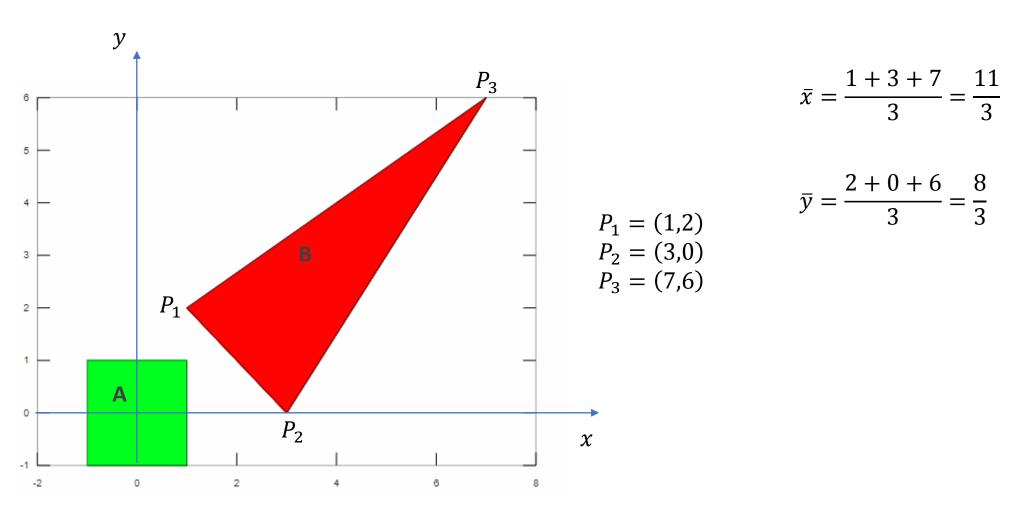


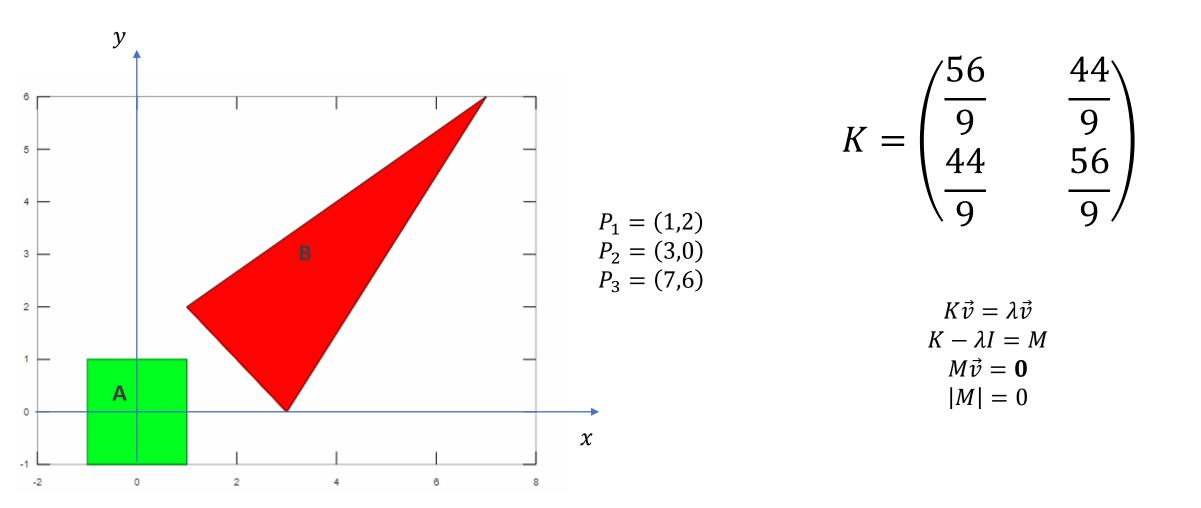
$$K = \begin{pmatrix} \operatorname{cov}(x, y) & \operatorname{cov}(x, y) \\ \operatorname{cov}(x, y) & \operatorname{cov}(y, y) \end{pmatrix}$$

$$\operatorname{cov}(x,y) = \frac{1}{n} \sum_{i=1}^{n} (x - \bar{x})(y - \bar{y})$$



$$\begin{aligned} \cos(x,x) &= \frac{1}{3} \left[ \left( 1 - \frac{11}{3} \right)^2 + \left( 3 - \frac{11}{3} \right)^2 + \left( 7 - \frac{11}{3} \right)^2 \right] = \frac{(-8)^2 + (-2)^2 + 10^2}{3 \cdot 3^2} = \frac{56}{9} \\ P_1 &= (1,2) \\ P_2 &= (3,0) \\ P_3 &= (7,6) \end{aligned}$$
$$\begin{aligned} \cos(x,y) &= \cos(y,x) &= \frac{1}{3} \left[ \left( 1 - \frac{11}{3} \right) \left( 2 - \frac{8}{3} \right) + \left( 3 - \frac{11}{3} \right) \left( 0 - \frac{8}{3} \right) + \left( 7 - \frac{11}{3} \right) \left( 6 - \frac{8}{3} \right) \right] = \frac{44}{9} \\ \cos(y,y) &= \frac{1}{3} \left[ \left( 2 - \frac{8}{3} \right)^2 + \left( 0 - \frac{8}{3} \right)^2 + \left( 6 - \frac{8}{3} \right)^2 \right] = \frac{(-2)^2 + (-8)^2 + 10^2}{3 \cdot 3^2} = \frac{56}{9} \end{aligned}$$
$$\begin{aligned} \overline{y} &= \frac{2 + 0 + 6}{2} = \frac{8}{2} \end{aligned}$$

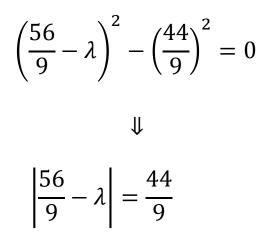
$$\frac{1}{3} = \frac{1}{3}$$

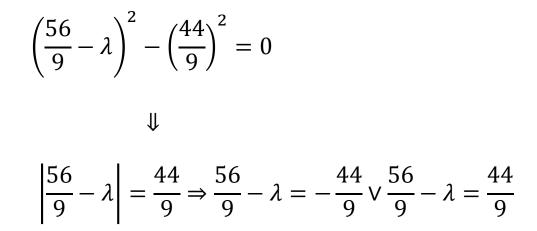


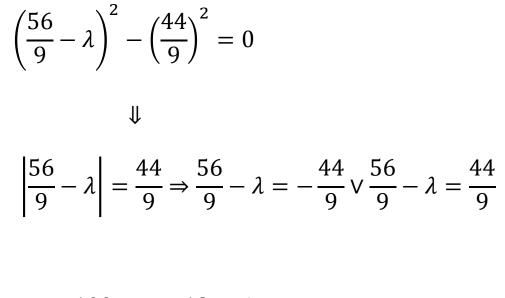
$$|M| = \begin{vmatrix} \frac{56}{9} - \lambda & \frac{44}{9} \\ \frac{44}{9} & \frac{56}{9} - \lambda \end{vmatrix} = \left(\frac{56}{9} - \lambda\right)^2 - \left(\frac{44}{9}\right)^2$$

$$|M| = 0 \Rightarrow \frac{56^2}{9^2} - \frac{112\lambda}{9} + \lambda^2 - \frac{44^2}{9^2} = 0$$

$$\lambda_{1,2} = \frac{-\left(-\frac{112}{9}\right) \pm \sqrt{\left(-\frac{112}{9}\right)^2 - 4\frac{56^2 - 44^2}{81}}}{2}$$







$$\lambda_1 = \frac{100}{9}; \lambda_2 = \frac{12}{9} = \frac{4}{3}$$

$$\lambda_1 = \frac{100}{9}: \qquad (K + \lambda_1 I) \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$\lambda_2 = \frac{4}{3}: \qquad (K + \lambda_2 I) \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$\lambda_{1} = \frac{100}{9}:$$

$$\begin{pmatrix} \frac{56-100}{9} & \frac{44}{9} \\ \frac{44}{9} & \frac{56-100}{9} \end{pmatrix} \binom{x}{y} = \binom{0}{0} \Rightarrow \begin{pmatrix} \frac{56}{9} - \frac{100}{9} \end{pmatrix} x + \frac{44}{9} y = 0 \Rightarrow x = y \Rightarrow \overrightarrow{v_{1}} = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \Rightarrow 44x - 44y = 0$$

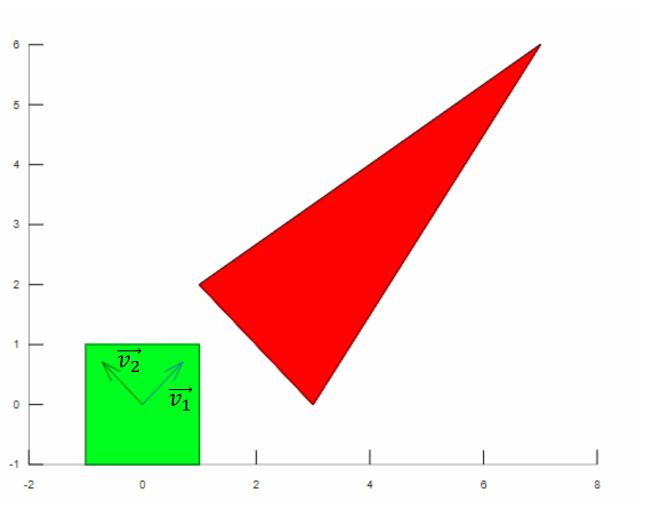
$$\lambda_2 = \frac{4}{3}$$
:  $(K + \lambda_2 I) \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$ 

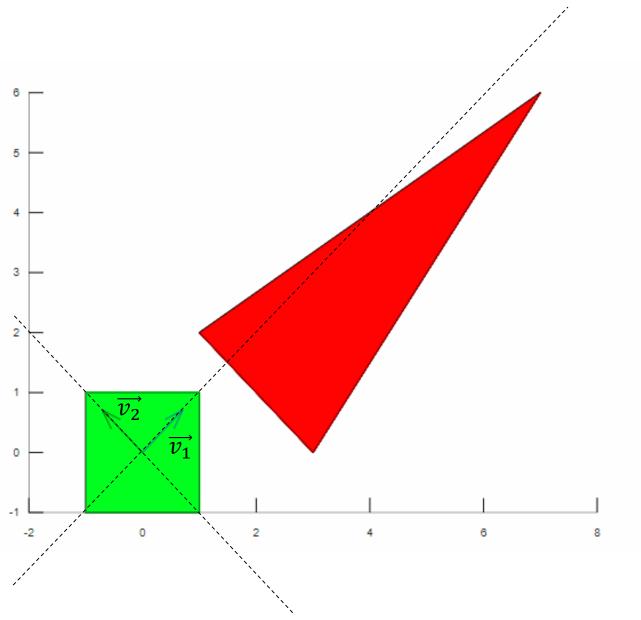
$$\lambda_{1} = \frac{100}{9}:$$

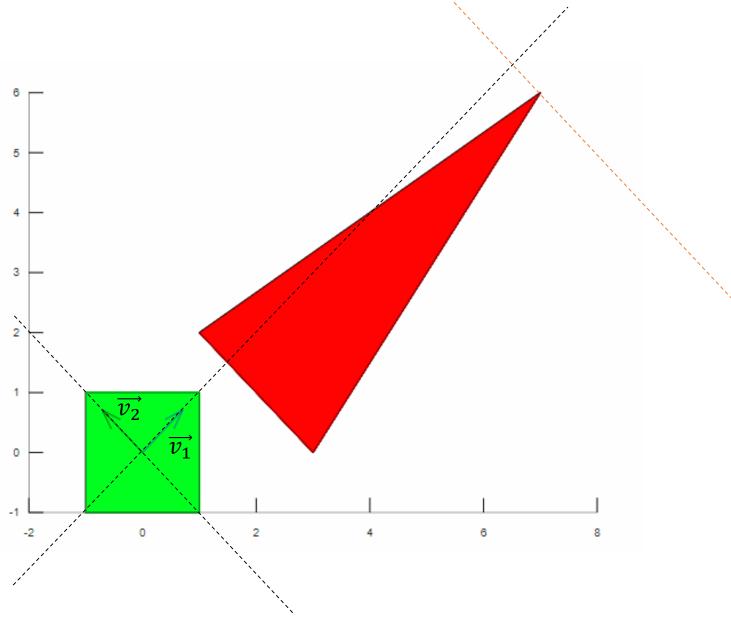
$$\begin{pmatrix} \frac{56-100}{9} & \frac{44}{9} \\ \frac{44}{9} & \frac{56-100}{9} \end{pmatrix} \binom{x}{y} = \binom{0}{0} \Rightarrow \frac{\binom{56}{9} - \frac{100}{9}}{44x - 44y = 0} \Rightarrow \quad x = y \quad \Rightarrow \quad \overrightarrow{v_{1}} = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$

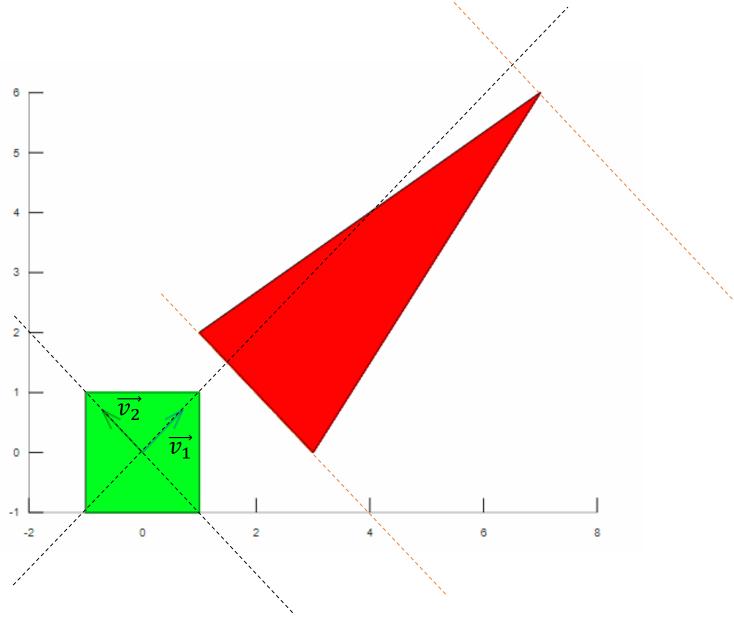
$$\lambda_{2} = \frac{4}{3}:$$

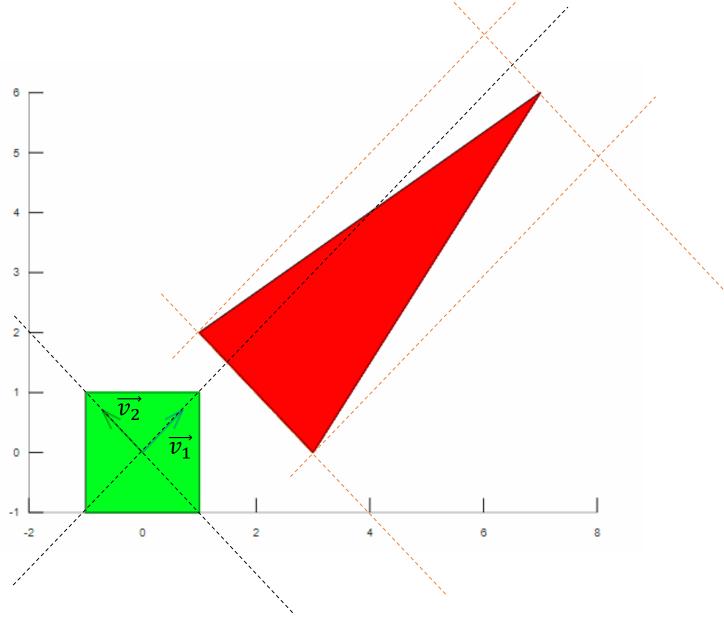
$$\begin{pmatrix} \frac{56-12}{9} & \frac{44}{9} \\ \frac{44}{9} & \frac{56-12}{9} \end{pmatrix} \binom{x}{y} = \binom{0}{0} \Rightarrow \frac{\binom{56}{9} - \frac{12}{9}}{44x + 44y = 0} \Rightarrow \quad -x = y \quad \Rightarrow \quad \overrightarrow{v_{2}} = \left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$



