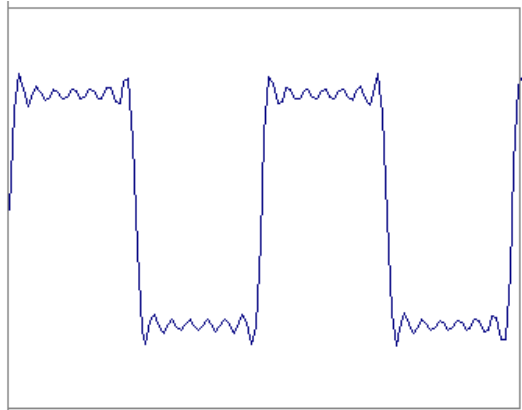
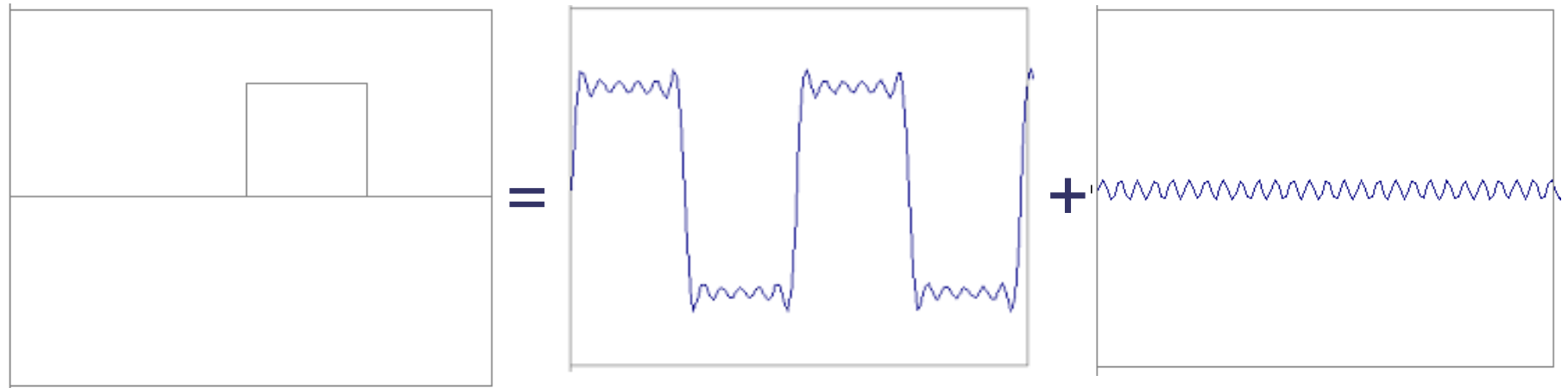
FFT



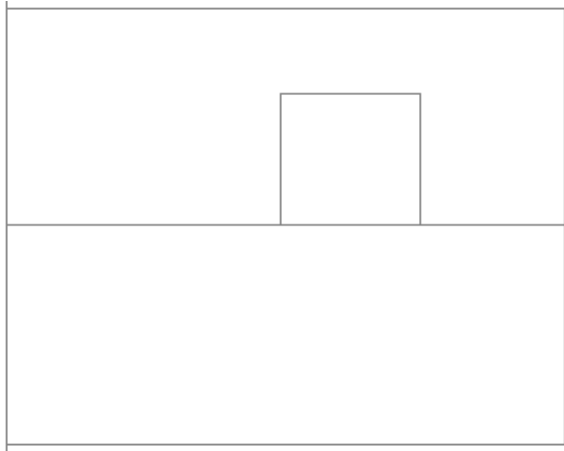
FFT



FFT

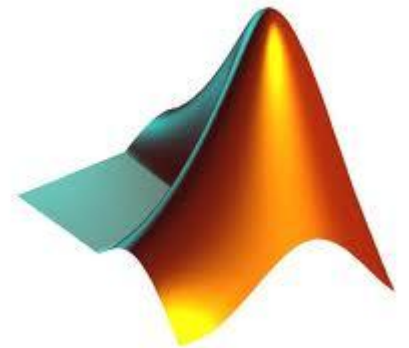
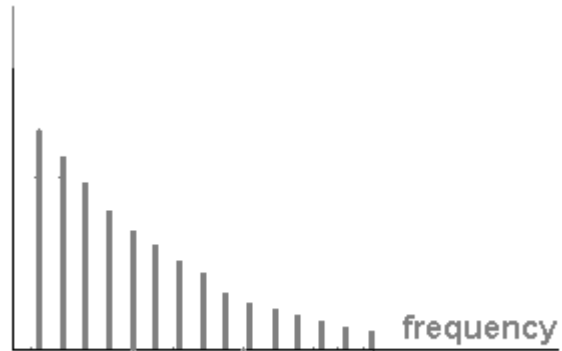


