Clipping

Lesson

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Outline of Lesson 06

- * Line clipping algorithms in the CG Pipeline
- Cohen-Sutherland
- * Cyrus-Beck
- Nicholl-Lee-Nicholl

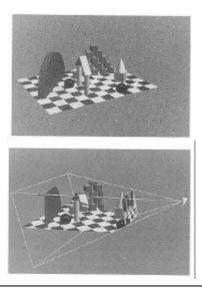
Transformations

• Scene composition

- World space

Viewing frustrum

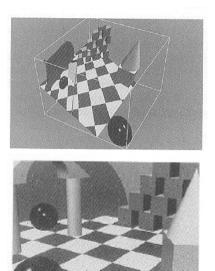
- Eye position, orientation



Transformation

• 3D Screen space

- Clipped to frustrum
- Distortion towards far clipping plane
- Z-buffer occlusion detection
- Projection to 2D



Where Culling & Clipping Fit In

Scene Database

Culling

Lighting

View Transform

Clipping

Map to Viewport

Rasterization

Video Out

- •Goal #1: Reject objects as early as possible
 - this will save the most work
- •Goal #2: Rejection test must be efficient – we're trying to avoid work

•Generally perform culling early on

- remove objects wholly outside frustum
- avoids lighting & transformation

And perform clipping later on

- cut off parts outside viewport
- simplifies rasterization

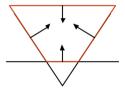
Data

View Frustum Culling

- Discard any object outside viewing volume early on
 - performed by application (or application framework)
- Viewing volume is formed by 6 planes
 - suppose all normals are oriented towards interior
 - then the interior is set of all points such that

 $a_i x + b_i y + c_i z + d_i \ge 0$

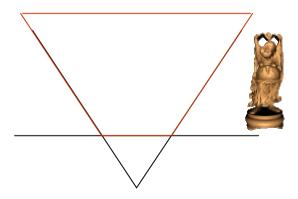
- Given a set of polygons
 - test for intersection with viewing volume
 - any polygon not intersecting frustum can be culled
- What's wrong with this simple algorithm?



Inefficient Per-Polygon Processing

•What if a million polygon object is entirely outside frustum?

-we certainly don't want to test every one!



Culling with Bounding Volumes

•Let's enclose our object in a convex volume

- -bounding sphere
 - compact representation
 - may not fit object tightly
- -bounding box
 - · axis-aligned or oriented with object
- -convex polytope
 - · allows tightest fit
 - · most expensive to deal with

•Now test bounding volume first

- -if outside frustum, reject object
- -otherwise visit individual components



Hierarchical Bounding Volumes

•And we can do even better with a hierarchy of volumes

•Begin testing at the root node

- if outside, reject all objects
- otherwise, recursively test sub-nodes

•Of course this raises the question: how best to build this hierarchy?





CG-1 WS03/04

Backface Culling

•Even for polygons inside frustum, some may be culled

-if we assume that our objects are closed

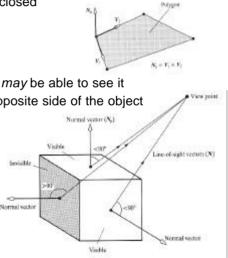
Consider polygon normal

 $N_P = V_1 \mathbf{X} V_2$

- -Oriented polygon edges V_1 , V_2
- -if it's pointing towards the eye, we may be able to see it
- -pointing away means it's on the opposite side of the object

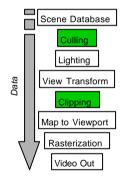
•Line-of-sight vector N

- $N_P \bullet N$
- > 0 : surface visible
- < 0 : surface not visible
- \Rightarrow Draw only visible surfaces

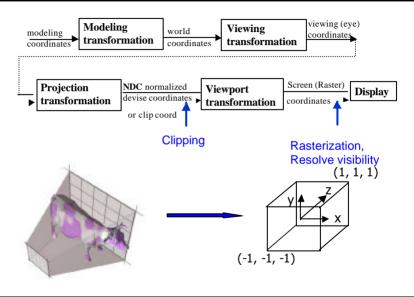


From Culling to Clipping

- Culling tries to reject objects wholly outside viewing volume
 - -typically done by application
 - -happens prior to lighting, transformation, ...
- Now, we want to cut off pieces outside frustum
 - -this is clipping
- Clipping happens just prior to rasterization
 - -almost always done by graphics system
 - -frequently implemented in hardware



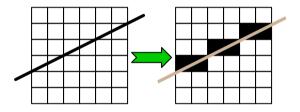
Transformations & Clipping



CG-1 WS03/04

Why not Per-Pixel Clipping during Rasterization?