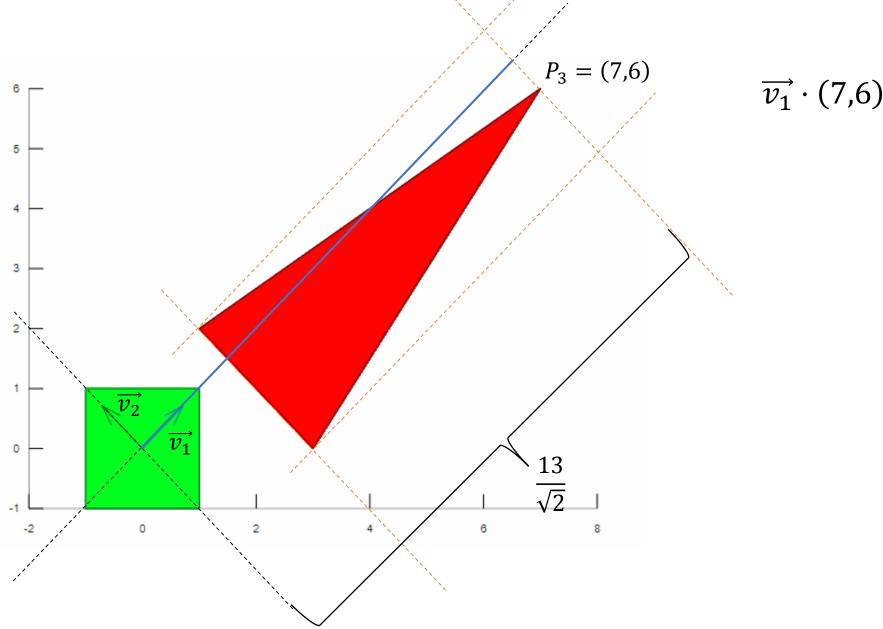




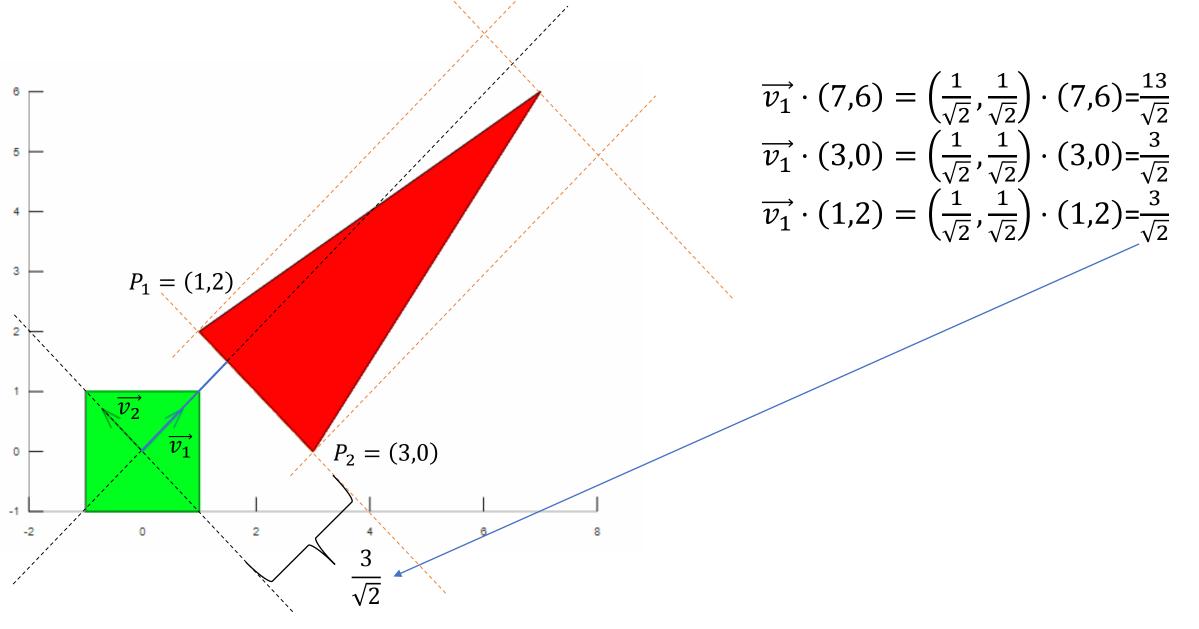


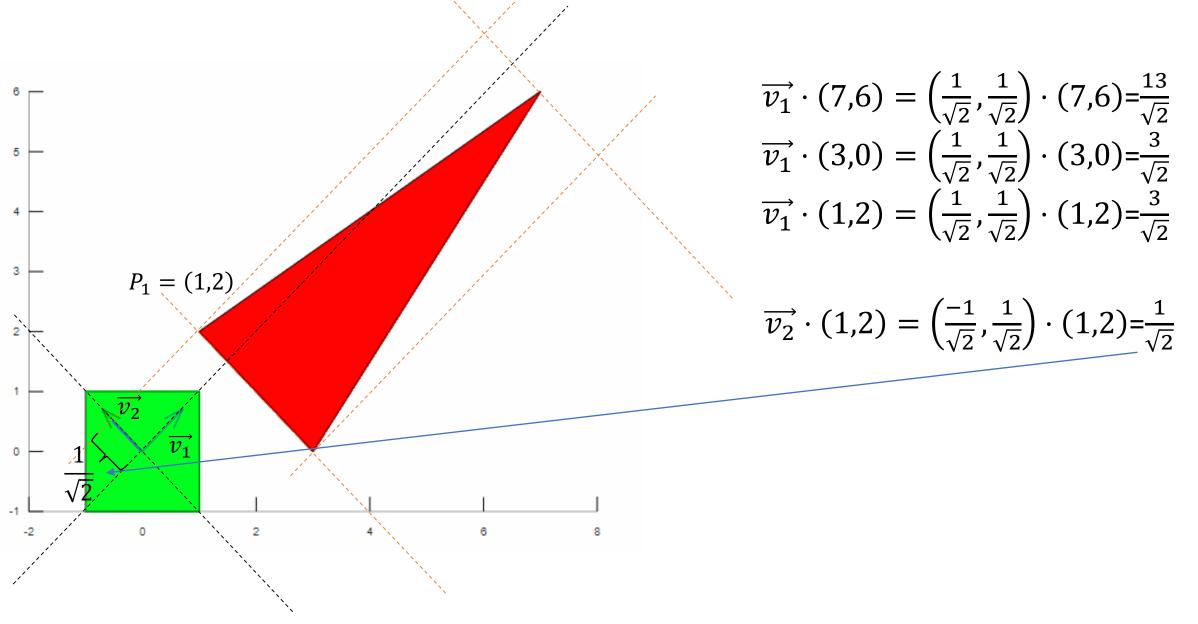


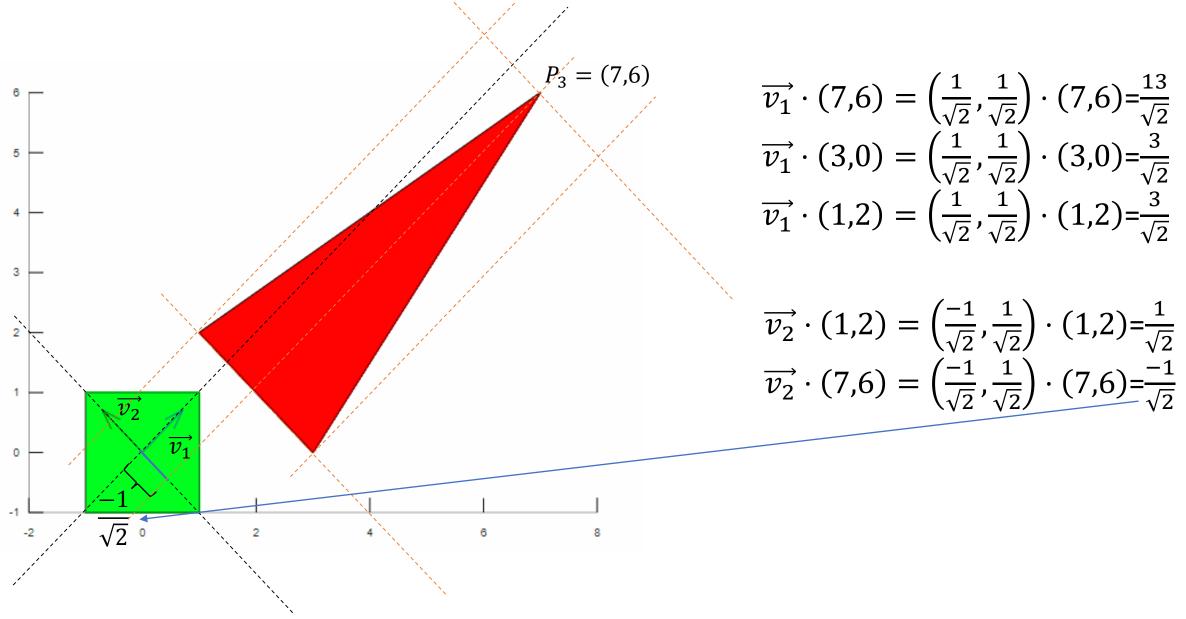
**Separating Axis Theorem** 

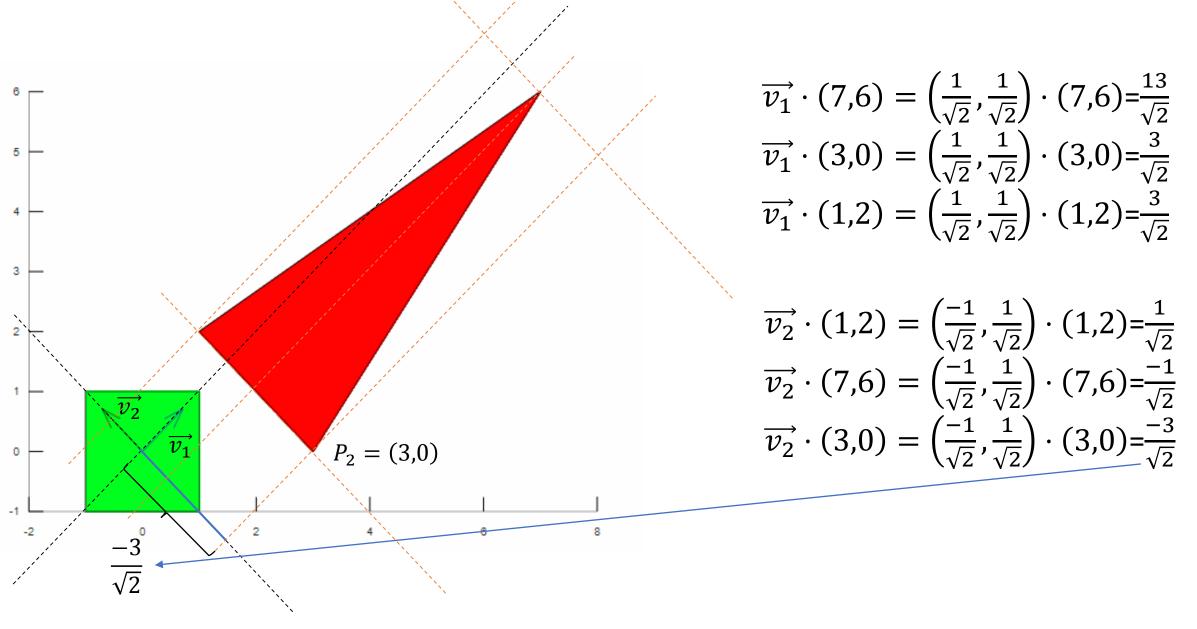


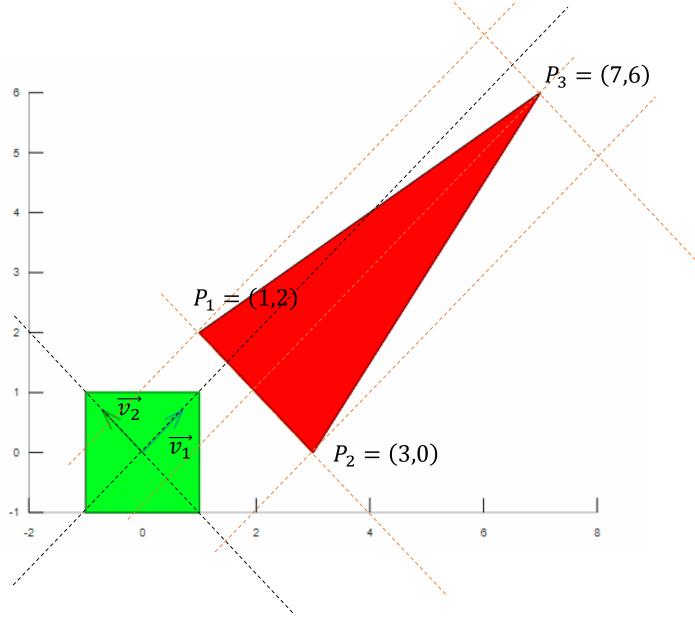
$$\overrightarrow{v_1} \cdot (7,6) = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot (7,6) = \frac{13}{\sqrt{2}}$$







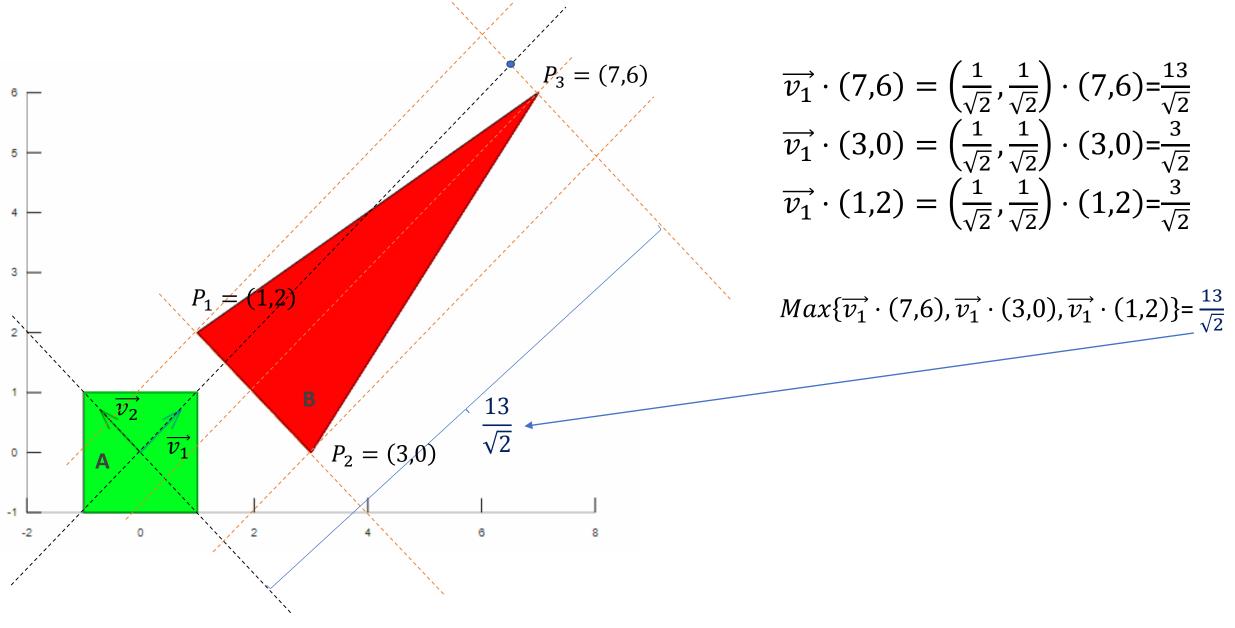




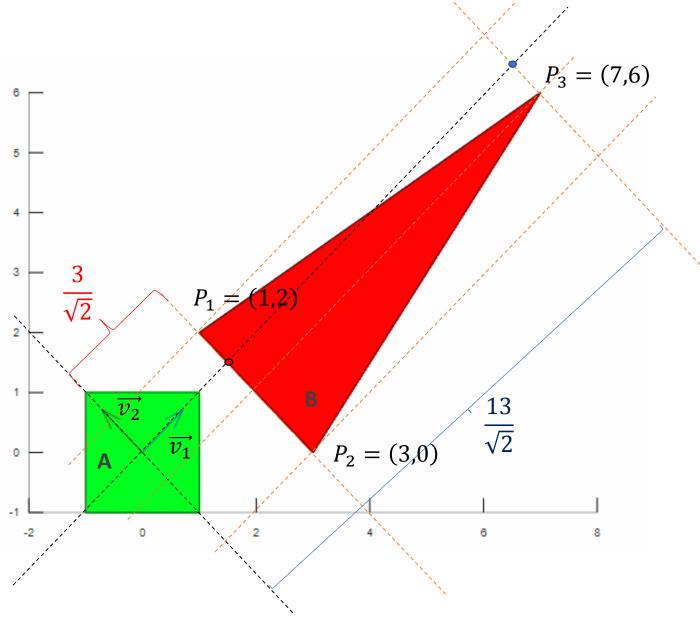
$$\overrightarrow{v_1} \cdot (7,6) = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot (7,6) = \frac{13}{\sqrt{2}}$$
$$\overrightarrow{v_1} \cdot (3,0) = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot (3,0) = \frac{3}{\sqrt{2}}$$
$$\overrightarrow{v_1} \cdot (1,2) = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot (1,2) = \frac{3}{\sqrt{2}}$$

 $Max\{\overrightarrow{v_1} \cdot (7,6), \overrightarrow{v_1} \cdot (3,0), \overrightarrow{v_1} \cdot (1,2)\}=?$ 