FFT

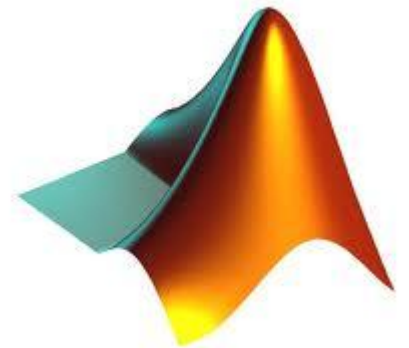
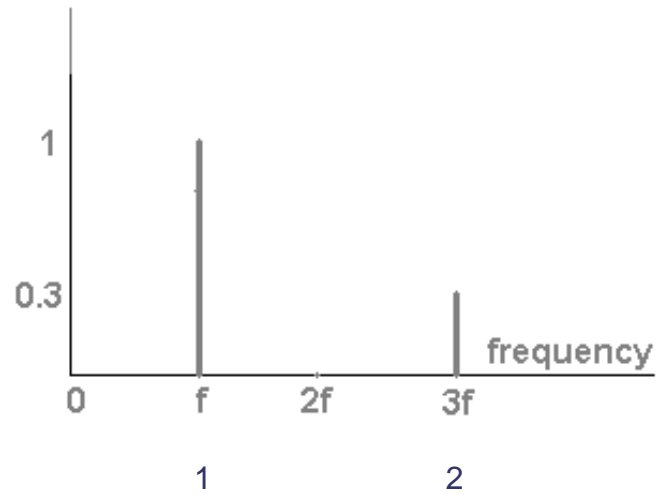
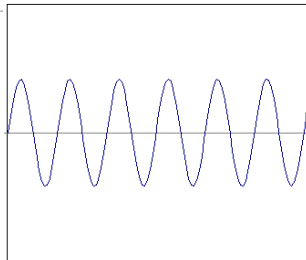
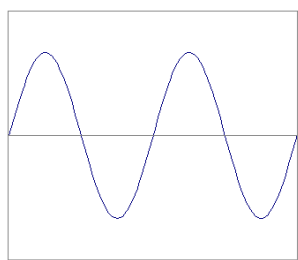
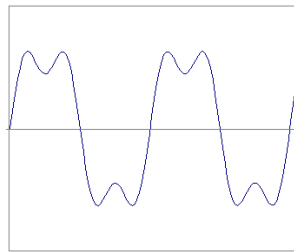
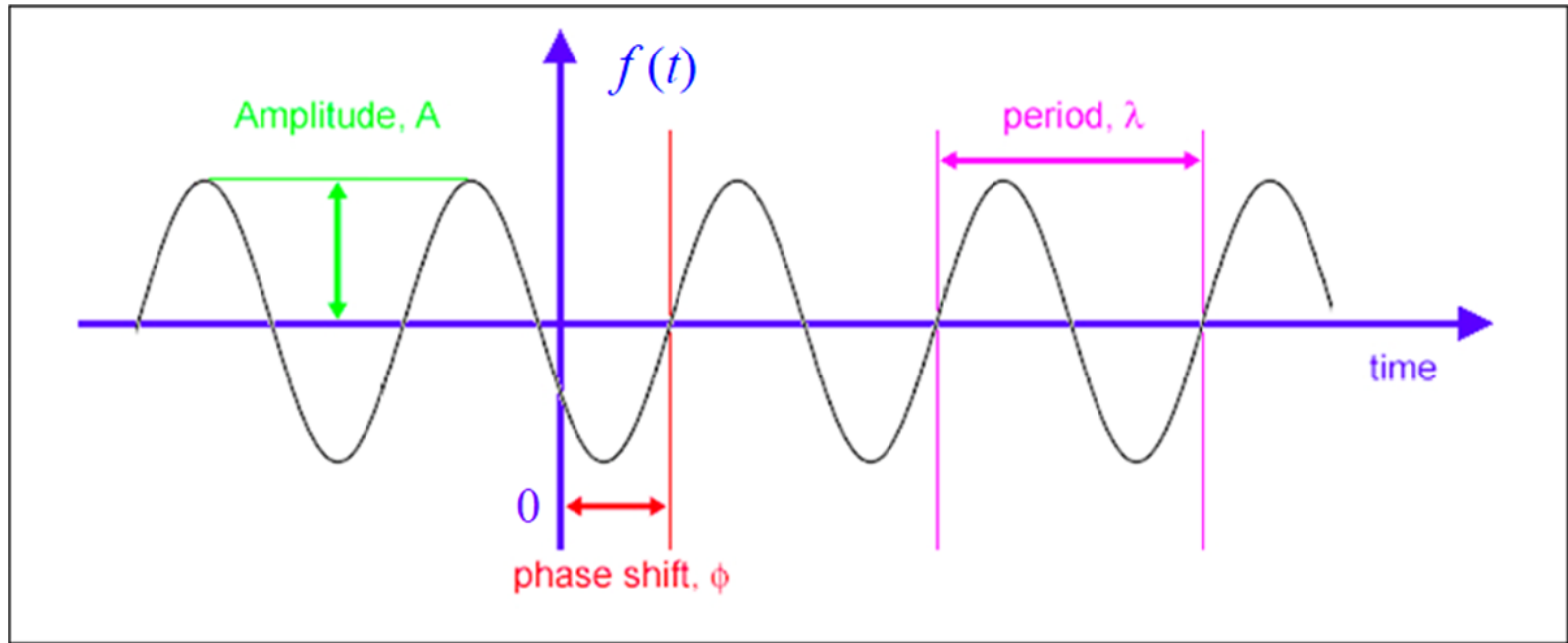


=

$$A \sum_{k=1}^{\infty} \frac{1}{k} \sin(2\pi kt)$$

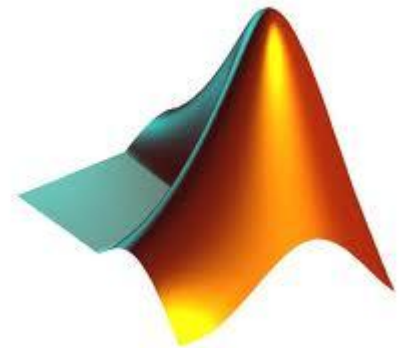


FFT



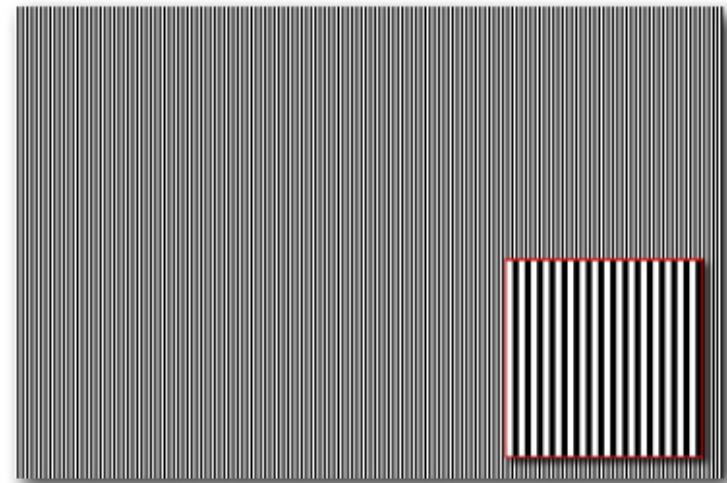
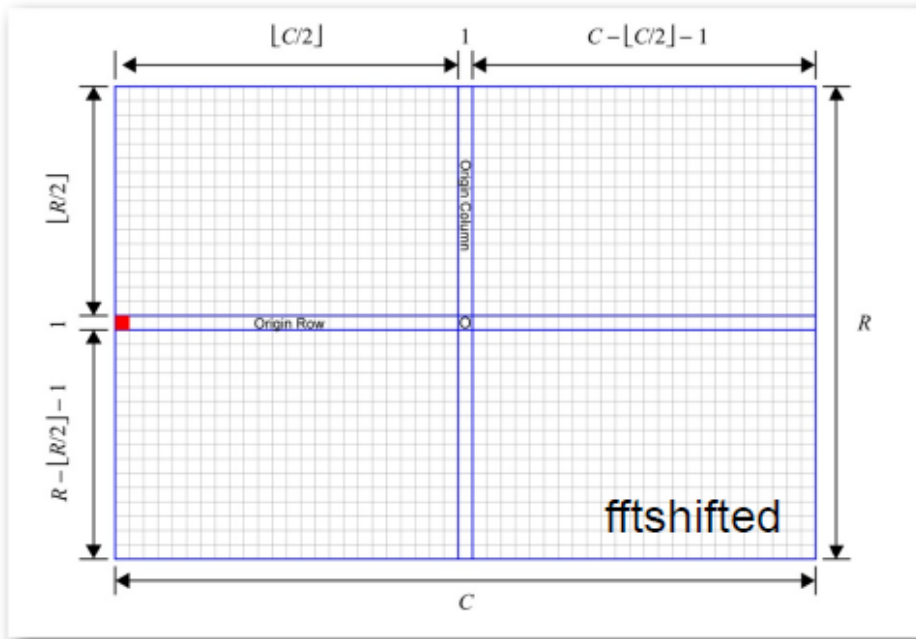
FFT - Skladanie signálu MATLAB

```
Fs = 1000;           % Sampling frequency
T = 1/Fs;           % Sample time
L = 1000;           % Length of signal
t = (0:L-1)*T;      % Time vector
y1 = 0.9*sin(2*pi*10*t);
y2 = 0.3*sin(2*pi*30*t);
y3 = y1 + y2;
figure, plot(Fs*t(1:200),y1(1:200));
figure, plot(Fs*t(1:200),y2(1:200));
figure, plot(Fs*t(1:200),y3(1:200));
```