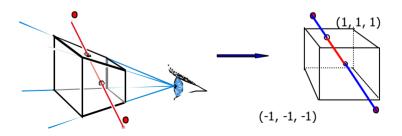
- During rasterization, we visit every pixel covered by primitive
 - -if any pixel is outside the viewport, reject it



- What's wrong with this?
- It can be pretty inefficient
 - -suppose a 1000 pixel polygon is completely outside viewport

Clipping

- After the mapping of the view volume (a frustum for perspective views; parallelepiped for orthographic views) to the canonical view volume. All vertices are in NDC.
- Primitives not within the canonical view volume are to be clipped. Clipping is more efficient and faster when carried out with NDC.



Point Clipping (Culling)

- In 3D view space
- Vertex inside canonical view frustrum ?
 - OpenGL: x,y,z [-1...1]
 - Direct3D: x,y [-1...1], z [0...1]

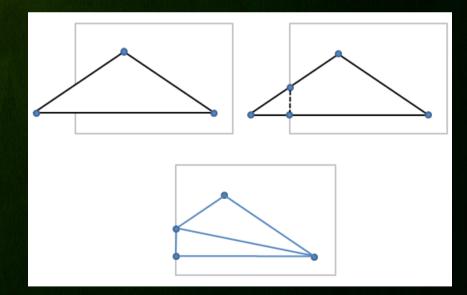
The CG Pipeline Geometry Postprocessing

Geometry Postprocessing, Rasterization

Fragments

 During geometry postprocessing lines and triangles are clipped against the window

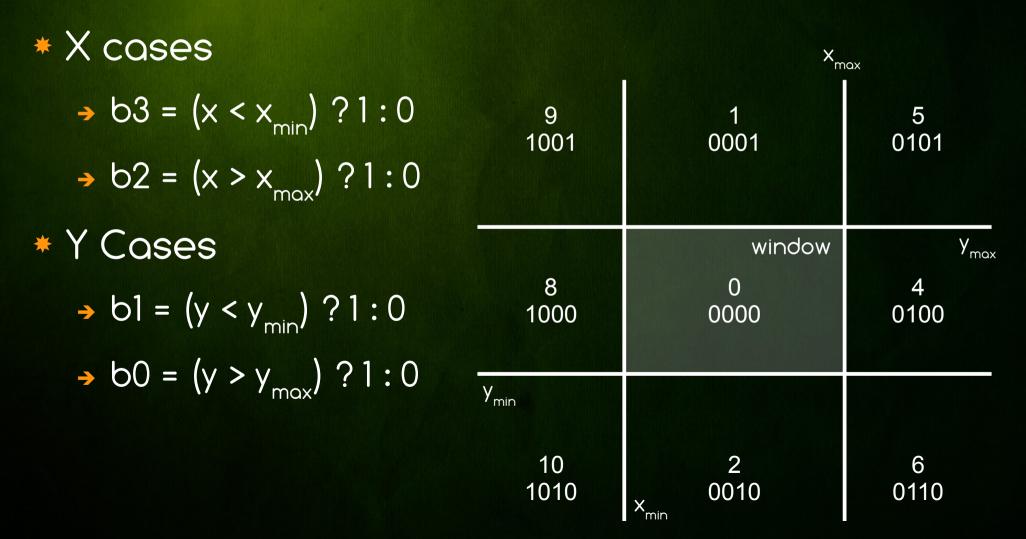
- We can not write outside the frame buffer
- Clipping should be
 - Fast for many primitives
 - Implemented on HW (GPU)