**Separating Axis Theorem** 

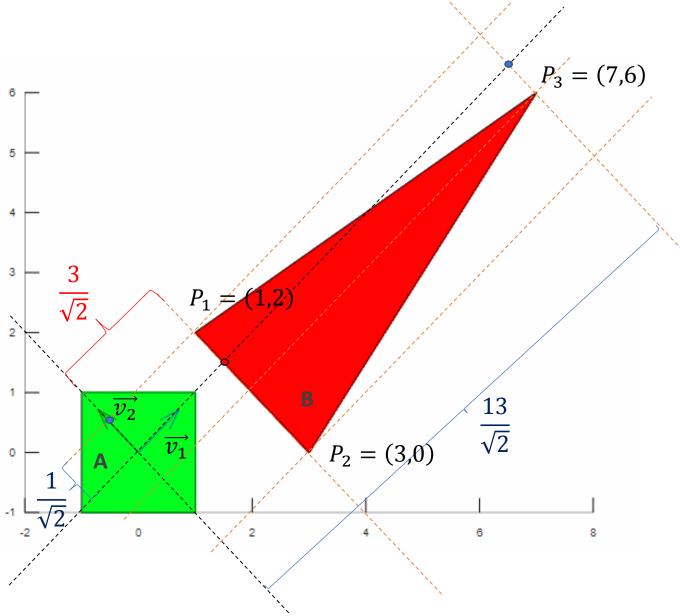


**Separating Axis Theorem** 



$$\overrightarrow{v_1} \cdot (7,6) = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot (7,6) = \frac{13}{\sqrt{2}}$$
$$\overrightarrow{v_1} \cdot (3,0) = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot (3,0) = \frac{3}{\sqrt{2}}$$
$$\overrightarrow{v_1} \cdot (1,2) = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot (1,2) = \frac{3}{\sqrt{2}}$$

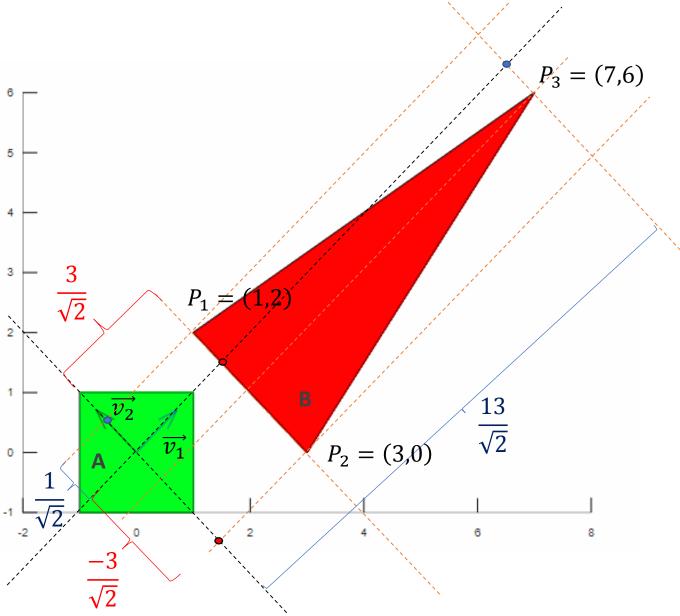
$$Max\{\vec{v_{1}} \cdot (7,6), \vec{v_{1}} \cdot (3,0), \vec{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$$
$$Min\{\vec{v_{1}} \cdot (7,6), \vec{v_{1}} \cdot (3,0), \vec{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$$



 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$ 

$$\overrightarrow{v_{2}} \cdot (1,2) = \left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot (1,2) = \frac{1}{\sqrt{2}}$$
$$\overrightarrow{v_{2}} \cdot (7,6) = \left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot (7,6) = \frac{-1}{\sqrt{2}}$$
$$\overrightarrow{v_{2}} \cdot (3,0) = \left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot (3,0) = \frac{-3}{\sqrt{2}}$$

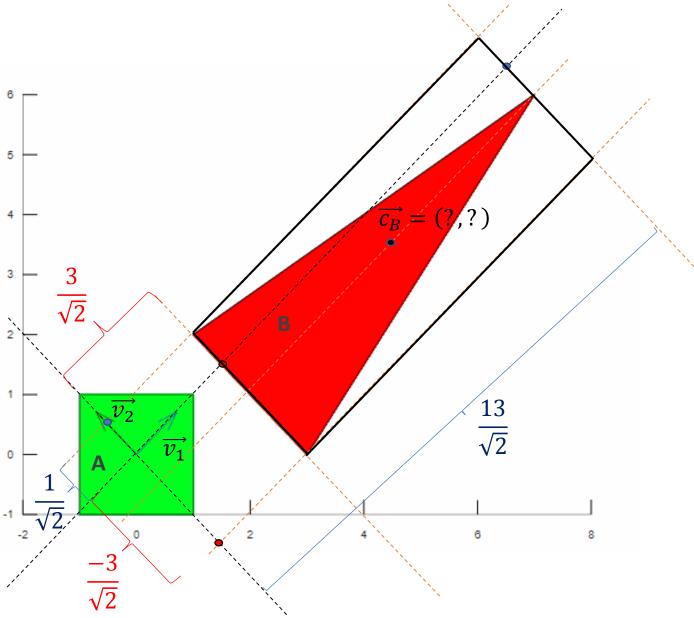
 $Max\{\overrightarrow{v_2} \cdot (7,6), \overrightarrow{v_2} \cdot (3,0), \overrightarrow{v_2} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$ 



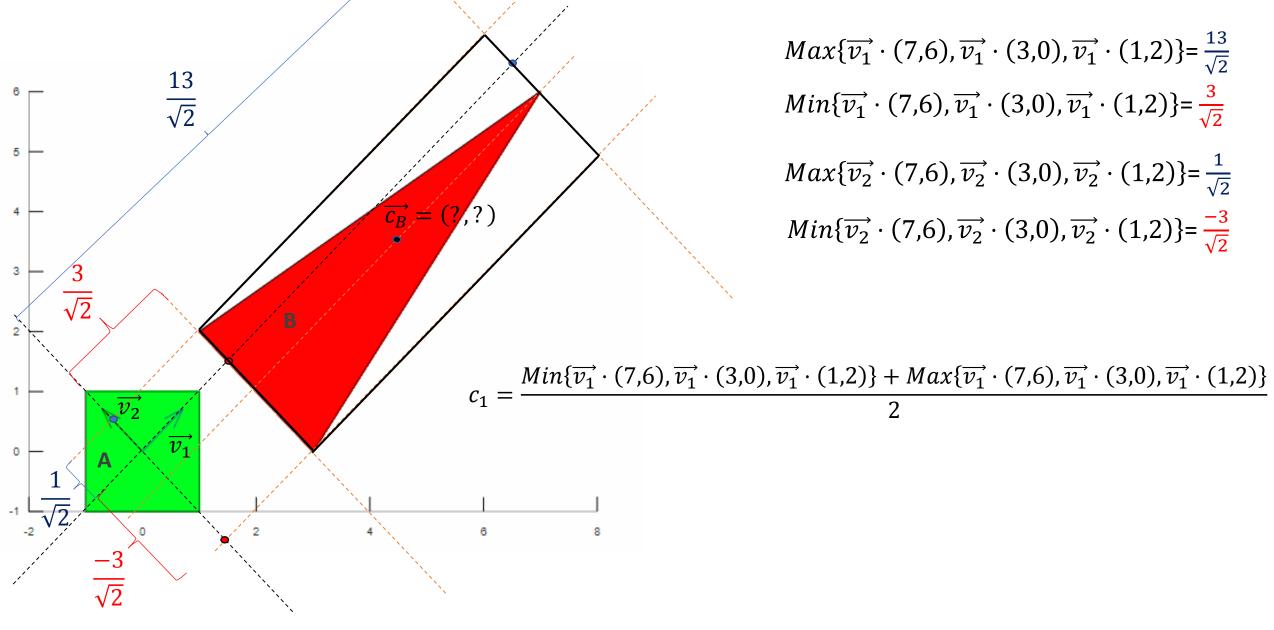
 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$ 

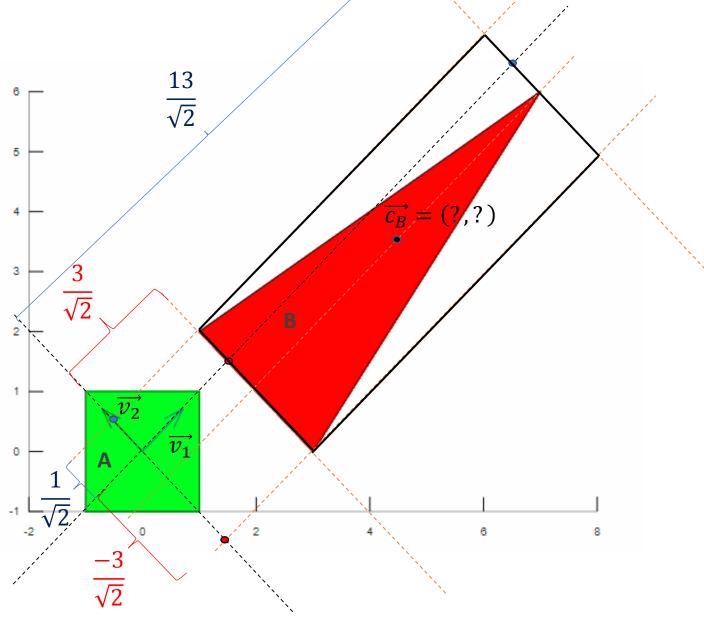
$$\overrightarrow{v_{2}} \cdot (1,2) = \left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot (1,2) = \frac{1}{\sqrt{2}}$$
$$\overrightarrow{v_{2}} \cdot (7,6) = \left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot (7,6) = \frac{-1}{\sqrt{2}}$$
$$\overrightarrow{v_{2}} \cdot (3,0) = \left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot (3,0) = \frac{-3}{\sqrt{2}}$$

 $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 



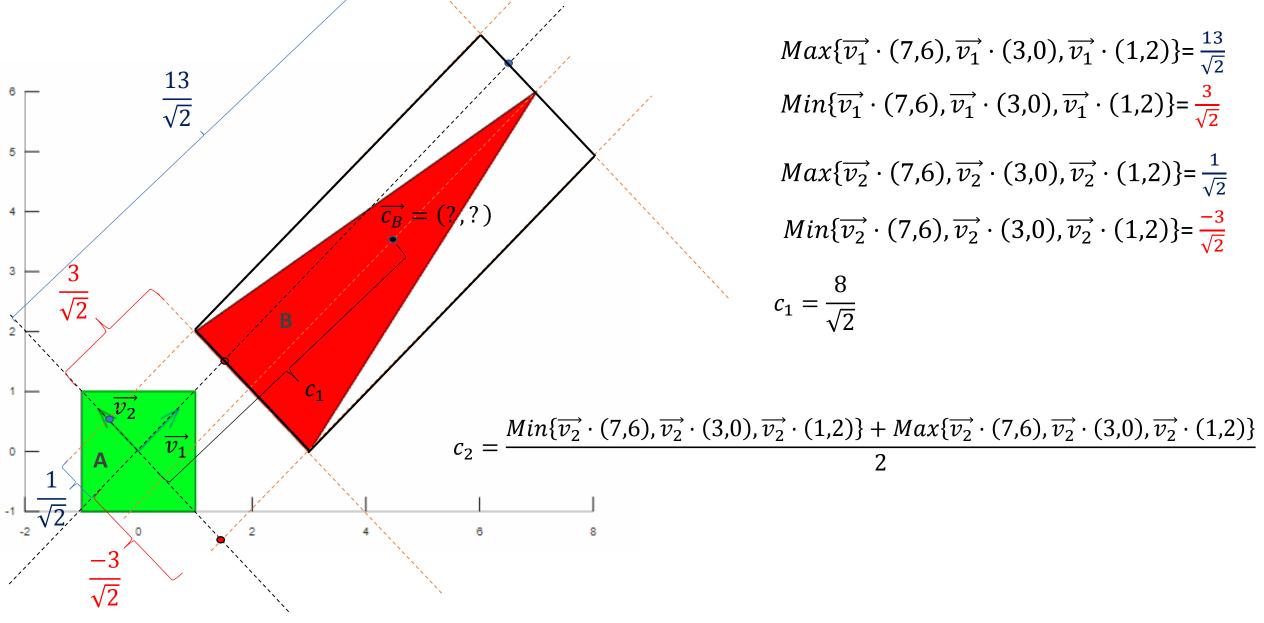
 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

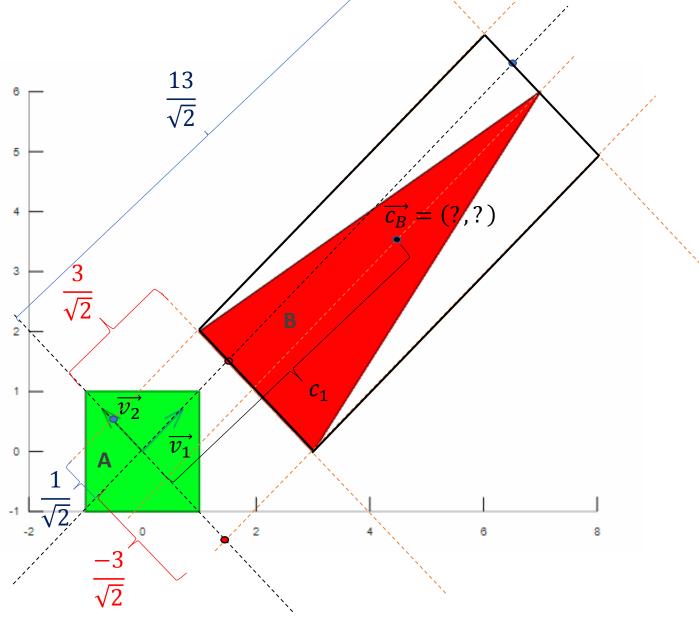




 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

$$c_1 = \frac{\frac{3}{\sqrt{2}} + \frac{13}{\sqrt{2}}}{2} = \frac{16}{2\sqrt{2}} = \frac{8}{\sqrt{2}}$$

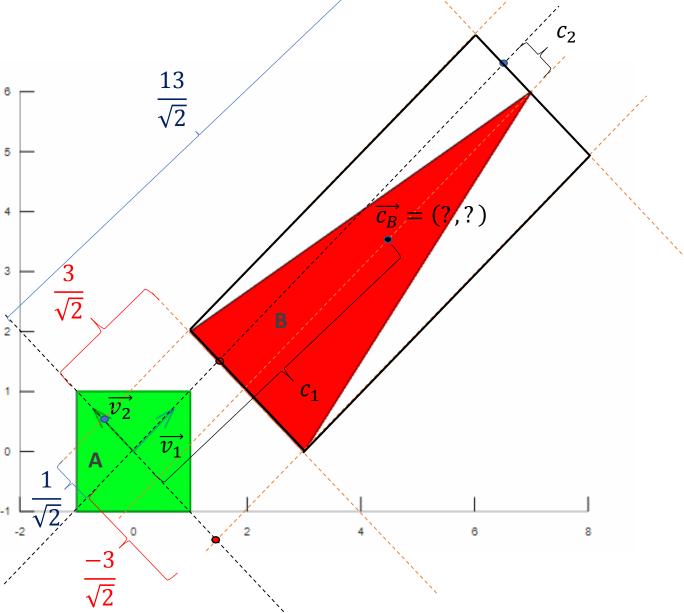




 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

$$c_{1} = \frac{8}{\sqrt{2}}$$

$$c_{2} = \frac{\frac{-3}{\sqrt{2}} + \frac{1}{\sqrt{2}}}{2} = \frac{1-3}{2\sqrt{2}} = \frac{-2}{2\sqrt{2}} = \frac{-1}{\sqrt{2}}$$