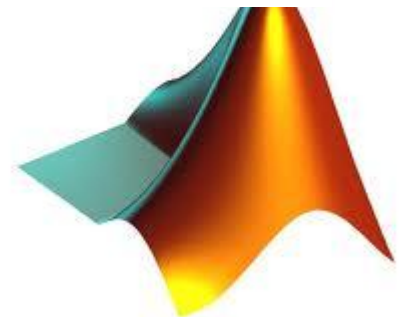


FFT

"horizontal" is the wavefront direction.

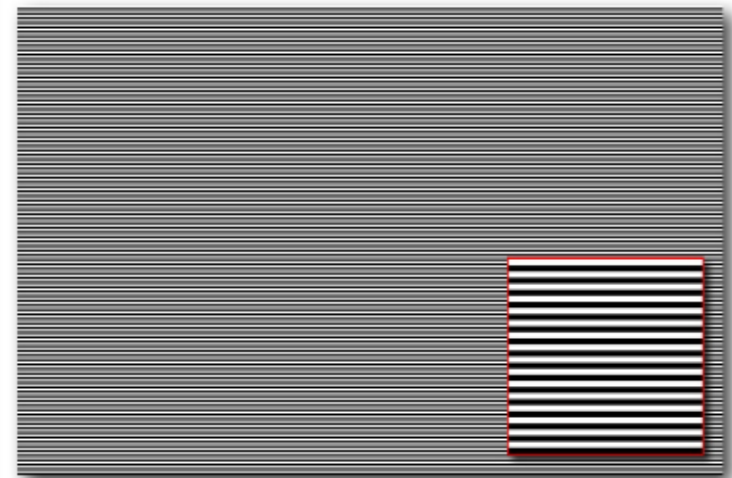
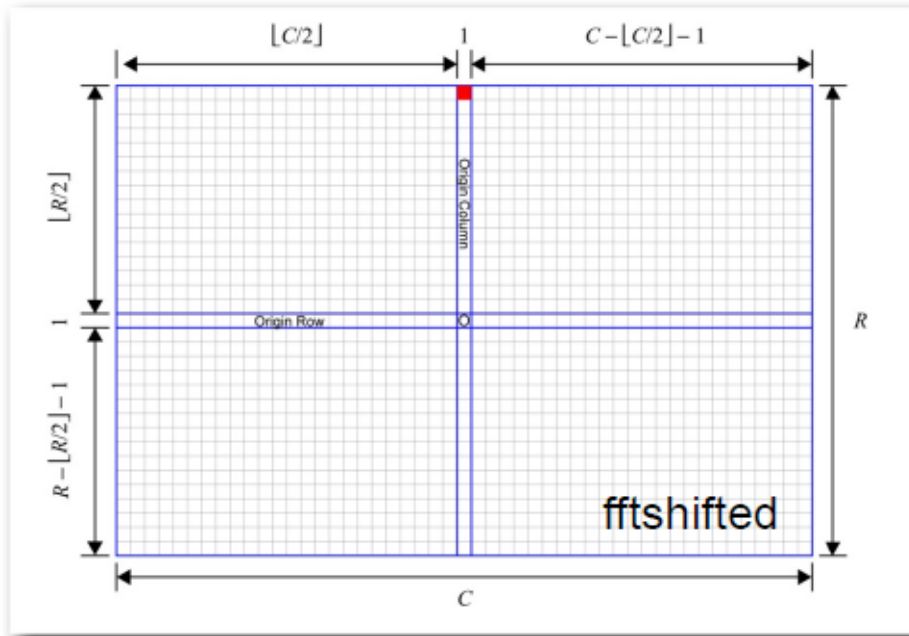


highest-possible-frequency horizontal sinusoid

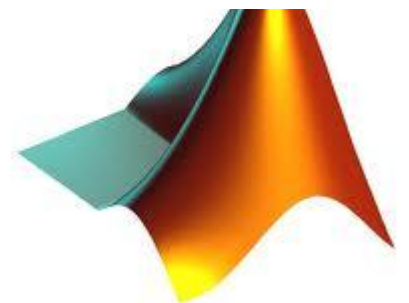


FFT

"vertical" is the wavefront direction.

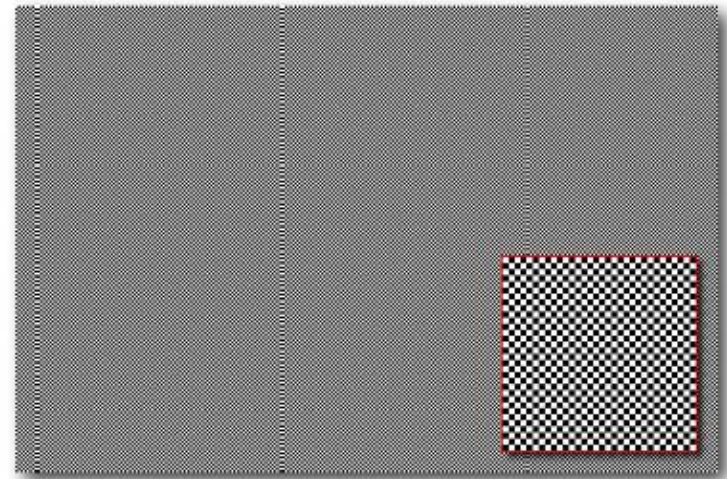
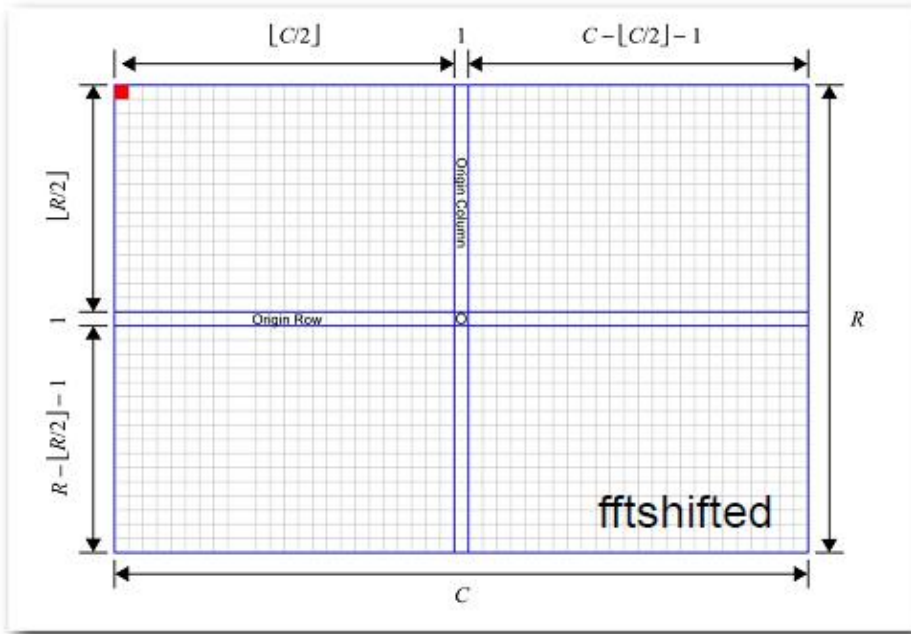