Main Purpose

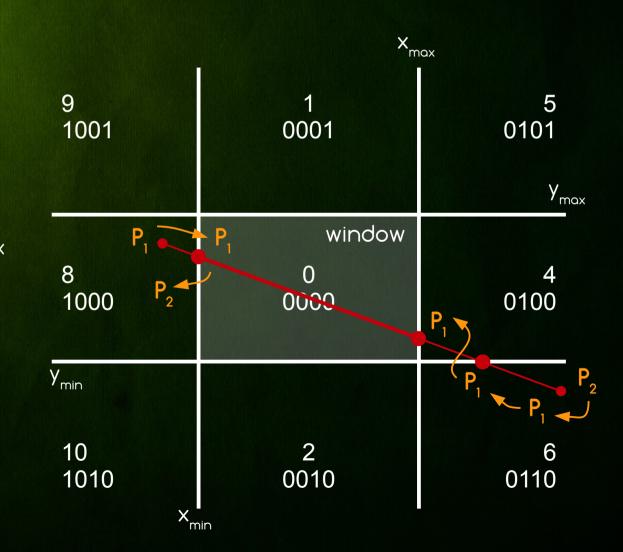
- Clipping lines against rectangular (axis aligned)
 2D(3D) window
- * Algorithm Principle
 - Divides a 2D (3D) space into 9 (27) regions
 - Efficiently determine the (portions of) lines that are visible in the window
 - Clip lines against window edges

* 9 codes (4bit) for each region: code = $b_3 b_2 b_1 b_0$



* Execution example

- Clip P₁ against x_{min}
- \rightarrow Swap P₁ and P₂
- → Clip P₁ against y_{min}
- Olip P1 against xmax
- Done with P1P2



```
c2 = code(x2, y2);
while (false) {
    c1 = code(x1, y1);
    if (c1 & c2 != 0) return false;
    else if (c1 | c2 == 0) return true;
    else {
         if (c1 == 0) { swap(x1, x2); swap(y1, y2); swap(c1, c2); }
         else if (c1 \in \{1, 5, 9\}) { x1 = x1 + (x2-x1) * (y<sub>mox</sub>-y1) / (y2-y1); y1 = y<sub>mox</sub>; }
         else if (c1 \in \{2, 6, 10\}) { x1 = x1 + (x2-x1) * (y<sub>min</sub>-y1) / (y2-y1); y1 = y<sub>min</sub>; }
         else if (c1 \in \{4, 5, 6\}) \{ y1 = y1 + (y2-y1)^* (x_{max} - x1) / (x2-x1); x1 = x_{max}; \}
         else if (c1 \in \{8, 9, 10\}) \{ y1 = y1 + (y2-y1)^* (x_{min}-x1) / (x2-x1); x1 = x_{min}; \}
```

Main Purpose

Clipping lines against any convex polygon

* Algorithm Principle

- Find line parameter of intersection with each edge of polygon
- Update min and max line parameter to be inside the halfspace of each edge
- If min < max calculate clipped line segment points</p>

Intersection of hyperplane and line segment

- Hyperplane (origin O, normal n)
- Line segment (start point P0, end point P1)

* P lies on line segment

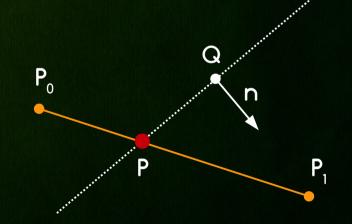
→ P = PO + t(P1 - PO) | 0 <= t <= 1
</p>