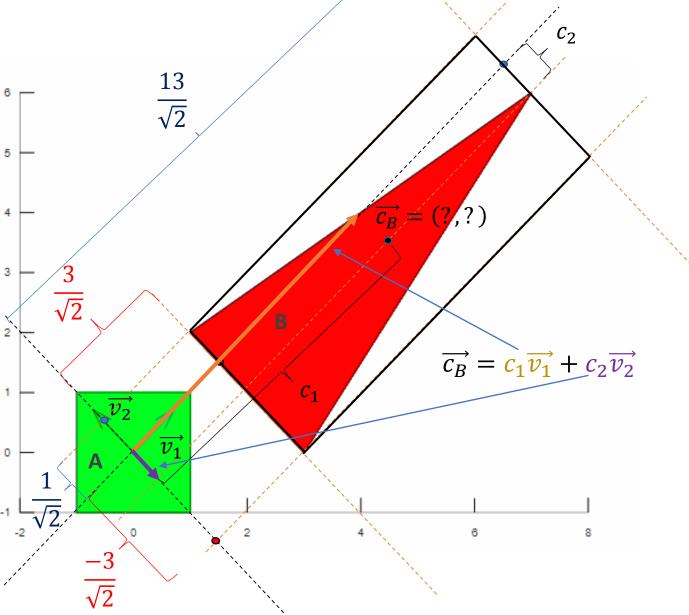


 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

 $c_1 = \frac{8}{\sqrt{2}}$ 

 $c_2 = \frac{-1}{\sqrt{2}}$ 

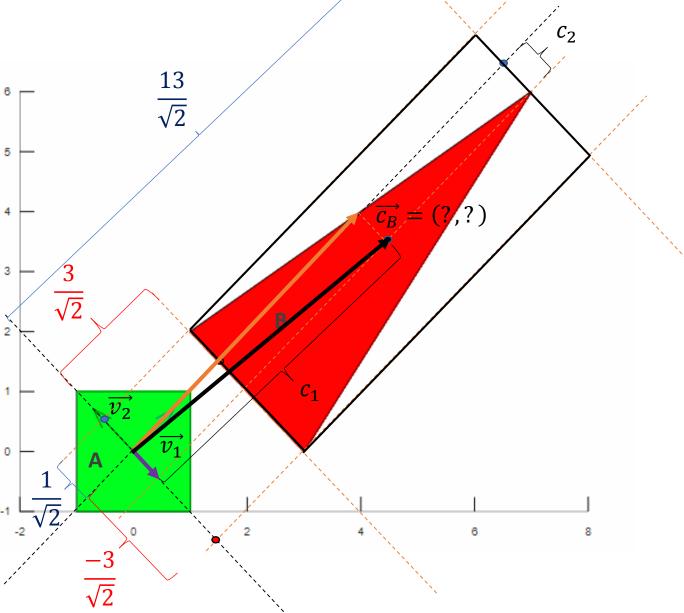
 $\overrightarrow{c_B} = ?$ 



 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

 $c_1 = \frac{8}{\sqrt{2}}$ 

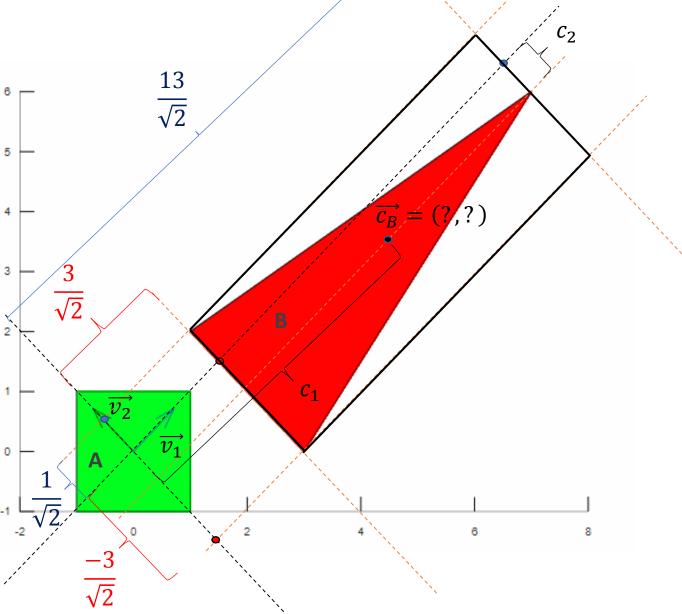
 $c_2 = \frac{-1}{\sqrt{2}}$ 



 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

$$c_1 = \frac{8}{\sqrt{2}}$$
$$c_2 = \frac{-1}{\sqrt{2}}$$

 $\overrightarrow{c_B} = c_1 \overrightarrow{v_1} + c_2 \overrightarrow{v_2}$ 

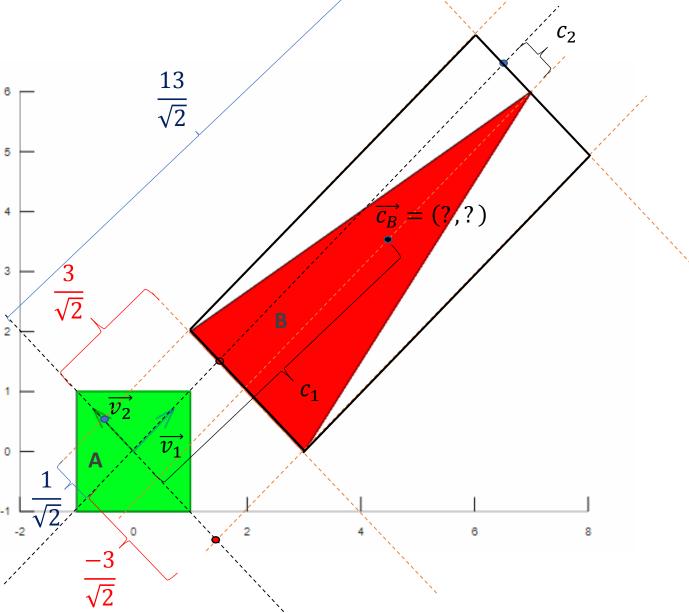


 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

 $\overrightarrow{c_B} = \frac{8}{\sqrt{2}} \left( \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right) + \frac{-1}{\sqrt{2}} \left( \frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right)$ 

 $c_1 = \frac{8}{\sqrt{2}}$ 

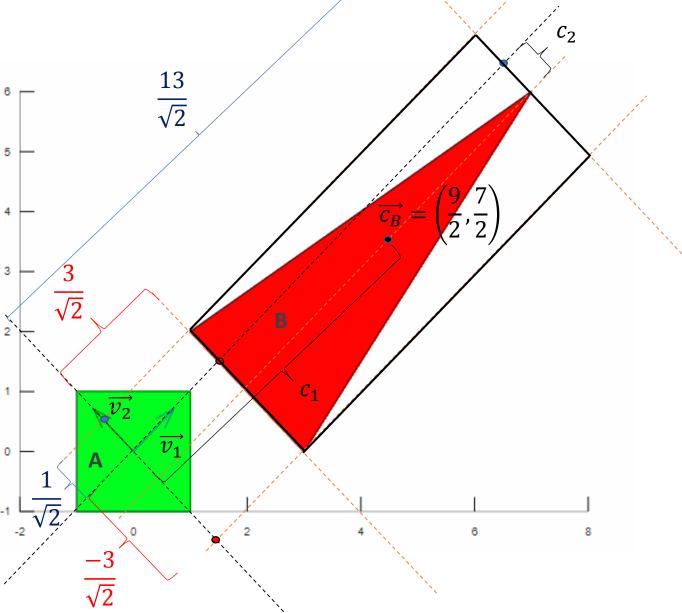
 $c_2 = \frac{-1}{\sqrt{2}}$ 



 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

$$c_1 = \frac{8}{\sqrt{2}}$$
$$c_2 = \frac{-1}{\sqrt{2}}$$

$$\overrightarrow{c_B} = \left(\frac{8}{2}, \frac{8}{2}\right) + \left(\frac{1}{2}, \frac{-1}{2}\right)$$

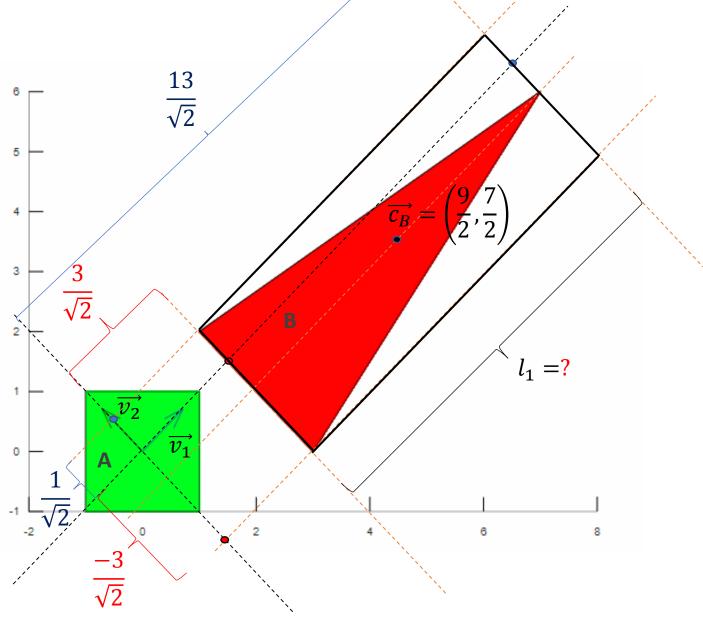


 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

 $c_1 = \frac{8}{\sqrt{2}}$ 

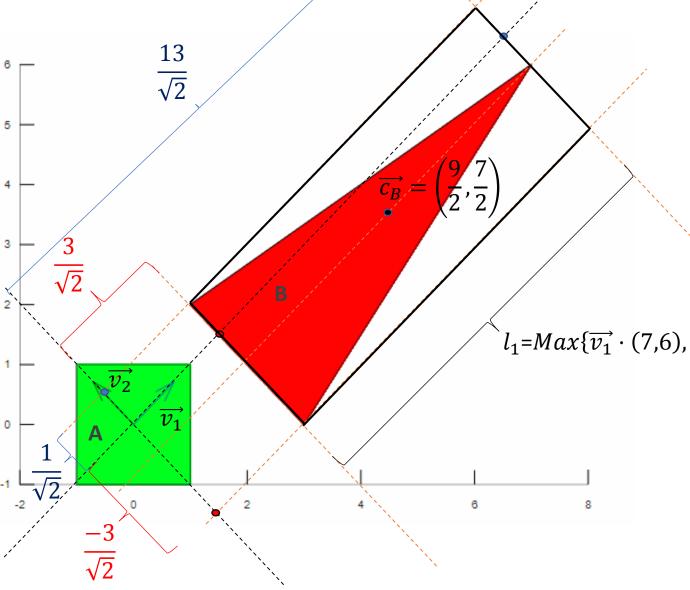
 $c_2 = \frac{-1}{\sqrt{2}}$ 

 $\overrightarrow{c_B} = \left(\frac{9}{2}, \frac{7}{2}\right)$ 



 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

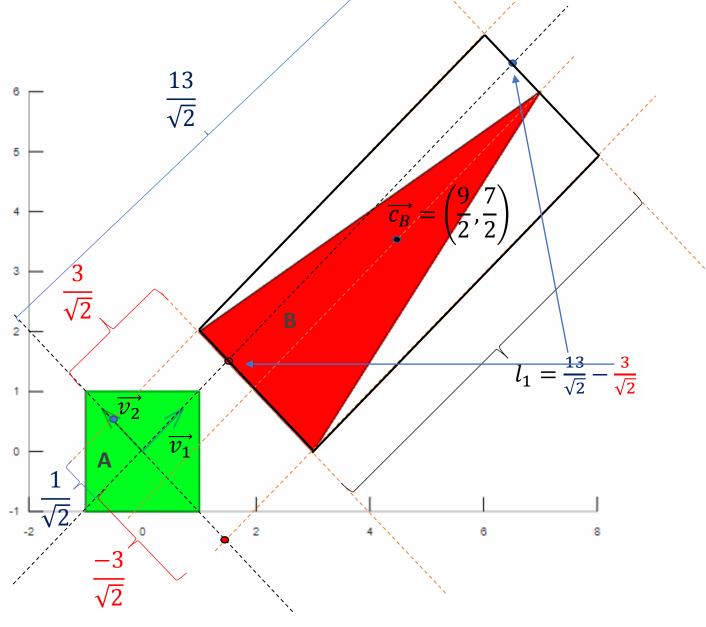
$$\overrightarrow{c_B} = \left(\frac{9}{2}, \frac{7}{2}\right)$$



 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

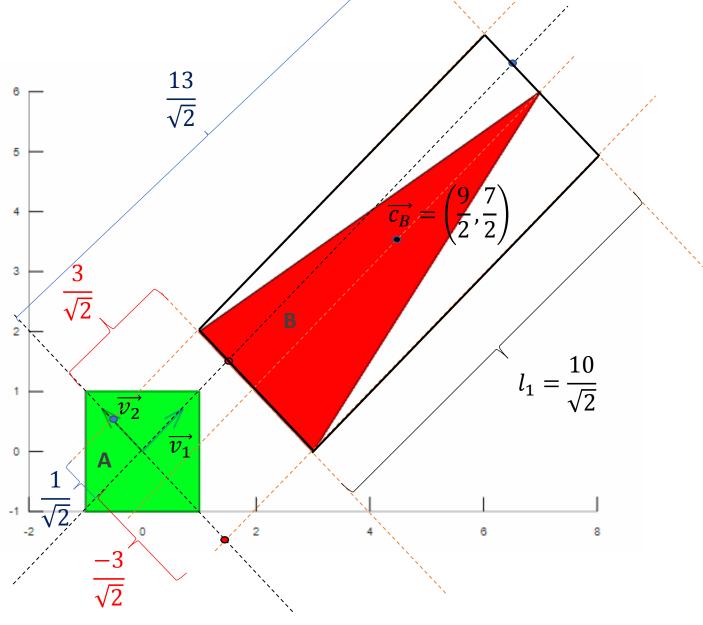
 $\overrightarrow{c_B} = \left(\frac{9}{2}, \frac{7}{2}\right)$ 

 $i_1 = Max\{\overrightarrow{v_1} \cdot (7,6), \overrightarrow{v_1} \cdot (3,0), \overrightarrow{v_1} \cdot (1,2)\} - Min\{\overrightarrow{v_1} \cdot (7,6), \overrightarrow{v_1} \cdot (3,0), \overrightarrow{v_1} \cdot (1,2)\}$ 



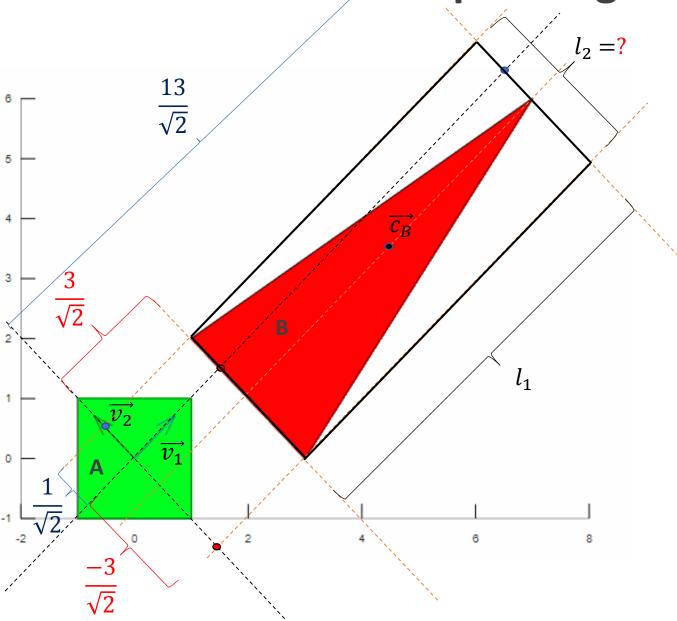
 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

$$\overrightarrow{c_B} = \left(\frac{9}{2}, \frac{7}{2}\right)$$



 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

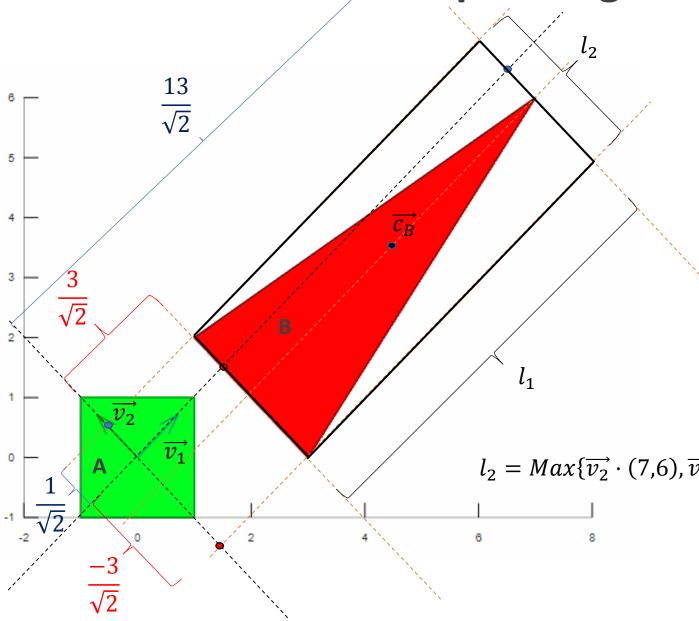
$$\overrightarrow{c_B} = \left(\frac{9}{2}, \frac{7}{2}\right)$$