highest-possible-frequency vertical sinusoid

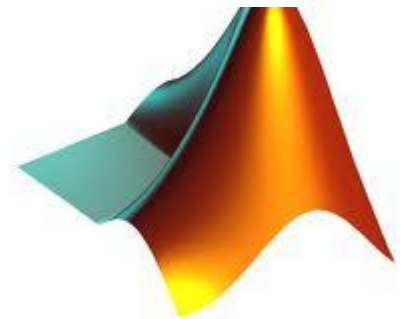


FFT

a checker-board pattern.

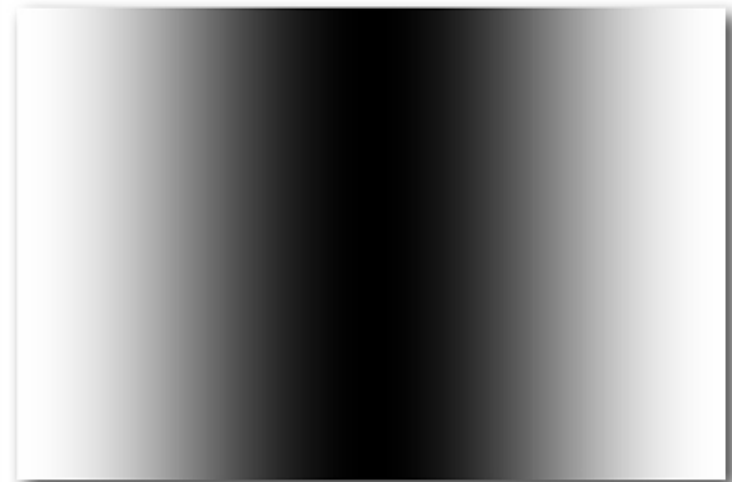
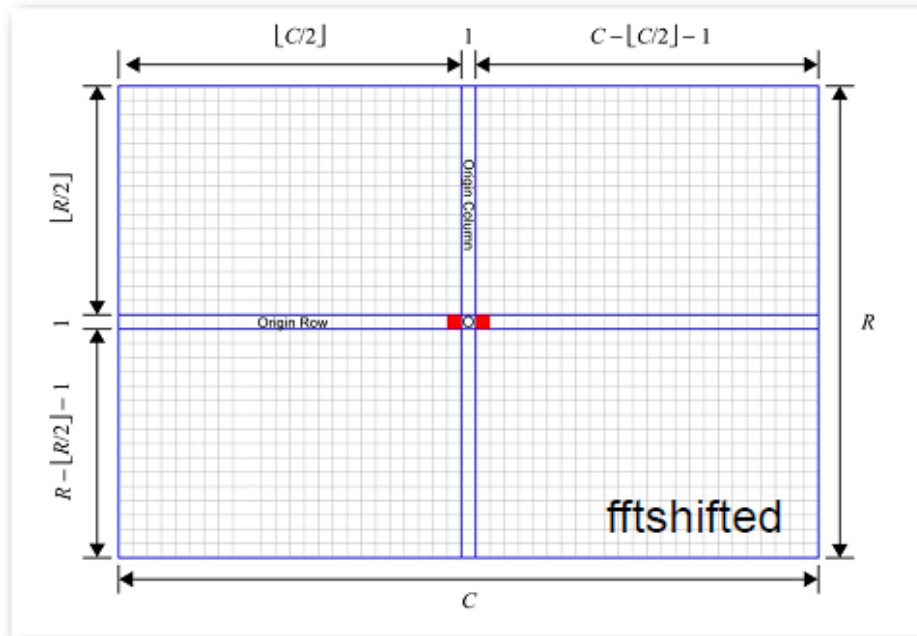


highest-possible-freq horizontal+vertical sinusoid (R & C even)

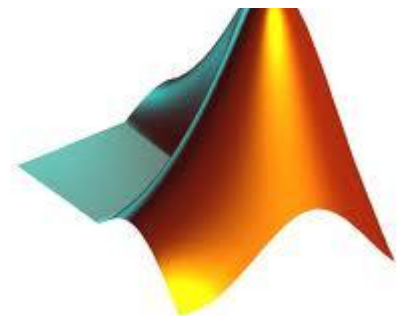


FFT

"horizontal" is the
wavefront direction.