* P lies on hyperplane

→ (P - Q) * n = 0

Solve t = (Q-P0) *n / (P1-P0) *n

→ dq = (Q-P0) *n | d1 = (P1-P0) *n →



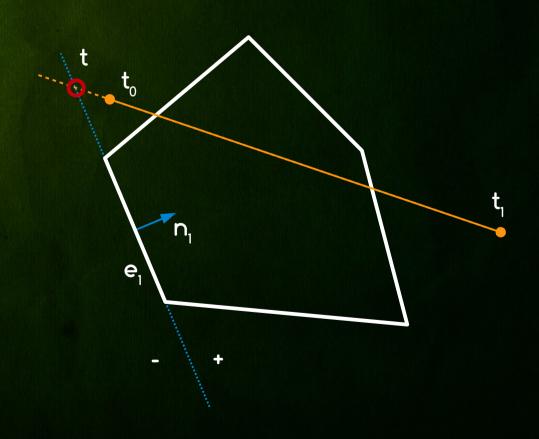
- Instead of calculating new intersected points Cyrus-Beck operates only on line parameters t0 and t1 - this is faster
- * First set t0 = 0 and t1 = 1 (original line segment)
- For each edge find intersection parameter t and set
 - → If (d1 > 0) t0 = max(t, t0) (out-to-in case)
 - → If (d1 < 0) t1 = min(t,t1) (in-to-out case)</p>
- * This will find the smallest intersection interval
- * At the end find new P0 and P1 for t0 and t1

- Input: Convex polygon and line segment
- Output: Clipped line segment being fully inside given polygon (or nothing)

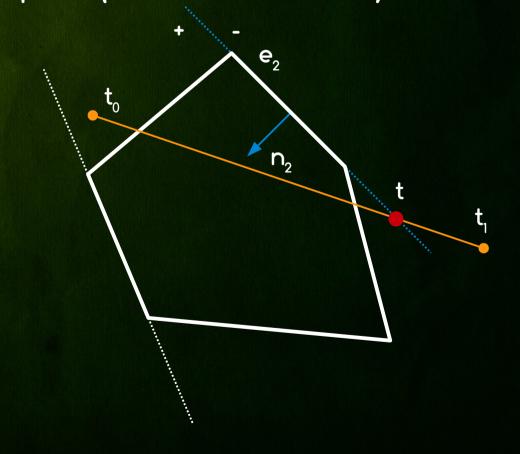
Set clipping parameters
t0 = 0, t1 = 1



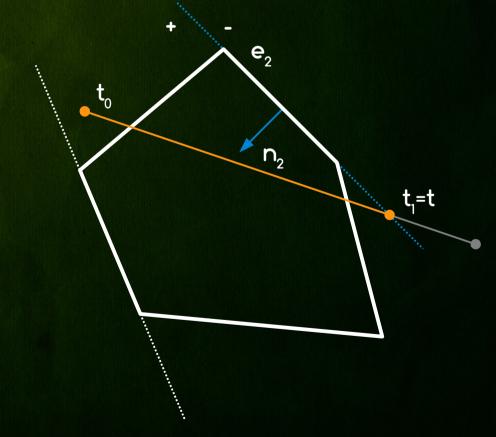
- * Find intersection parameter t with edge e1
- * d1 = (P1-P0) * n1 > 0 \rightarrow clip t0 (out-to-in case)
- * t0 = max(t,t0)
 - Since t < t0</p>
 - No update is done



★ Find intersection parameter t with edge e2
 ★ d1 = (P1-P0) * n2 < 0 → clip t1 (in-to-out case)

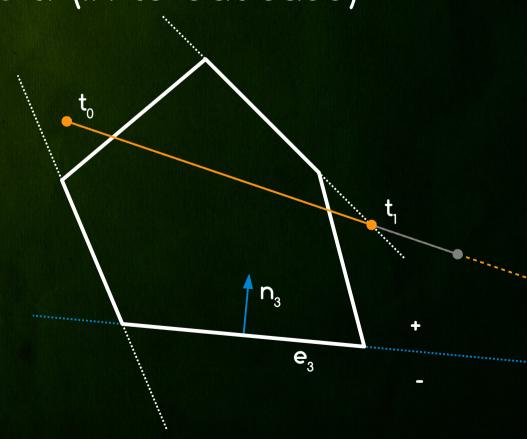


- * Find intersection parameter t with edge e2
- * d1 = (P1-P0) *n2 < 0 → clip t1 (in-to-out case)
- * t1 = min(t,t1)
 - Since t < t1</p>
 - We update t1 = t