 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

$$\overrightarrow{c_B} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

 $l_1 = \frac{10}{\sqrt{2}}$ 

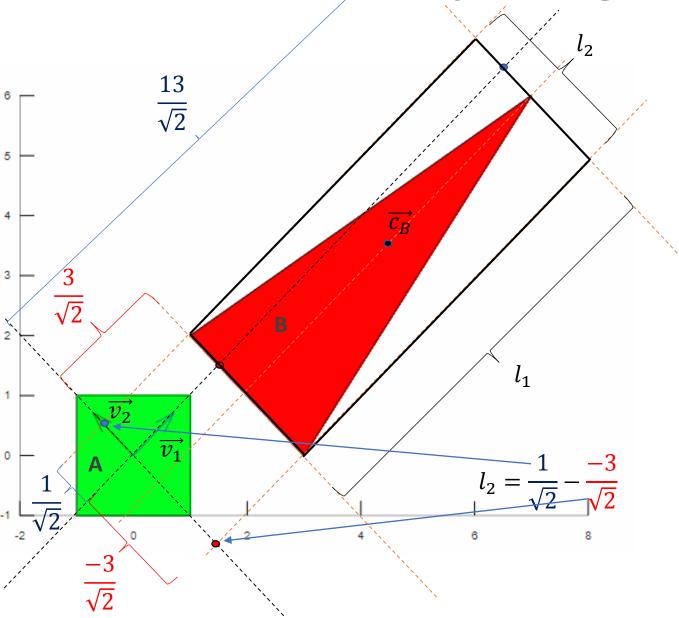


 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

$$\overrightarrow{c_B} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

 $l_1 = \frac{10}{\sqrt{2}}$ 

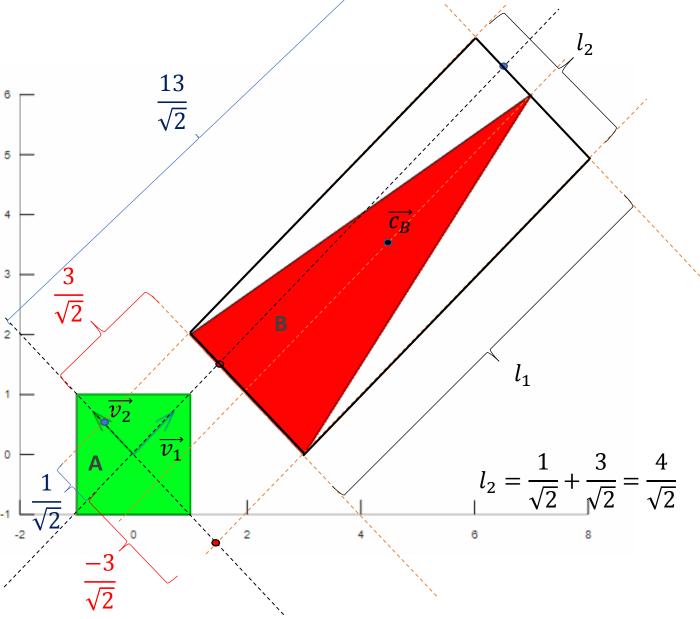
 $l_2 = Max\{\overrightarrow{v_2} \cdot (7,6), \overrightarrow{v_2} \cdot (3,0), \overrightarrow{v_2} \cdot (1,2)\} - Min\{\overrightarrow{v_2} \cdot (7,6), \overrightarrow{v_2} \cdot (3,0), \overrightarrow{v_2} \cdot (1,2)\}$ 



 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

$$\overrightarrow{c_B} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

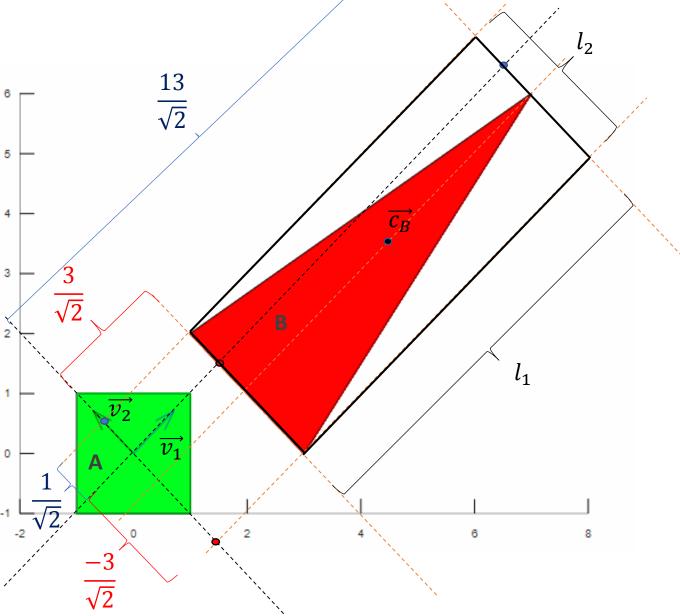
 $l_1 = \frac{10}{\sqrt{2}}$ 



 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

$$\overrightarrow{c_B} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

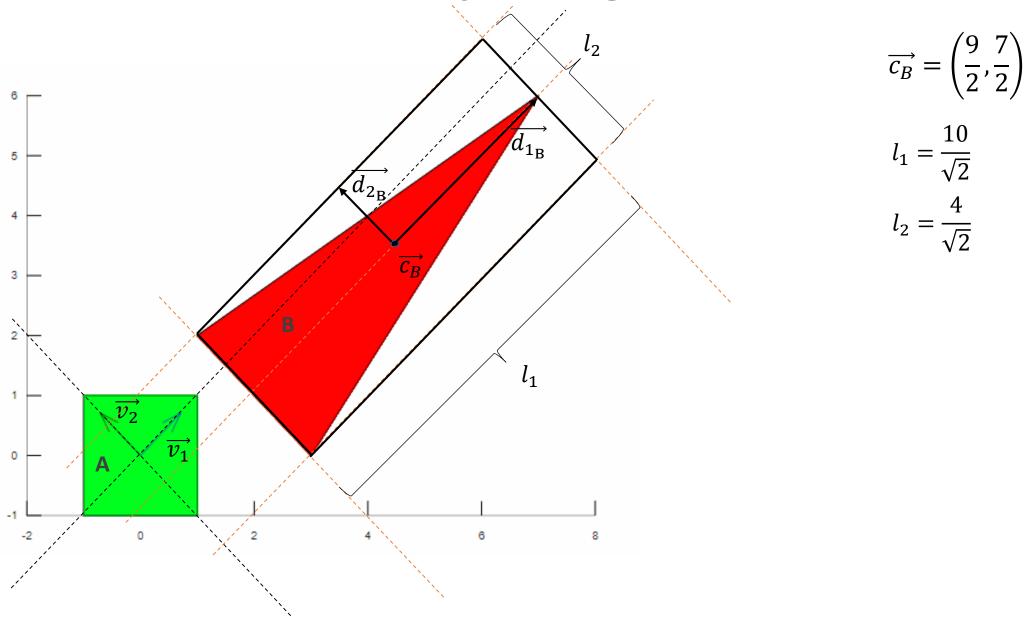
$$l_1 = \frac{10}{\sqrt{2}}$$

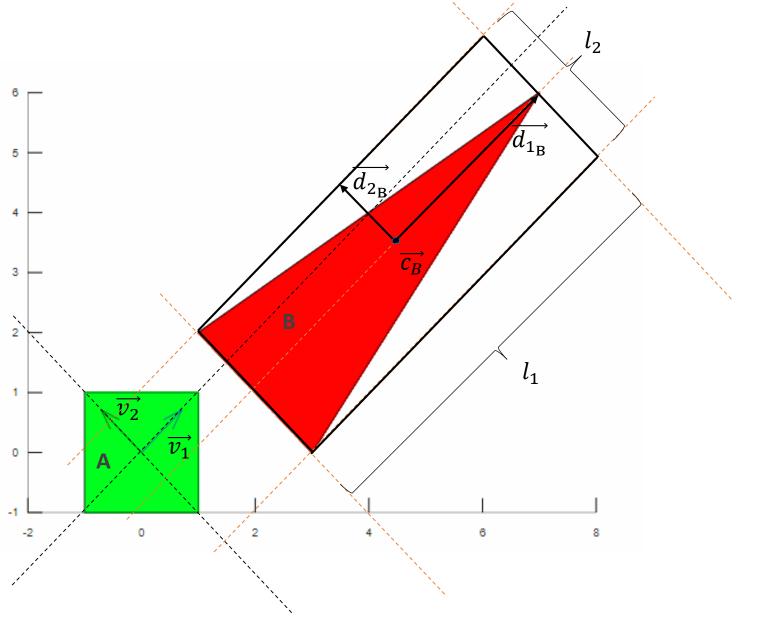


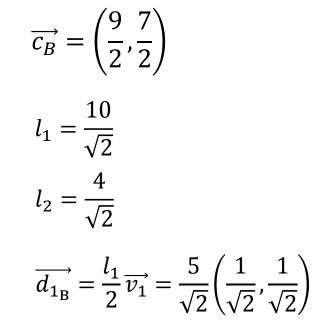
 $Max\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{13}{\sqrt{2}}$  $Min\{\overrightarrow{v_{1}} \cdot (7,6), \overrightarrow{v_{1}} \cdot (3,0), \overrightarrow{v_{1}} \cdot (1,2)\} = \frac{3}{\sqrt{2}}$  $Max\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{1}{\sqrt{2}}$  $Min\{\overrightarrow{v_{2}} \cdot (7,6), \overrightarrow{v_{2}} \cdot (3,0), \overrightarrow{v_{2}} \cdot (1,2)\} = \frac{-3}{\sqrt{2}}$ 

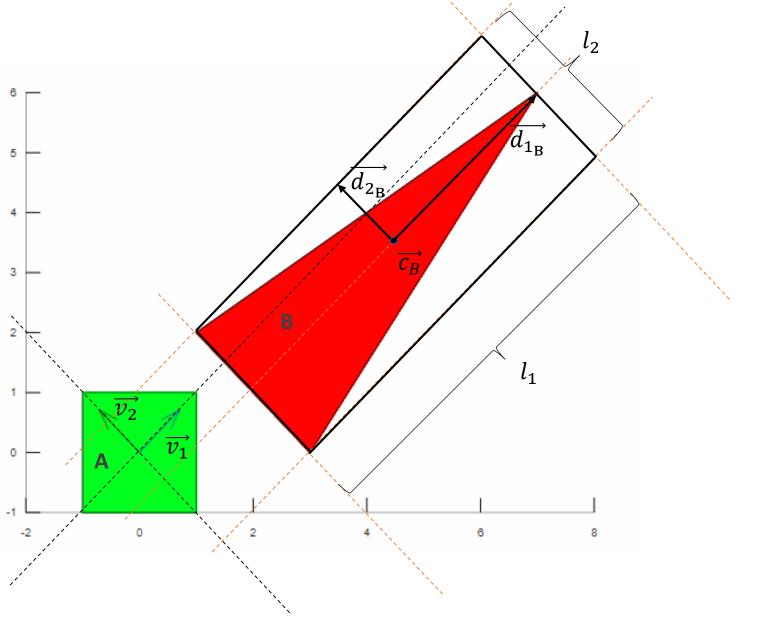
$$\overrightarrow{c_B} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

$$l_1 = \frac{10}{\sqrt{2}}$$
$$l_2 = \frac{4}{\sqrt{2}}$$

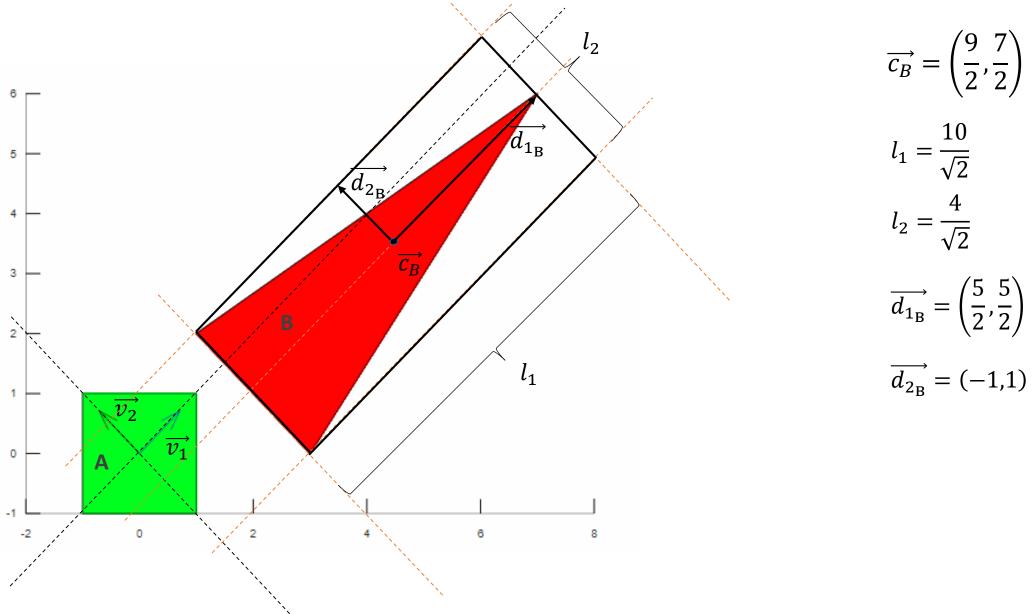


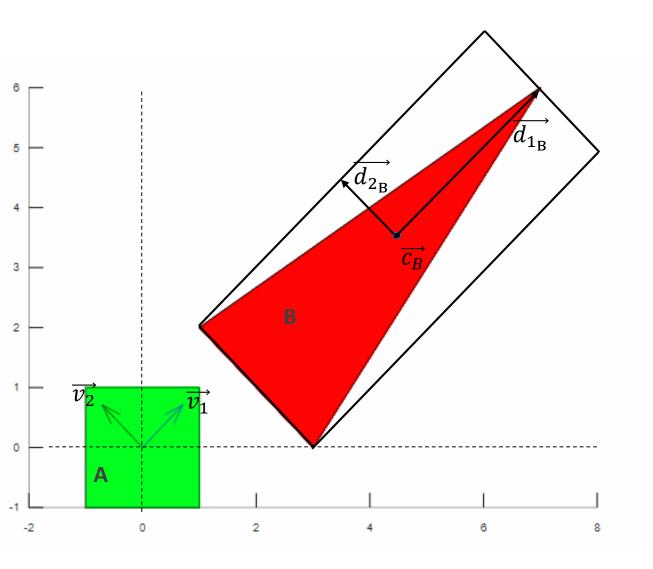






$\overrightarrow{c_B} = \left(\frac{9}{2}, \frac{7}{2}\right)$
$l_1 = \frac{10}{\sqrt{2}}$
$l_2 = \frac{4}{\sqrt{2}}$
$\overrightarrow{d_{1_{\mathrm{B}}}} = \frac{l_1}{2} \overrightarrow{v_1} = \frac{5}{\sqrt{2}} \left( \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right)$
$\overrightarrow{d_{2_{\mathrm{B}}}} = \frac{l_2}{2} \overrightarrow{v_2} = \frac{2}{\sqrt{2}} \left( \frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right)$





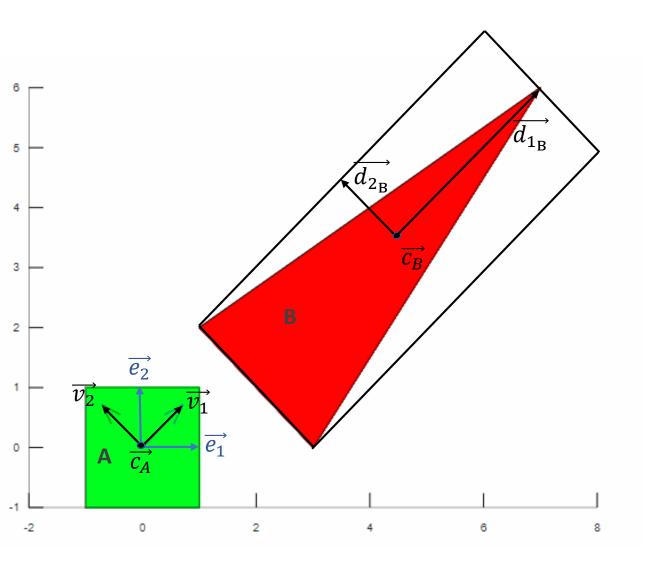
$$\overrightarrow{c_B} = \begin{pmatrix} 9 & 7 \\ \overline{2} & 7 \\ 2 \end{pmatrix}$$
$$\overrightarrow{d_{1_B}} = \begin{pmatrix} 5 & 5 \\ \overline{2} & 7 \\ 2 \end{pmatrix}$$

$$\overrightarrow{d_{2_{\rm B}}} = (-1,1)$$

 $\overrightarrow{c_A} = ?$ 

 $\overrightarrow{d_{1_{A}}} = ?$ 

 $\overrightarrow{d_{2_A}} = ?$ 

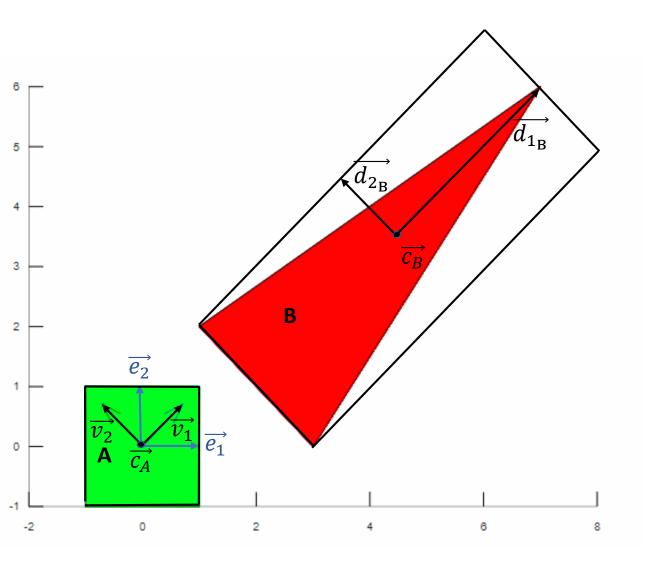


$$\overrightarrow{c_B} = \begin{pmatrix} 9 & 7 \\ \overline{2} & \overline{2} \end{pmatrix}$$
$$\overrightarrow{d_{1_B}} = \begin{pmatrix} 5 & 5 \\ \overline{2} & \overline{2} \end{pmatrix}$$
$$\overrightarrow{d_{2_B}} = (-1,1)$$