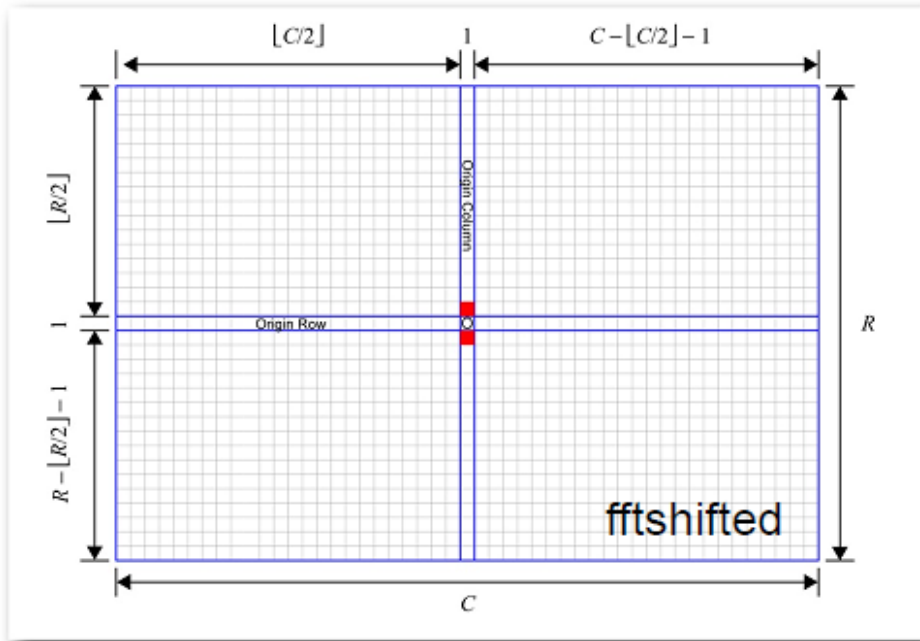


lowest-possible-frequency horizontal sinusoid

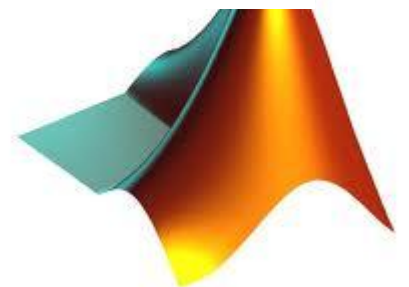


FFT

"vertical" is the wavefront direction.

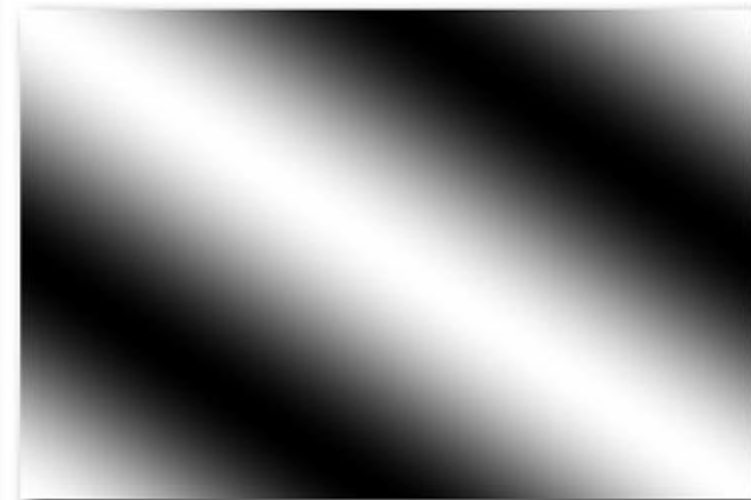
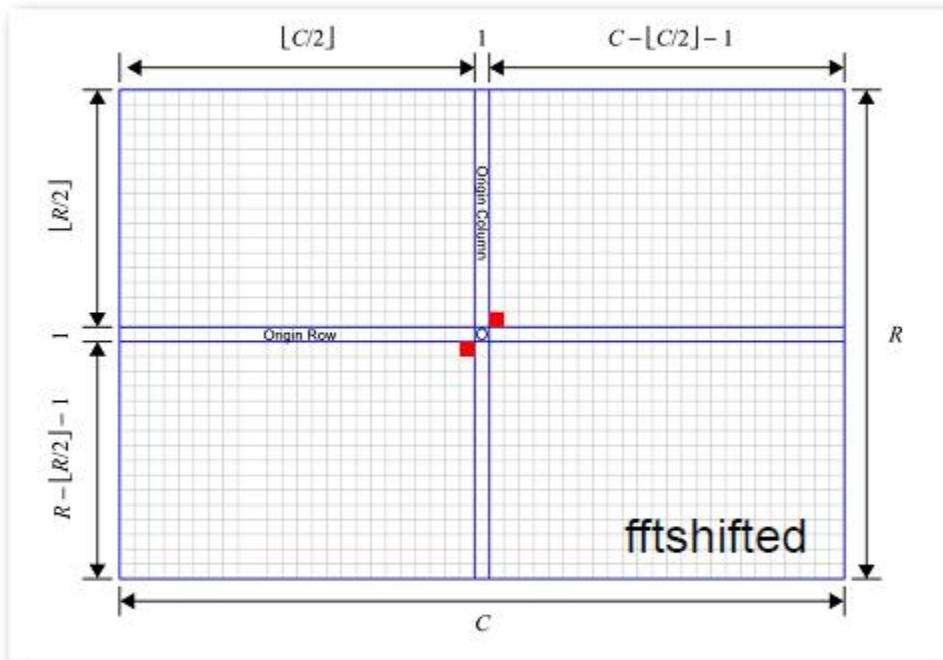


lowest-possible-frequency vertical sinusoid

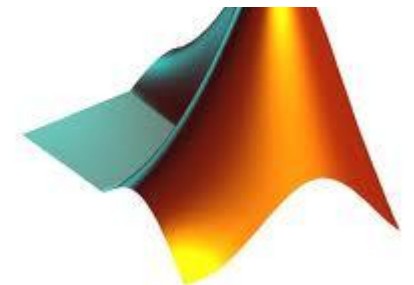


FFT

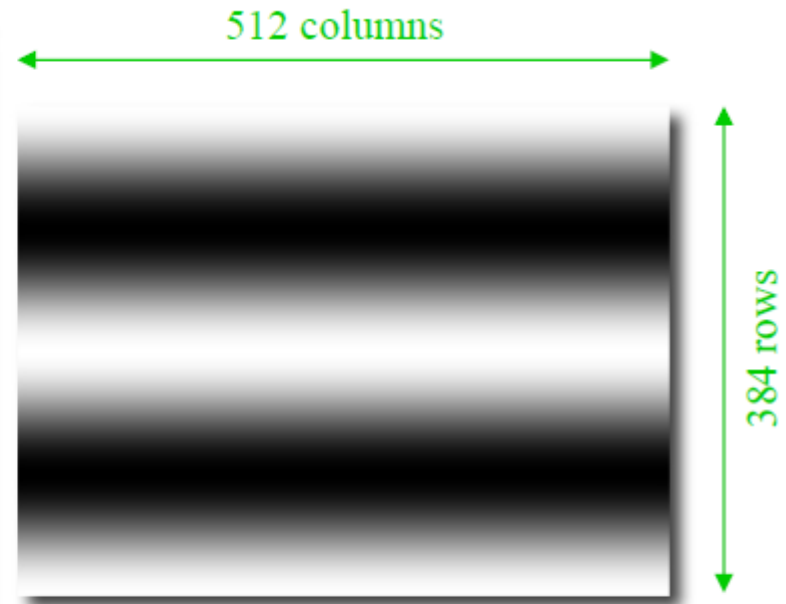
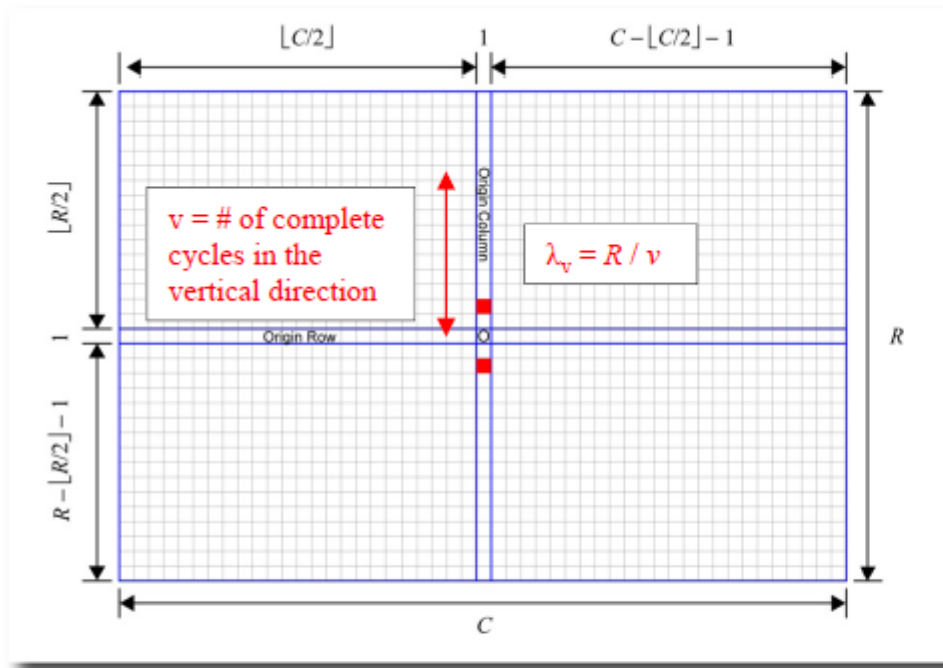
"negative diagonal" is the wavefront direction.



