

Lecture 4: Relations between Database Schemas

2-AIN-144/2-IKV-131 Knowledge Representation & Reasoning

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Relations between Databases

Multiple Database Setting

In realistic applications more than one **inter-related databases** may be employed.

- Data in the databases may partially overlap
- Constraints may be found inside each database but as well involve multiple databases

Formally, we model these databases by ER schemas $\mathcal{S}_1, \dots, \mathcal{S}_n$. Constraints between elements inside each schema are naturally expressed by IS-A relations, and other ER constraints (**intra-schema relations**). However there can also be constraints between elements from different schemas (**inter-schema relations**).

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- $E_1 =_{\text{int}} E_2$: E_1 and E_2 are **intensionally equivalent** – if \mathcal{S}_i and \mathcal{S}_j referred to the same set of objects, extensions of E_1 and E_2 would be equivalent

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- $E_1 \leq_{\text{int}} E_2$: E_1 is intentionally more specific than E_2 – if S_i and S_j referred to the same set of objects, extension of E_1 would be contained within the extension of E_2

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Inter-Schema Relations (cont.)

Given ER schemas $\mathcal{S}_1, \dots, \mathcal{S}_n$ and their corresponding DB states $\mathcal{B}_1, \dots, \mathcal{B}_n$, the **semantics of inter-schema relations** is as follows:

- $E_1 =_{\text{int}} E_2$ requires $E_1^{\mathcal{B}_i} \cap \Delta^{\mathcal{B}_j} = E_2^{\mathcal{B}_j} \cap \Delta^{\mathcal{B}_i}$
- $E_1 \leq_{\text{int}} E_2$ requires $E_1^{\mathcal{B}_i} \cap \Delta^{\mathcal{B}_j} \subseteq E_2^{\mathcal{B}_j}$
- $E_1 =_{\text{ext}} E_2$ requires $E_1^{\mathcal{B}_i} = E_2^{\mathcal{B}_j}$
- $E_1 \leq_{\text{ext}} E_2$ requires $E_1^{\mathcal{B}_i} \subseteq E_2^{\mathcal{B}_j}$

for any entities E_1 of \mathcal{S}_i and E_2 of \mathcal{S}_j where $1 \leq i, j \leq n$ and $i \neq j$.

Example

Assume ER schemas S_1 (study results information system: students, professors, courses, . . .), S_2 (students' body of academic senate: all senators who are students), S_3 (correspondence seminar organization: allows student and non-student members). We have e.g. the following inter-schema relations:

$$\text{Student}_3 \leq_{\text{ext}} \text{Student}_1$$

$$\text{Senator}_2 \leq_{\text{ext}} \text{Student}_1$$

$$\text{Senator}_2 \leq_{\text{int}} \text{Student}_3$$

Note: in the examples we will always assume that E_j belongs to schema S_j .

Straightforward transformation into DL:

- $S_i \rightsquigarrow \mathcal{T}_{S_i}$
- $E_1 =_{\text{int}} E_2 \rightsquigarrow E_1 \equiv_{\text{int}} E_2$
- $E_1 \leq_{\text{int}} E_2 \rightsquigarrow E_1 \sqsubseteq_{\text{int}} E_2$
- $E_1 =_{\text{ext}} E_2 \rightsquigarrow E_1 \equiv_{\text{ext}} E_2$
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Semantics of inter-schema axioms is analogous: given DL Tboxes $\mathcal{T}_{S_1}, \dots, \mathcal{T}_{S_n}$ and the respective DL interpretations $\mathcal{I}_1, \dots, \mathcal{I}_n$, and some concepts E_1 of \mathcal{T}_{S_i} and E_2 of \mathcal{T}_{S_j} :

- $E_1 \equiv_{\text{int}} E_2$ requires $E_1^{\mathcal{I}_i} \cap \Delta^{\mathcal{I}_j} = E_2^{\mathcal{I}_j} \cap \Delta^{\mathcal{I}_i}$
- $E_1 \sqsubseteq_{\text{int}} E_2$ requires $E_1^{\mathcal{I}_i} \cap \Delta^{\mathcal{I}_j} \subseteq E_2^{\mathcal{I}_j}$
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- $E_1 \sqsubseteq_{\text{ext}} E_2$ requires $E_1^{\mathcal{I}_i} \subseteq E_2^{\mathcal{I}_j}$