 $\overrightarrow{c_A} = ?$ 

 $\overrightarrow{d_{1_A}} = ?$ 

 $\overrightarrow{d_{2_A}} = ?$ 

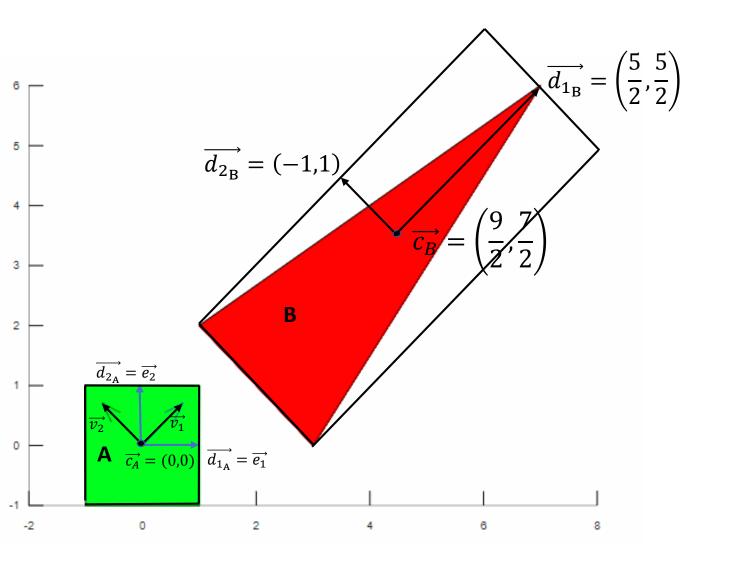


$$\overrightarrow{c_B} = \begin{pmatrix} 9 & 7 \\ \overline{2} & \overline{2} \end{pmatrix}$$
$$\overrightarrow{d_{1_B}} = \begin{pmatrix} 5 & 5 \\ \overline{2} & \overline{2} \end{pmatrix}$$
$$\overrightarrow{d_{2_B}} = (-1,1)$$

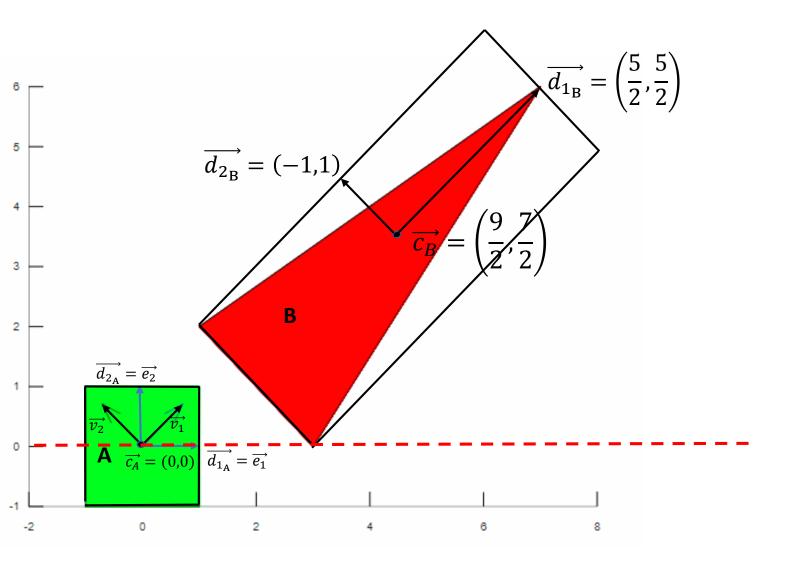
$$\overrightarrow{c_A} = (0,0)$$

$$\overrightarrow{d_{1_{\mathrm{A}}}} = \overrightarrow{e_1}$$

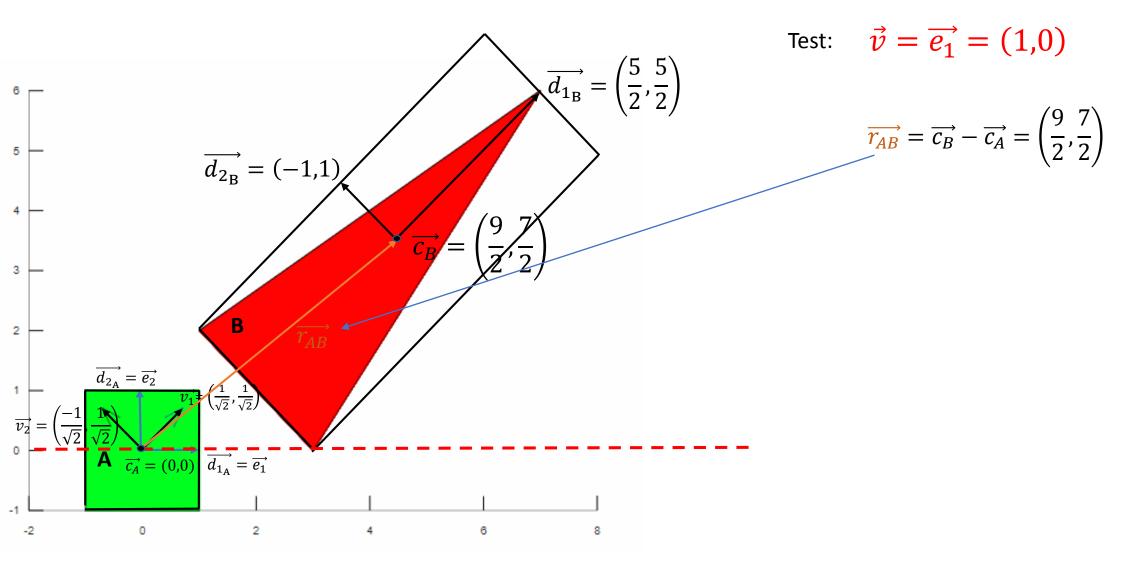
 $\overrightarrow{d_{2_{\rm A}}} = \overrightarrow{e_2}$ 

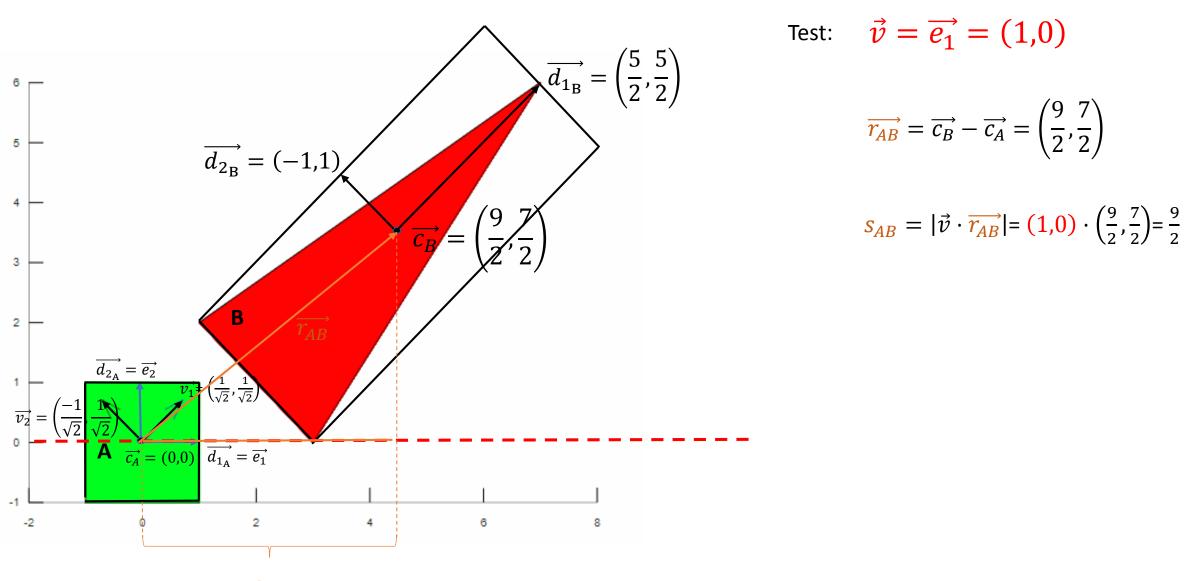


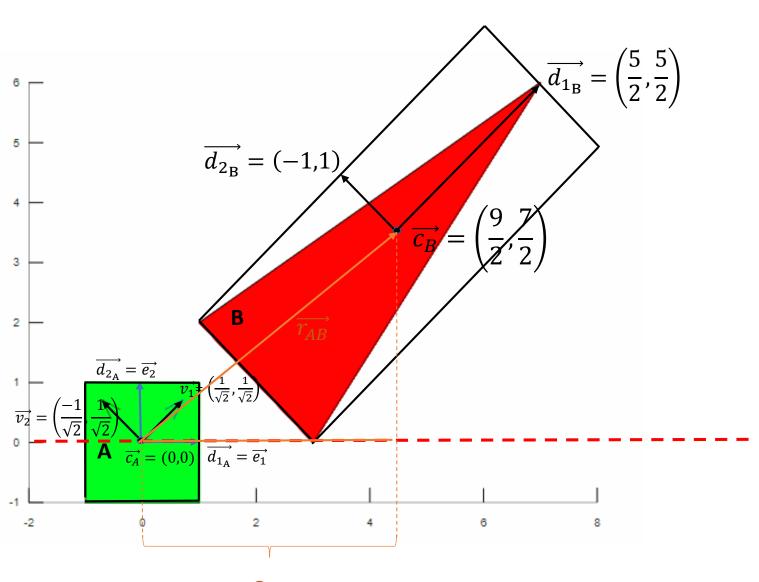
Test:



Test: 
$$\vec{v} = \vec{e_1} = (1,0)$$





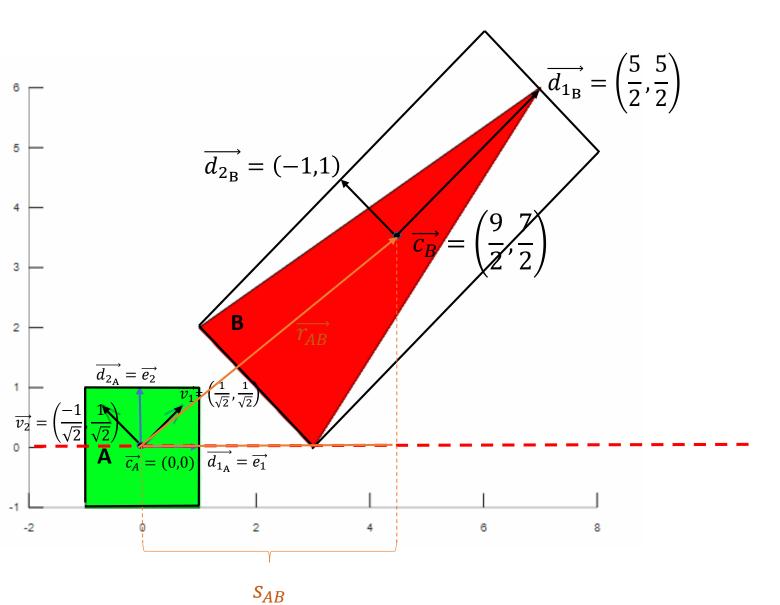


Test: 
$$\vec{v} = \vec{e_1} = (1,0)$$

$$\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

$$s_{AB} = |\vec{v} \cdot \overrightarrow{r_{AB}}| = (1,0) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) = \frac{9}{2}$$

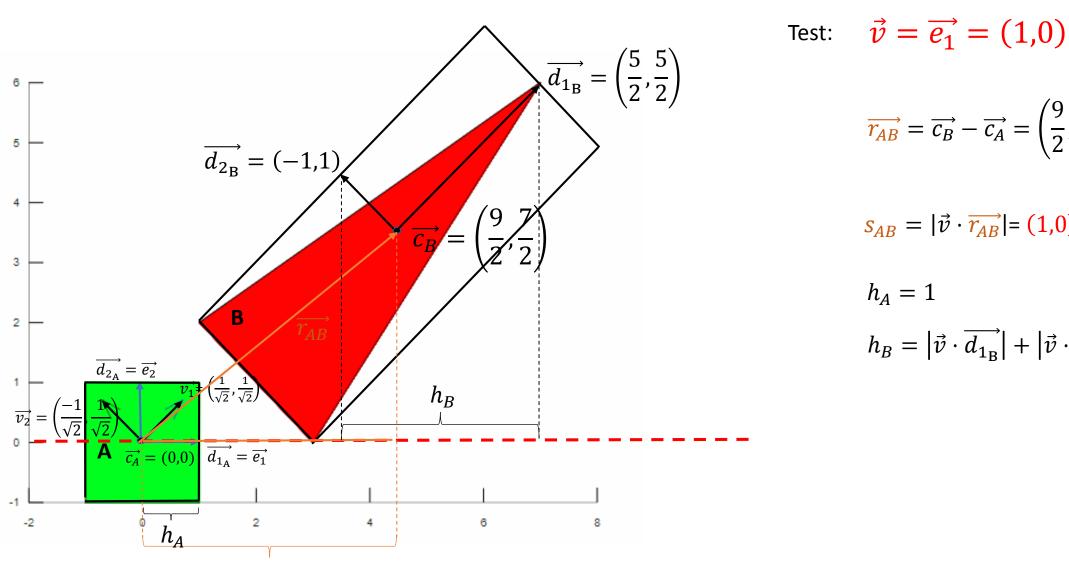
$$h_A = \left| \vec{v} \cdot \overrightarrow{d_{1_A}} \right| + \left| \vec{v} \cdot \overrightarrow{d_{2_A}} \right|$$



Test: 
$$\vec{v} = \vec{e_1} = (1,0)$$
  
 $\vec{r_{AB}} = \vec{c_B} - \vec{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$ 

$$s_{AB} = |\vec{v} \cdot \overrightarrow{r_{AB}}| = (1,0) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) = \frac{9}{2}$$

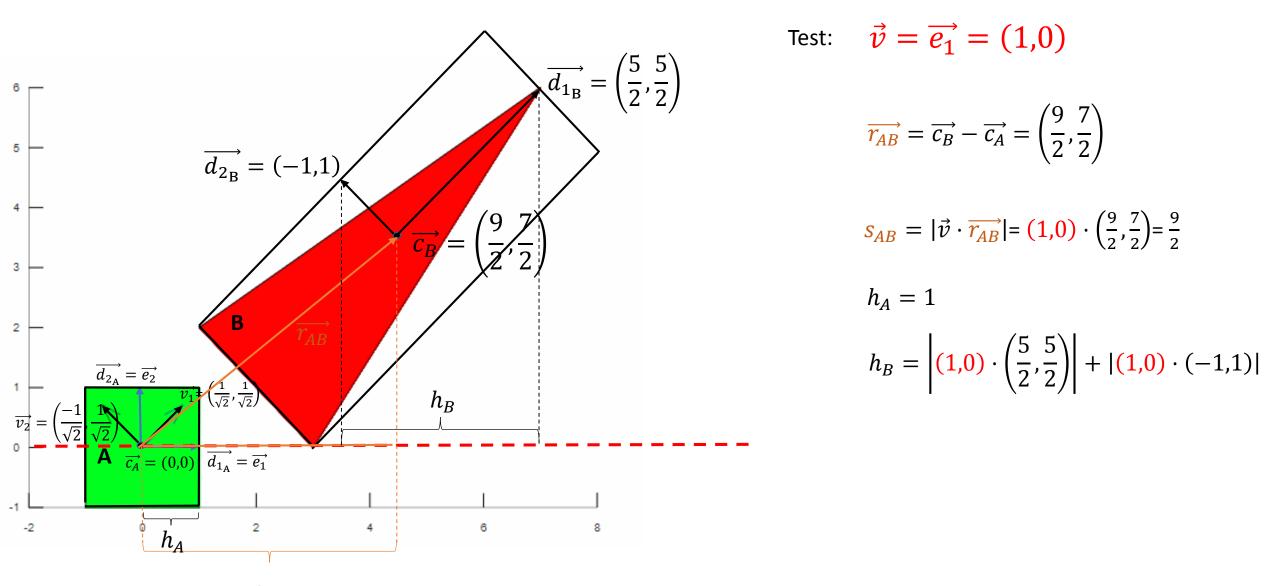
 $h_A = |(1,0) \cdot (1,0)| + |(1,0) \cdot (0,1)|$ 