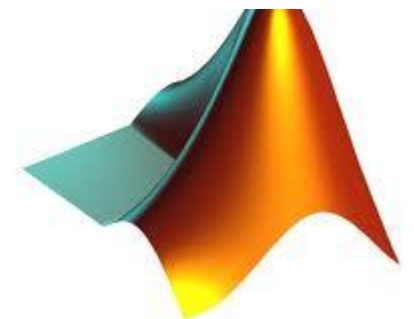
lowest-possible-frequency negative diagonal sinusoid



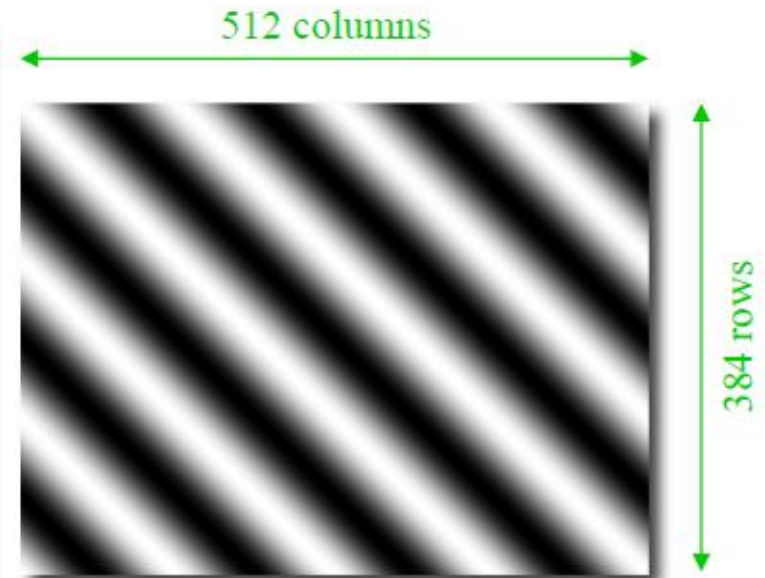
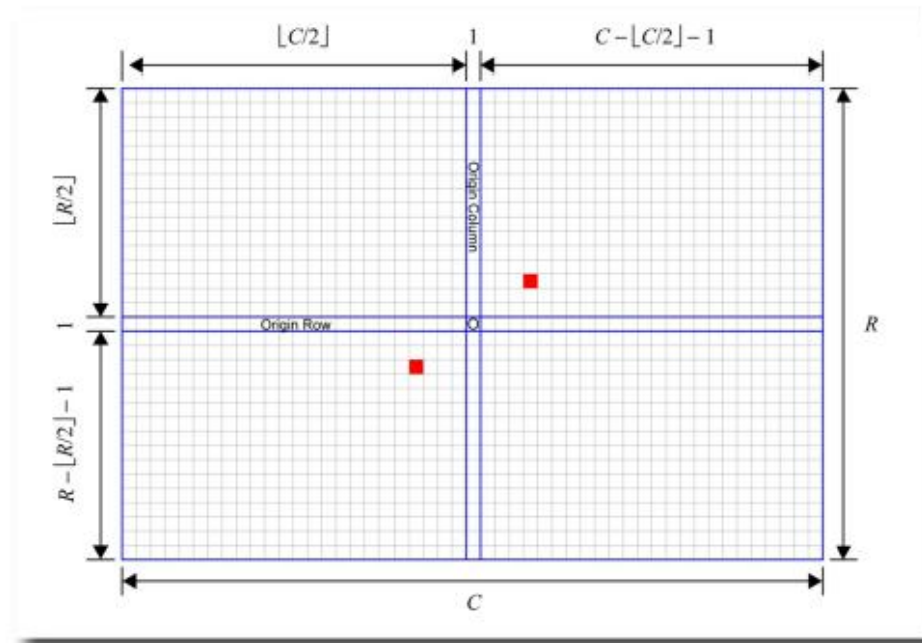
FFT



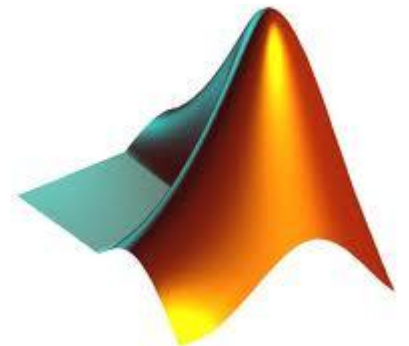
frequencies: $(u, v) = (0, 2)$; wavelength: $\lambda_v = 192$



FFT



frequencies: $(u, v) = (4, 3)$; wavelengths: $(\lambda_u, \lambda_v) = (128, 128)$