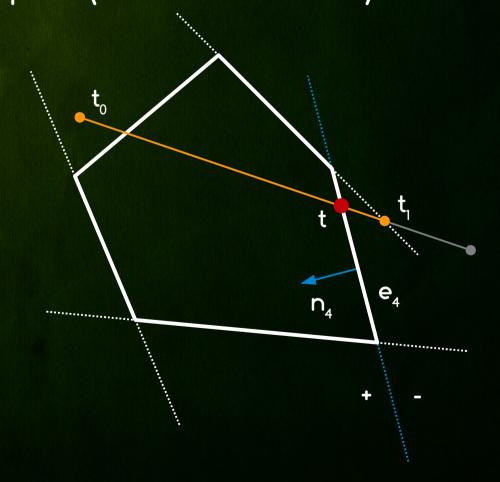


Liang-Barsky

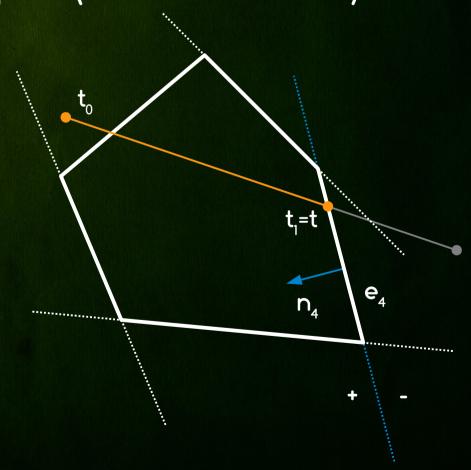
- * Find intersection parameter t with edge e3
- * d1 = (P1-P0) *n3 < 0 → clip t1 (in-to-out case)
- * t1 = min(t,t1)
 - Since t > t1
 - No update is done



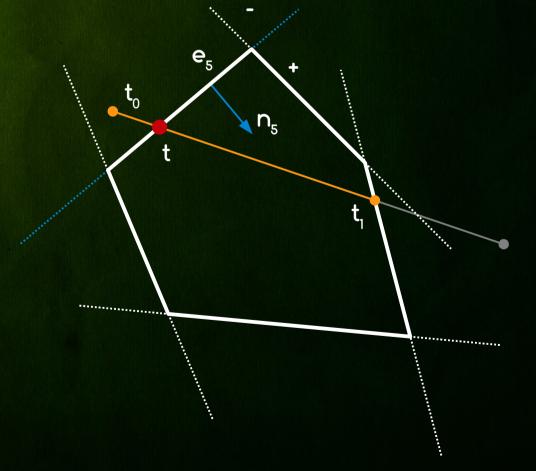
★ Find intersection parameter t with edge e4
 ★ d1 = (P1-P0) * n4 < 0 → clip t1 (in-to-out case)



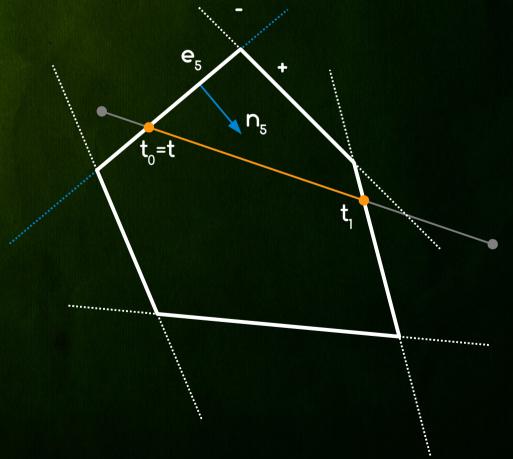
- * Find intersection parameter t with edge e4
- * d1 = (P1-P0) *n4 < 0 → clip t1 (in-to-out case)
- * t1 = min(t,t1)
 - Since t < t1</p>
 - We update t1 = t