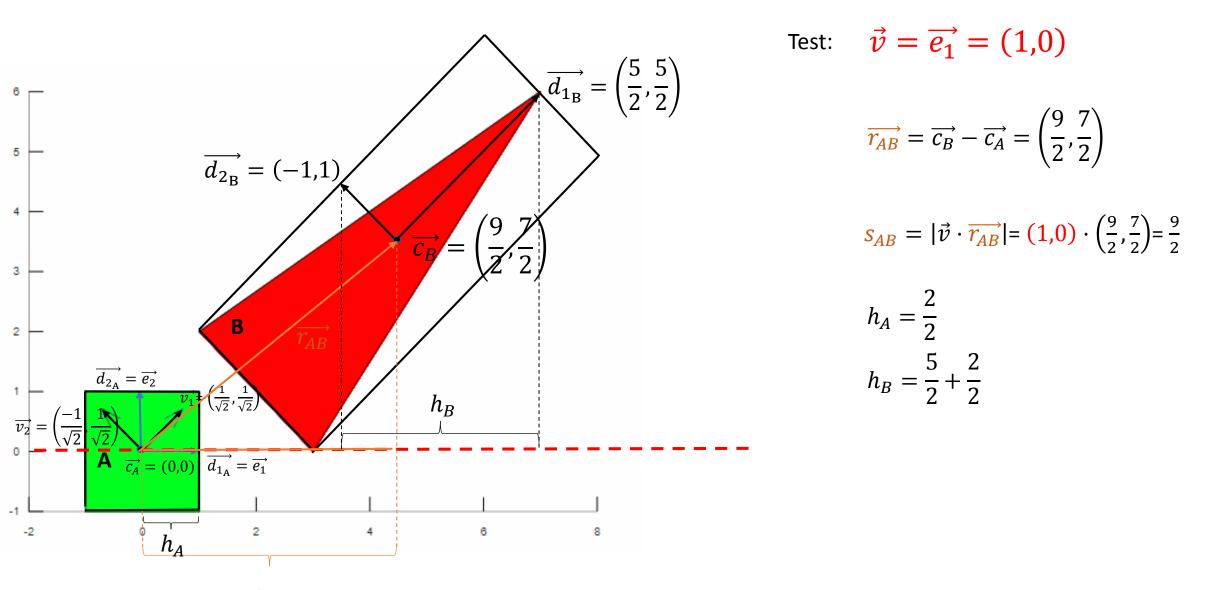


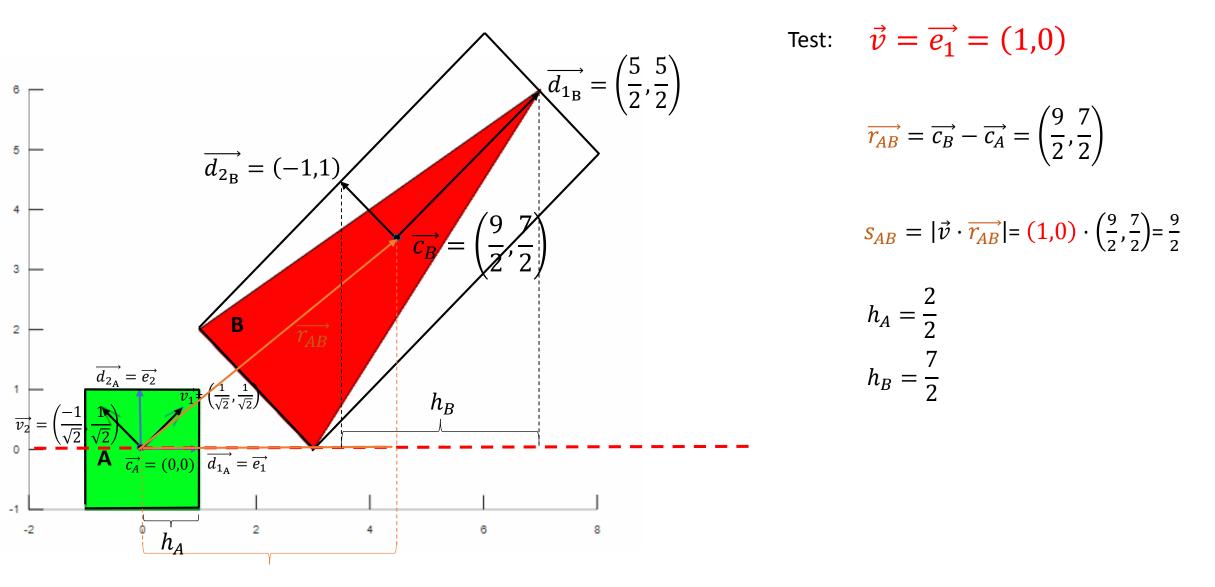
$$\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

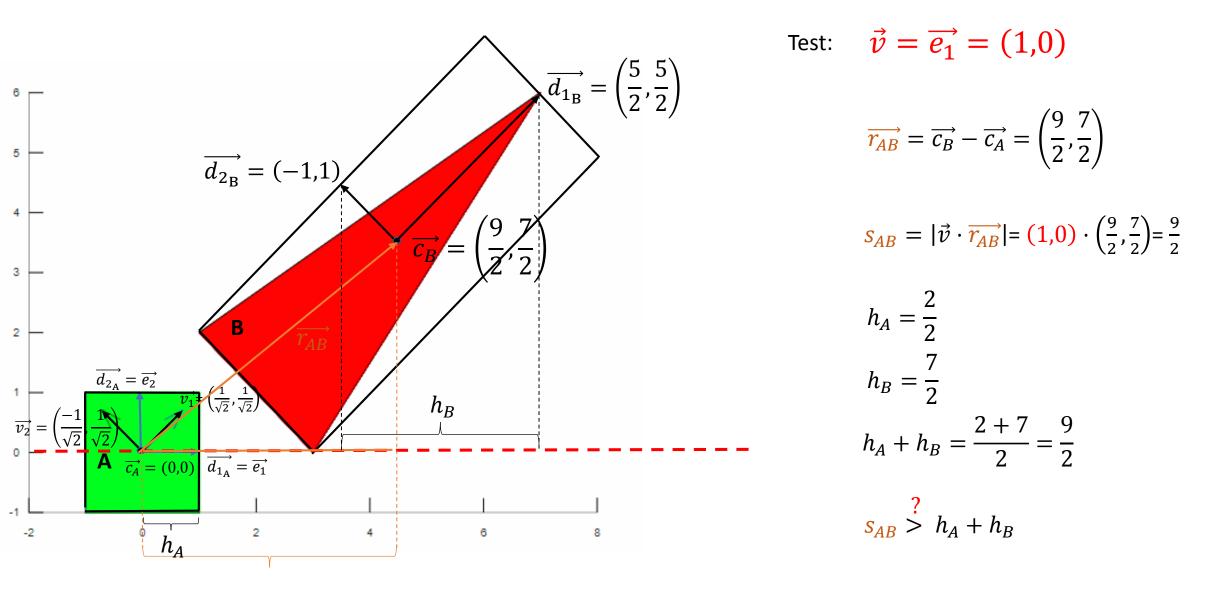
$$s_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = (1,0) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) = \frac{9}{2}$$

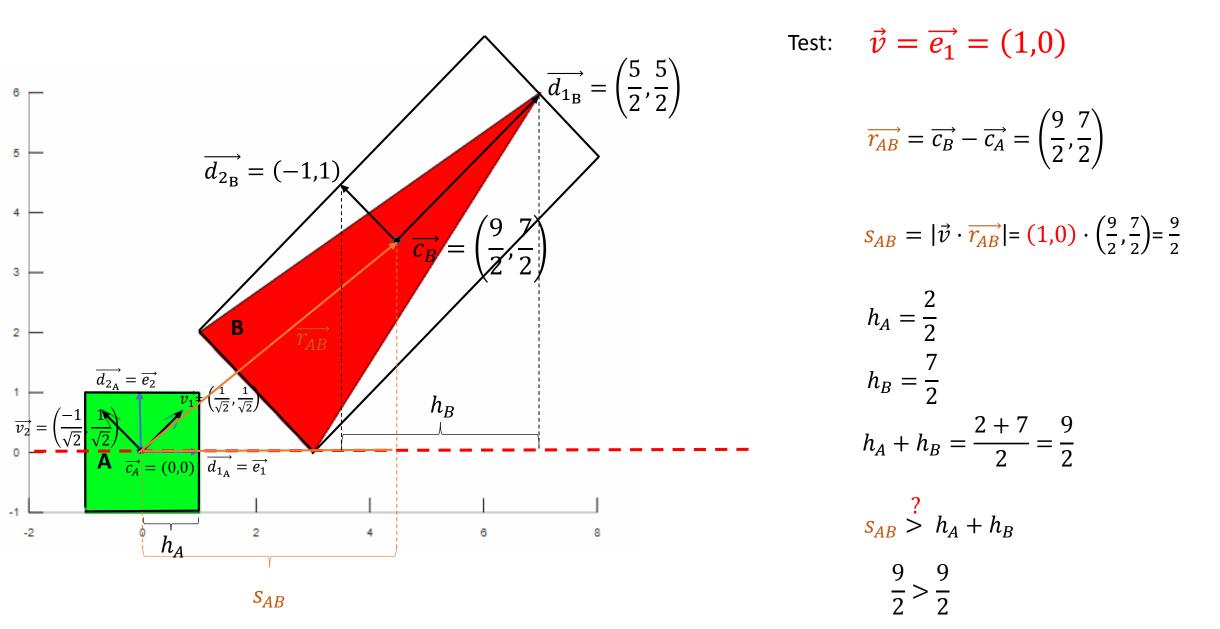
$$h_A = 1$$
$$h_B = \left| \vec{v} \cdot \overrightarrow{d_{1_B}} \right| + \left| \vec{v} \cdot \overrightarrow{d_{2_B}} \right|$$

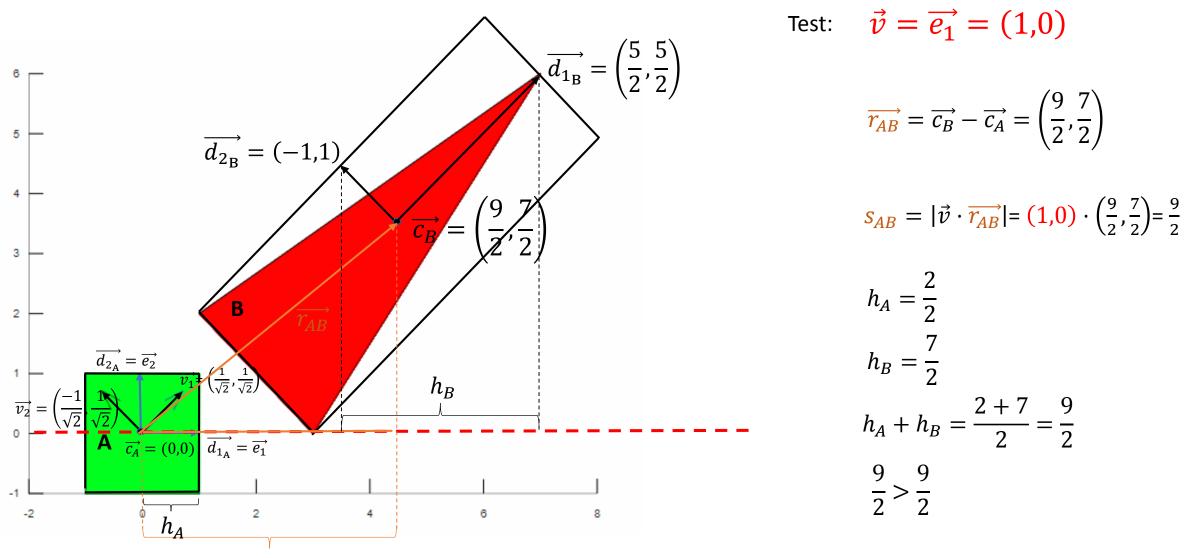






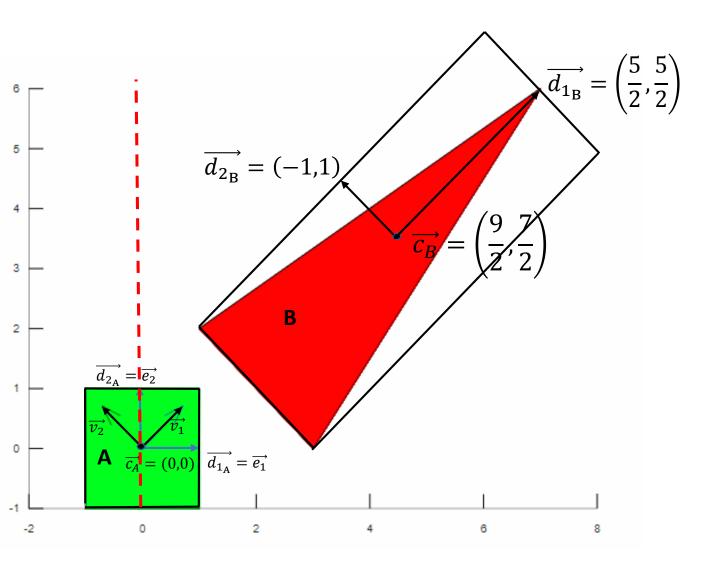




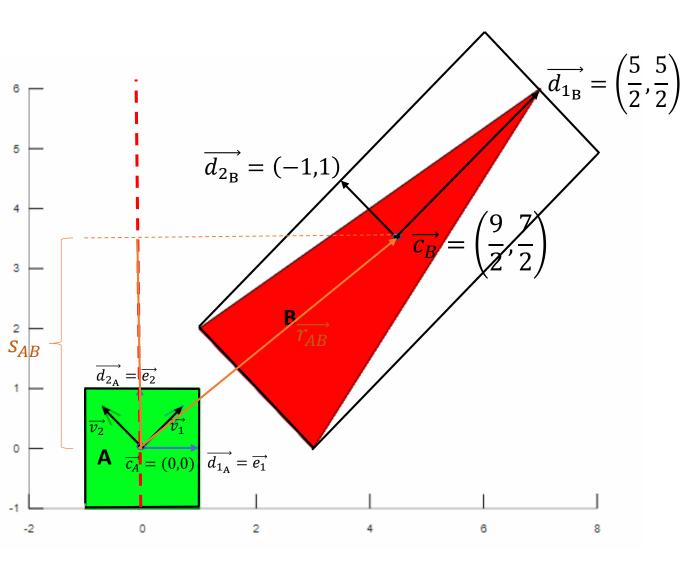


not true  $\Rightarrow$  can't say that they are not in a collision

 $S_{AB}$ 



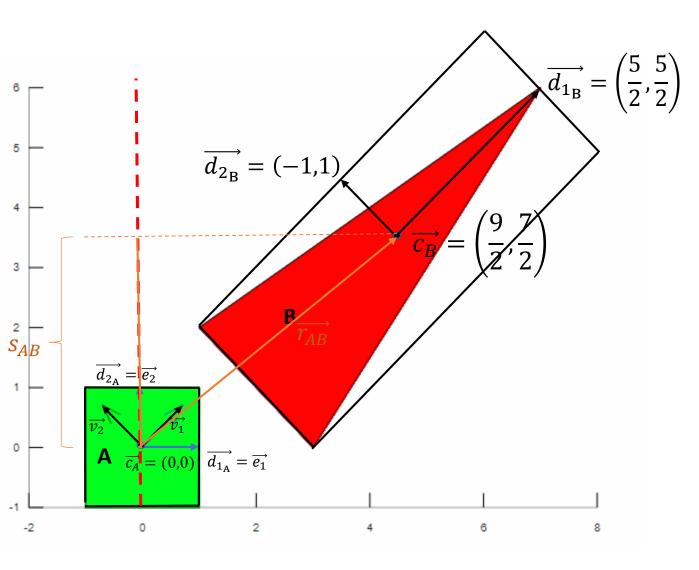
Test: 
$$\vec{v} = \vec{e_2} = (0,1)$$



Test: 
$$\vec{v} = \vec{e_2} = (0,1)$$

$$\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

$$S_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = (0,1) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) = \frac{7}{2}$$

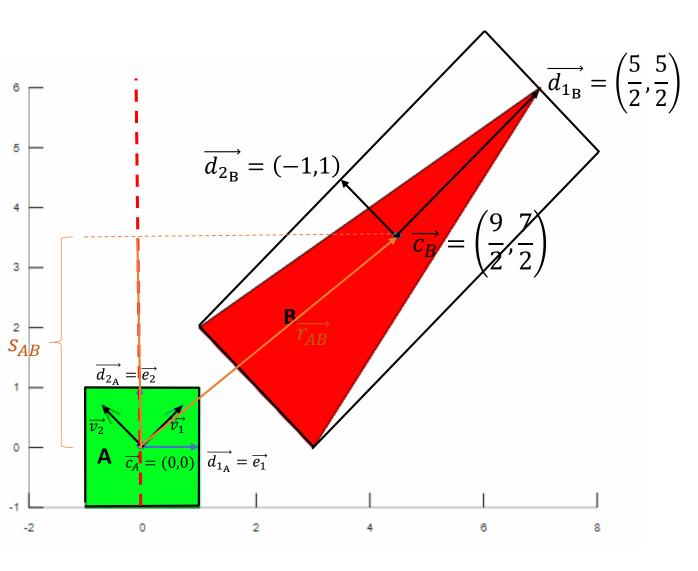


Test: 
$$\vec{v} = \vec{e_2} = (0,1)$$

$$\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

$$s_{AB} = |\vec{v} \cdot \overrightarrow{r_{AB}}| = (0,1) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) = \frac{7}{2}$$

$$h_B = \left| \vec{v} \cdot \overrightarrow{d_{1_B}} \right| + \left| \vec{v} \cdot \overrightarrow{d_{2_B}} \right|$$