FFT

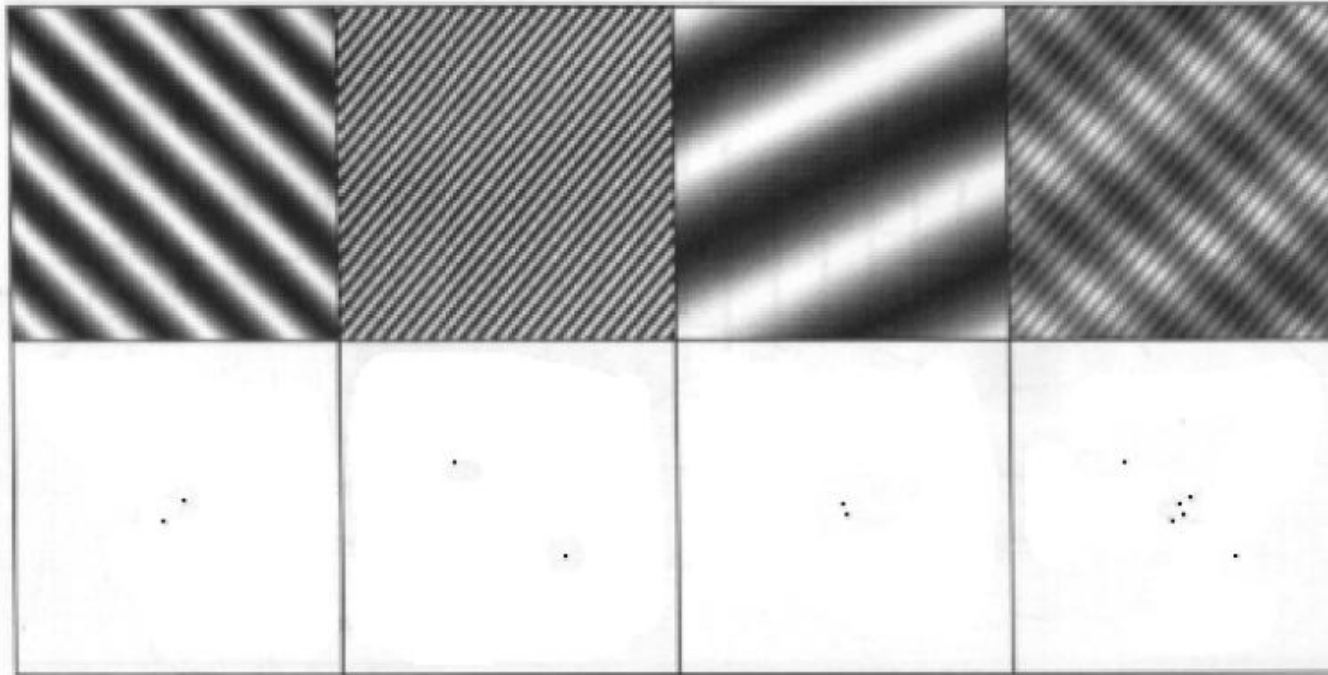
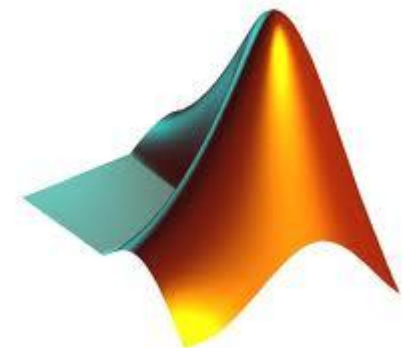
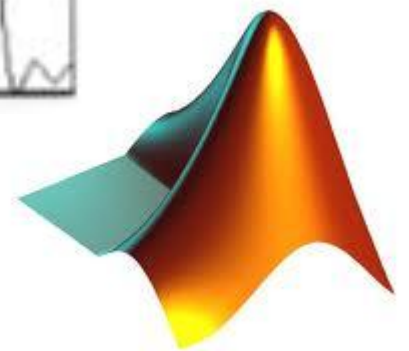
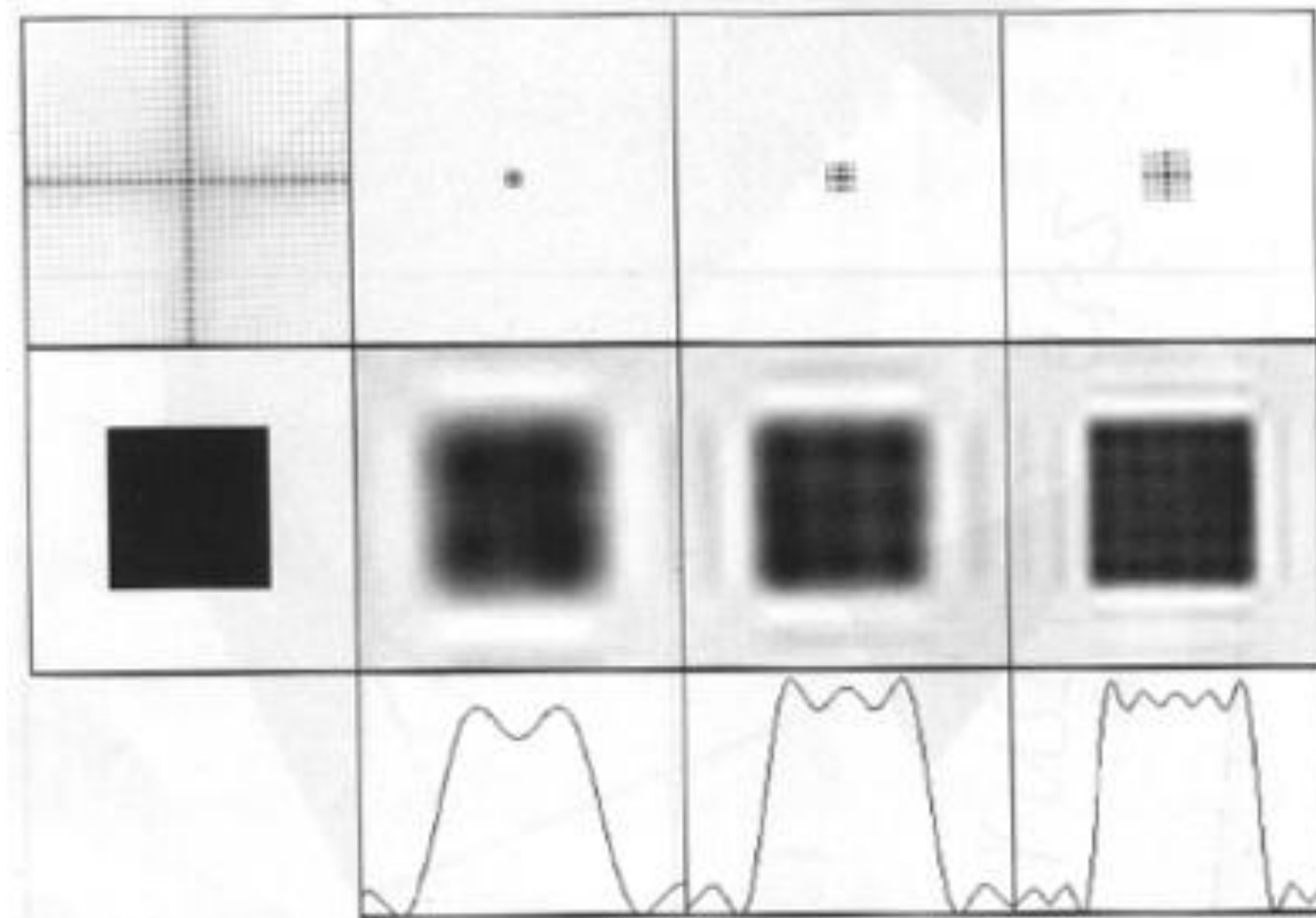


Figure 2: Images with perfectly sinusoidal variations in brightness: The first three images are represented by two dots. You can easily see that the position and orientation of those dots have something to do with what the original image looks like. The 4th image is the sum of the first three.