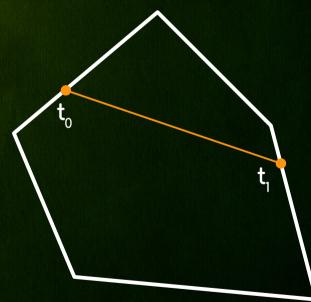
- * Find intersection parameter t with edge e5
- * d1 = (P1-P0) * $n5 > 0 \rightarrow clip t0$ (out-to-in case)



- * Find intersection parameter t with edge e5
- * d1 = (P1-P0) * $n5 > 0 \rightarrow clip t0$ (out-to-in case)
- * t0 = max(t,t0)
 - Since t > t0
 - → We update t0 = t



- * No more edges to update with
- If t0 > t1 whole line segment is outside of polygon
- If t0 <= t1 clip line</p>
 - → PO' = PO + tO (P1-PO)
 - → P1' = P0 + t1(P1-P0)



★ t₀ = 0; t₁ = 1;

*

* foreach edge $e_i = (q_i, n_i) \{$

$$d_1 = (\rho_1 - \rho_0)^* n_i; \quad d_q = (q_i - \rho_0)^* n_i;$$

- → if (d₁>0) { t = d₀/d₁; t₀ = max(t, t₀); } else
- → if $(d_1 < 0)$ { t = d_q/d_1 ; t₁ = min(t, t₁); } else

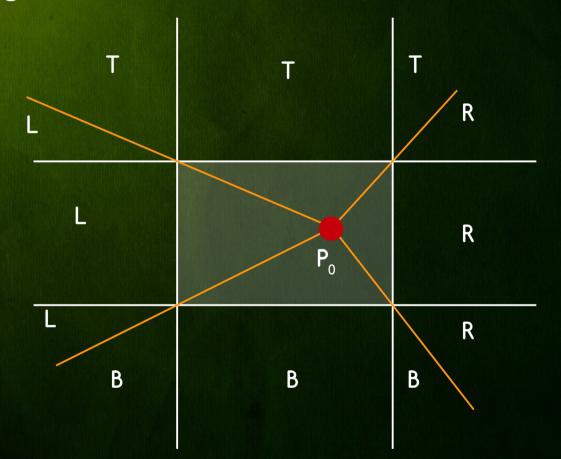
 \rightarrow if $((\rho_0 - q_i)^* n_i < 0)$ return false; // line is outside of poly

* if $(t_0 < t_1)$ return true; else return false;

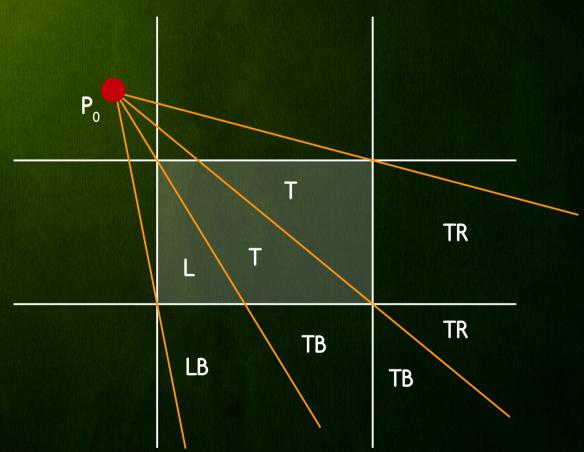
Main Purpose

- Clipping lines against rectangular (axis aligned) 2D only window
- * Algorithm Principle
 - Categorize first point of line segment similarly to Cohen-Sutherland
 - Virtual cast 4 rays from P0 through 4 corners of window and categorize all regions between rays.
 In each segment we know which window edges we have to clip with
 - Clip line segment with selected edges