In fact only \sqsubseteq_{ext} is necessary and other inter-schema relations can be reduced:

- $E_1 \equiv_{\text{ext}} E_2 \rightsquigarrow E_1 \sqsubseteq_{\text{ext}} E_2 \text{ and } E_2 \sqsubseteq_{\text{ext}} E_1$
- $E_1 \sqsubseteq_{\text{int}} E_2 \rightsquigarrow E_1 \sqcap \top_j \sqsubseteq_{\text{ext}} E_2$
- $E_1 \equiv_{\text{int}} E_2 \rightsquigarrow E_1 \sqsubseteq_{\text{int}} E_2 \text{ and } E_2 \sqsubseteq_{\text{int}} E_1$

for any concepts E_1 of \mathcal{T}_{S_i} , E_2 of \mathcal{T}_{S_j} , and for \top_j the top concept of \mathcal{T}_{S_j} , where $1 \leq i, j \leq n$ and $i \neq j$.

Example (cont.)

Let $\mathcal{S}_1, \dots, \mathcal{S}_3$ be as before and let us have in addition \mathcal{S}_4 (faculty body of academic senate) and \mathcal{S}_5 (financial information system). Thanks to DL can express even more complex inter-schema relations:

$$\text{Senator}_2 \sqsubseteq_{\text{ext}} \neg \text{Senator}_4$$

$$\text{Student}_3 \sqcap \text{Member}_3 \sqsubseteq_{\text{ext}} \exists \text{receives}_5. \text{Scholarship}_5$$

$$\text{Student}_3 \sqcap \text{Member}_3 \sqsubseteq_{\text{ext}} \forall \text{hasGrading}_1. \text{GradeA}_1$$

Cooperative Database Systems

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Formally a CDS is modeled as $(\mathcal{T}_{\mathcal{S}_0}, \mathcal{T}_{\mathcal{S}_1}, \dots, \mathcal{T}_{\mathcal{S}_n}, \Sigma)$ where:

- $\mathcal{T}_{\mathcal{S}_1}, \dots, \mathcal{T}_{\mathcal{S}_n}$ represent $\mathcal{S}_1, \dots, \mathcal{S}_n$
- $\mathcal{T}_{\mathcal{S}_0}$ represents common knowledge, which can also be empty
- Σ contains inter-schema axioms, typically between any pair of $\mathcal{T}_{\mathcal{S}_0}, \dots, \mathcal{T}_{\mathcal{S}_n}$

A model of a CDS consists of $n + 1$ DL interpretations $(\mathcal{I}_0, \dots, \mathcal{I}_n)$ s.t. $\mathcal{I}_i \models \mathcal{T}_{\mathcal{S}_i}$ for $i \geq 0$ and $\Delta^{\mathcal{I}_i} \subseteq \Delta^{\mathcal{I}_0}$ for $i > 0$.

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CDS allow e.g. to check and maintain global consistency of databases used inside an organization/application.

Database Schema Integration

Integrated Database Schemas

In integrated database schemas (IDS) we deal with n ER schemas $\mathcal{S}_1, \dots, \mathcal{S}_n$ which are integrated into a global (enterprise) schema \mathcal{S}_0 using inter-schema relations.

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IDS allow esp. to express a unified view and unified query interface over multiple databases.

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- 2 Calvanese, D., De Giacomo, G., Lenzerini, M., Nardi, D., Rosati, R.: Description logic framework for information integration. In: KR 1998, Morgan Kaufmann 1998.
- 3 Calvanese, D., Lenzerini, M., Nardi, D.: Unifying class-based representation formalisms. J. Artif. Intell. Res. (JAIR) 11, 199-240, 1999
- 4 Catarci, T., Lenzerini, M.: Representing and using interschema knowledge in cooperative information systems. Int. J. Cooperative Inf. Syst. 2(4), 375-398, 1993.

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