(Taken from p.177 of [1].)



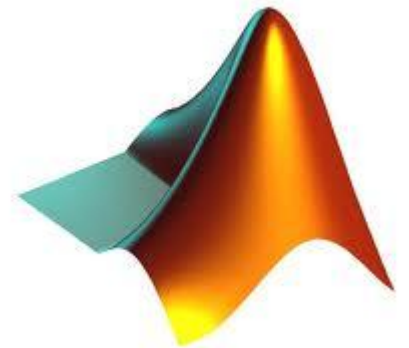
FFT



FFT MATLAB

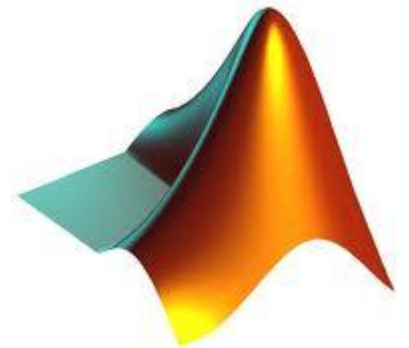
2-D Fast Fourier transform

```
PS = fftshift(log(abs(fft2(I))+1));  
M = max(PS(:));  
image(uint8(255*(PS/M)));
```



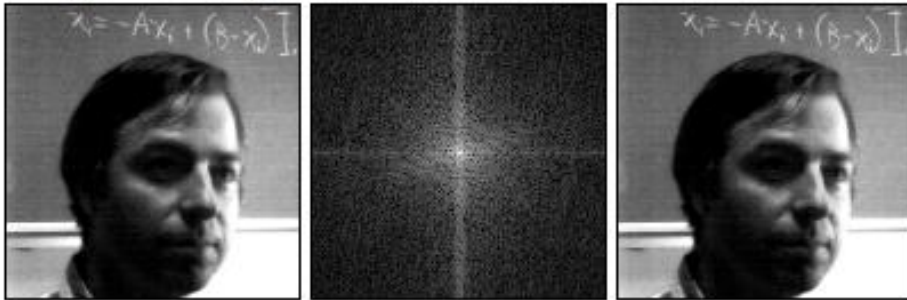
FFT ImageJ

- Image Processing and Analysis in Java
- Vytvorený v Jave – umožňuje ho spustiť na všetkých OS
- Open Source
- <http://rsbweb.nih.gov/ij/>

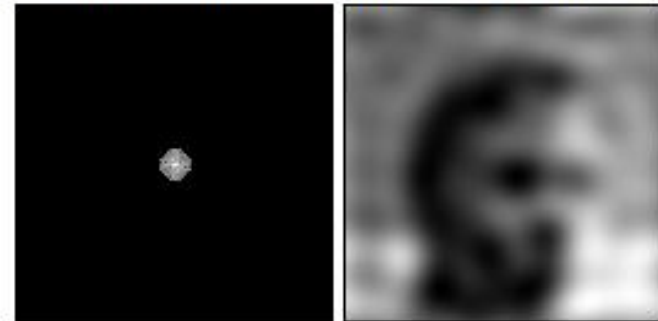


FFT ImageJ

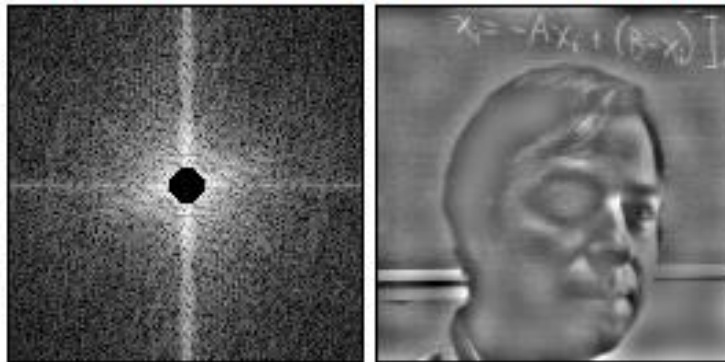
Brightness Image Fourier Transform Inverse Transformed



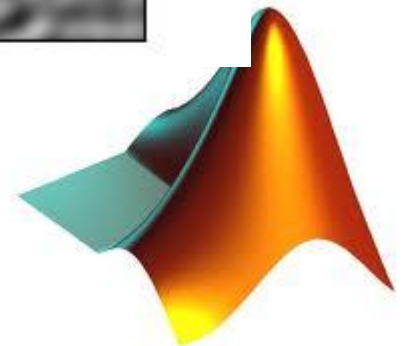
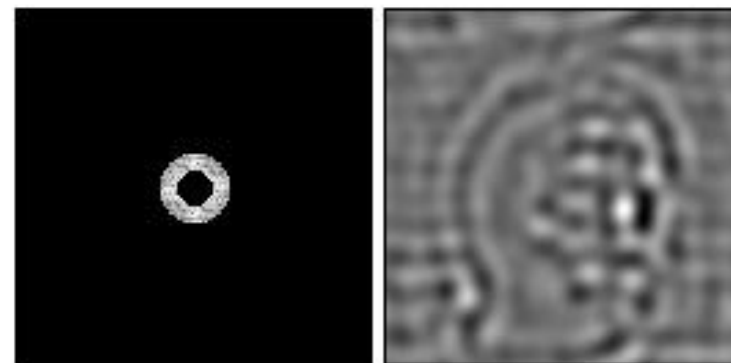
Low-Pass Filtered Inverse Transformed



High-Pass Filtered Inverse Transformed



Band-Pass Filtered Inverse Transformed



DCT

- pre typický obrázok so spojitými prechodmi farieb je väčšina vizuálne najdôležitejších informácií o obrázku koncentrovaná v malom počte kosínusových funkcií nízkych frekvencií
- frekvenčné koeficienty sú reálne

$A = \text{dct2}(B);$

$B = \text{idct2}(A);$

<http://www.mathworks.com/help/toolbox/images/ref/dct2.html>