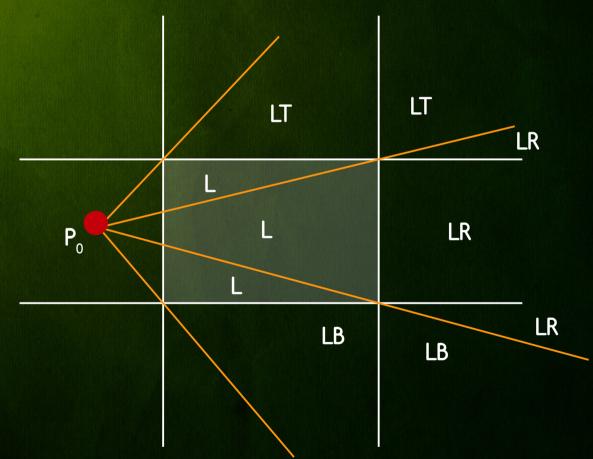
Window region



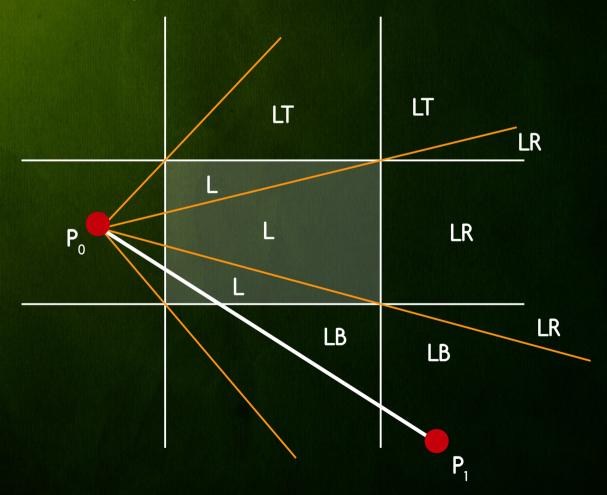
Corner region



* Edge region



* Edge region Example



procedure LeftEdgeRegionCase (ref real x1, y1, x2, y2; ref boolean visible) begin

```
real dx, dy;
```

end:

```
if x^2 < xmin
    then visible := false
    else if y2 < ymin
        then LeftBottom (xmin,ymin,xmax,ymax,x1,y1,x2,y2,visible)
        else if y2 > ymax
             then
                 begin
                     { Use symmetry to reduce to LeftBottom case }
                     y_1 := -y_1; y_2 := -y_2; \{ \text{ reflect about x-axis } \}
                     LeftBottom (xmin,-ymax,xmax, -ymin,x1,y1,x2,y2,visible);
                     y1 := -y1; y2 := -y2; \{ reflect back \}
                 end
             else
                 begin
                     dx := x^2 - x^1; dy := y^2 - y^1;
                     if x^2 > xmax then
                          begin
                              y_2 := y_1 + dy^*(x_max - x_1)/dx; \quad x_2 := x_max;
                         end:
                     y_1 := y_1 + dy^*(x_{min} - x_1)/dx; \quad x_1 := x_{min};
                     visible := true:
                 end
```

```
procedure LeftBottom (
                            real xmin, ymin, xmax, ymax;
                        ref real x1, y1, x2, y2; ref boolean visible)
begin
    real dx, dy, a, b, c;
    dx := x^2 - x^1; dy := y^2 - y^1;
    a := (xmin - x1)^*dy; b := (ymin - y1)^*dx;
   if b > a
       then visible := false { (x^2, y^2) is below ray from (x^1, y^1) to bottom left corner }
       else
           begin
               visible := true:
               if x^2 < xmax
                   then
                       begin x_2 := x_1 + b/dy; y_2 := y_{min}; end
                   else
                       begin
                           c := (xmax - x1)^*dy;
                           if b > c
                               then { (x2,y2) is between rays from (x1,y1) to
                                       bottom left and right corner }
                                   begin x^2 := x^1 + b/dy; y^2 := ymin; end
                               else
                                   begin y_2 := y_1 + c/dx; x_2 := xmax; end
                       end:
           end:
    y1 := y1 + a/dx; x1 := xmin;
end:
```

Clipping Algorithms Summary

- * Cohen-Sutherland
 - Repeated clipping is expensive
 - Best when trivial accepts/rejects occur often

- Cheap intersection parameter calculation
- Points are clipped only once at the and
- Best when most lines have to be clipped
- * Liang-Barsky optimized Cyrus-Beck for window
- * Nicholl et. al. Fastest, not applicable in 3D