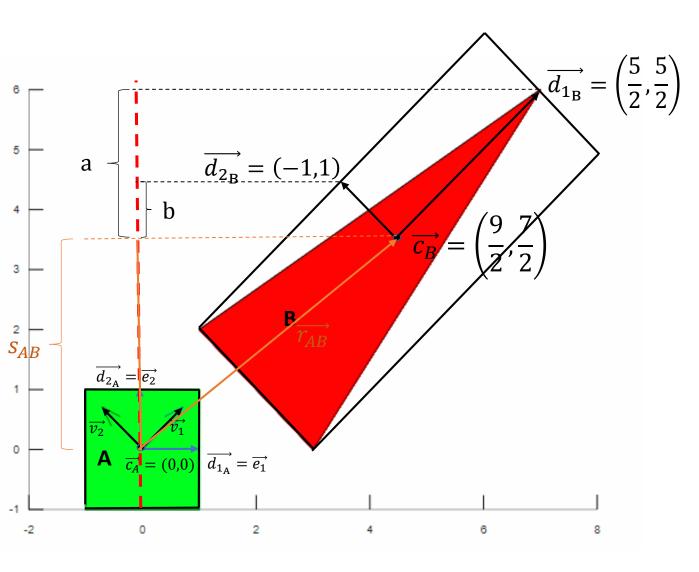


Test: 
$$\vec{v} = \vec{e_2} = (0,1)$$

$$\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

 $s_{AB} = |\vec{v} \cdot \overrightarrow{r_{AB}}| = (0,1) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) = \frac{7}{2}$ 

$$h_{B} = \left| \vec{v} \cdot \overrightarrow{d_{1_{B}}} \right| + \left| \vec{v} \cdot \overrightarrow{d_{2_{B}}} \right|$$
$$h_{B} = \left| (0,1) \cdot \overrightarrow{d_{1_{B}}} \right| + \left| (0,1) \cdot \overrightarrow{d_{2_{B}}} \right|$$



Test: 
$$\vec{v} = \vec{e_2} = (0,1)$$

$$\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

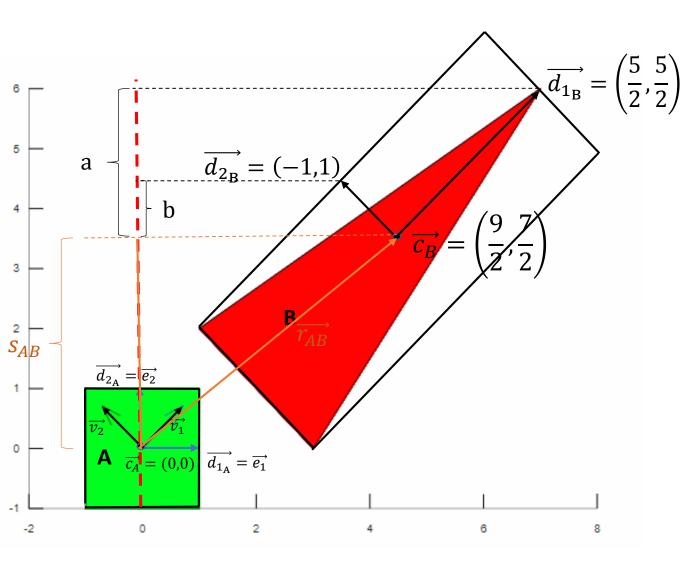
$$s_{AB} = |\vec{v} \cdot \overrightarrow{r_{AB}}| = (0,1) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) = \frac{7}{2}$$

$$h_{B} = \left| \vec{v} \cdot \overrightarrow{d_{1_{B}}} \right| + \left| \vec{v} \cdot \overrightarrow{d_{2_{B}}} \right|$$

$$h_{B} = \left| (0,1) \cdot \overrightarrow{d_{1_{B}}} \right| + \left| (0,1) \cdot \overrightarrow{d_{2_{B}}} \right|$$

$$h_{B} = \left| (0,1) \cdot \left( \frac{5}{2}, \frac{5}{2} \right) \right| + \left| (0,1) \cdot (-1,1) \right|$$

$$a \qquad b$$



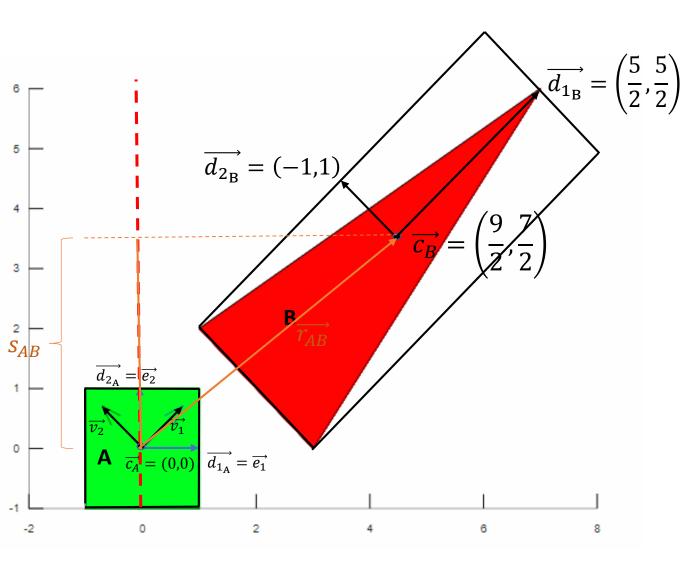
Test: 
$$\vec{v} = \vec{e_2} = (0,1)$$

$$\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

$$s_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = (0,1) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) = \frac{7}{2}$$

$$a_B = \left| (0,1) \cdot \left( \frac{5}{2}, \frac{5}{2} \right) \right| + \left| (0,1) \cdot (-1,1) \right|$$
  
a b

 $h_B = \frac{5}{2} + \frac{2}{2} = \frac{7}{2}$ 

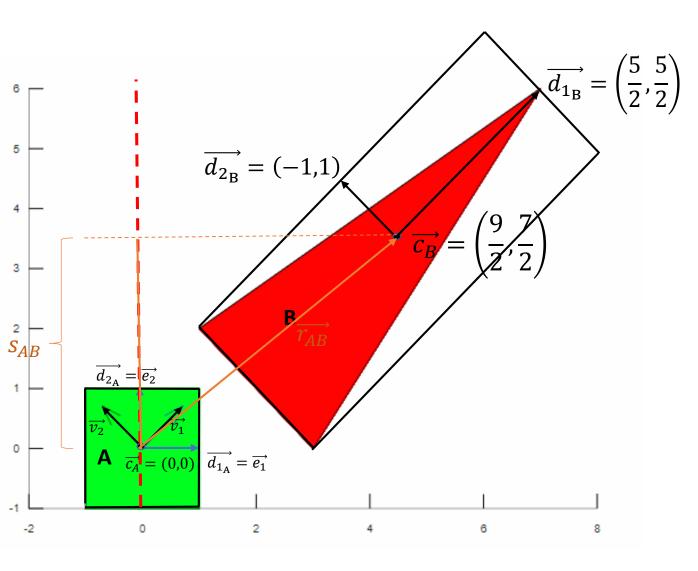


Test: 
$$\vec{v} = \vec{e_2} = (0,1)$$

$$\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

$$s_{AB} = |\vec{v} \cdot \overrightarrow{r_{AB}}| = (0,1) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) = \frac{7}{2}$$

$$h_B = \frac{7}{2}$$

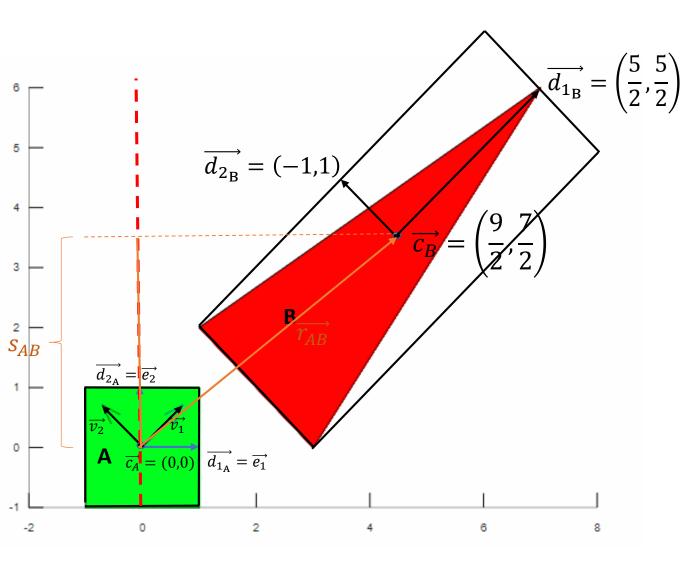


Test: 
$$\vec{v} = \vec{e_2} = (0,1)$$

$$\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

$$s_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = (0,1) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) = \frac{7}{2}$$

$$h_B = \frac{7}{2}$$
$$h_A = \left| \vec{v} \cdot \overrightarrow{d_{1_A}} \right| + \left| \vec{v} \cdot \overrightarrow{d_{2_A}} \right|$$



Test: 
$$\vec{v} = \vec{e_2} = (0,1)$$

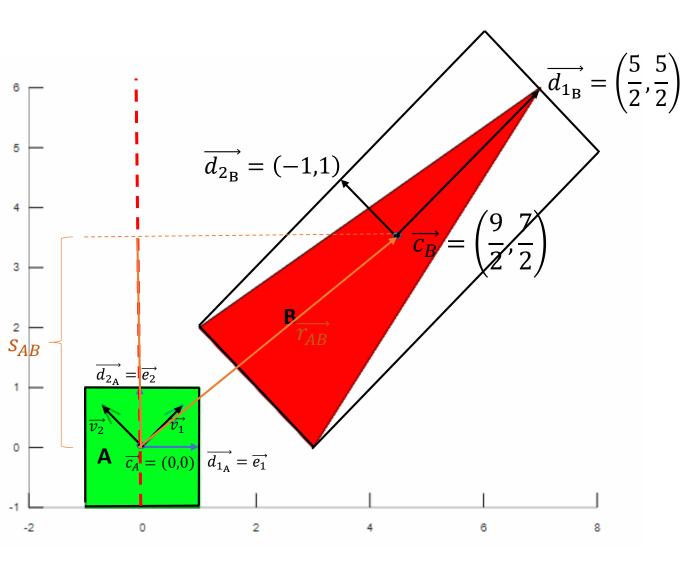
$$\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

$$s_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = (0,1) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) = \frac{7}{2}$$

$$h_{B} = \frac{7}{2}$$

$$h_{A} = |\vec{v} \cdot \overrightarrow{d_{1_{A}}}| + |\vec{v} \cdot \overrightarrow{d_{2_{A}}}|$$

$$h_{A} = |(0,1) \cdot (1,0)| + |(0,1) \cdot (0,1)|$$



Test: 
$$\vec{v} = \vec{e_2} = (0,1)$$

$$\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

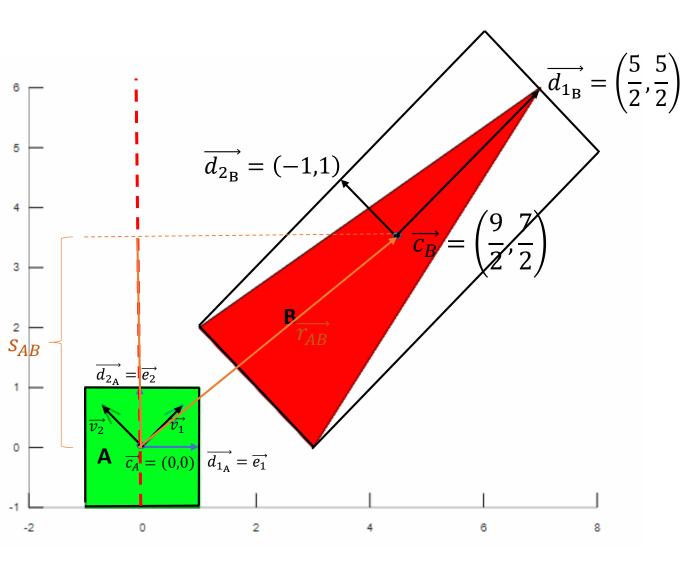
$$s_{AB} = |\vec{v} \cdot \overrightarrow{r_{AB}}| = (0,1) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) = \frac{7}{2}$$

$$h_B = \frac{7}{2}$$

$$h_A = \left| \vec{v} \cdot \overrightarrow{d_{1_A}} \right| + \left| \vec{v} \cdot \overrightarrow{d_{2_A}} \right|$$

$$h_A = \left| (0,1) \cdot (1,0) \right| + \left| (0,1) \cdot (0,1) \right|$$

$$h_A = \frac{2}{2}$$



Test: 
$$\vec{v} = \vec{e_2} = (0,1)$$

$$\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

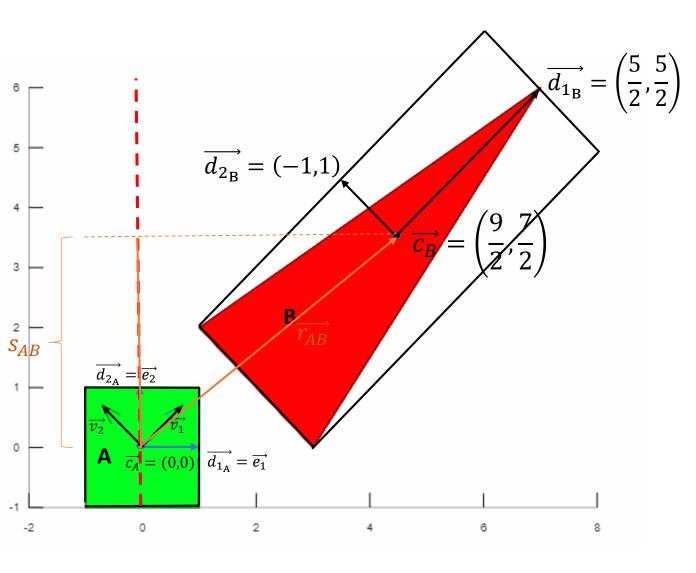
$$s_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = (0,1) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) = \frac{7}{2}$$

$$h_B = \frac{7}{2}$$

$$h_A = \frac{2}{2}$$

$$h_A + h_B = \frac{2+7}{2} = \frac{9}{2}$$

$$s_{AB} \stackrel{?}{>} h_A + h_B$$



Test: 
$$\vec{v} = \vec{e_2} = (0,1)$$

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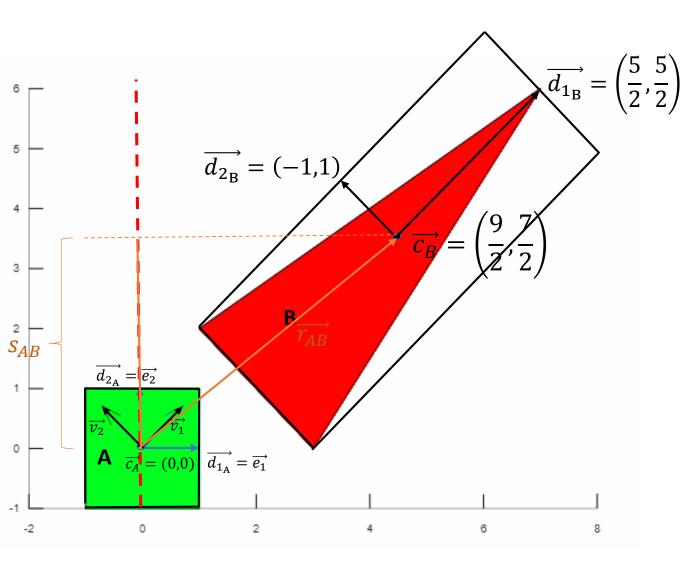
$$h_B = \frac{7}{2}$$

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$$s_{AB} \stackrel{?}{>} h_A + h_B$$

$$\frac{7}{2} > \frac{9}{2}$$



est: 
$$\vec{v} = \vec{e_2} = (0,1)$$

Т

$$\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$$

$$s_{AB} = |\vec{v} \cdot \overrightarrow{r_{AB}}| = (0,1) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) = \frac{7}{2}$$

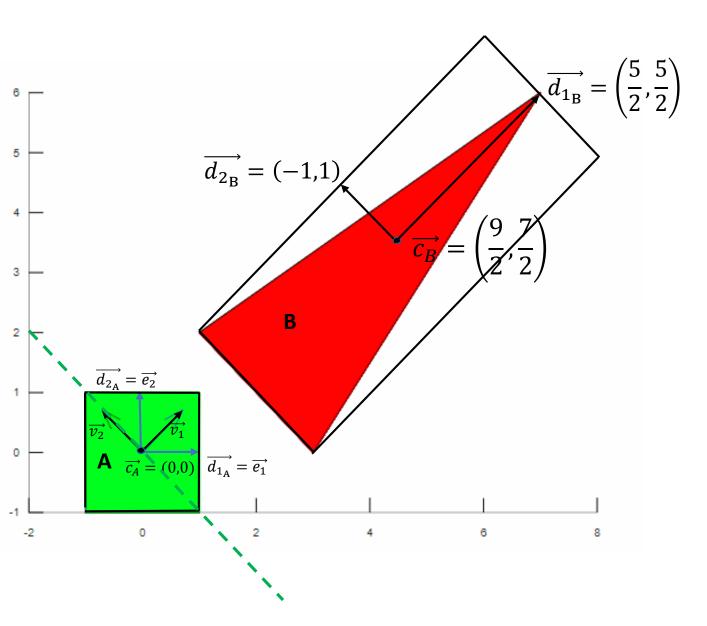
$$h_{B} = \frac{7}{2}$$

$$h_{A} = \frac{2}{2}$$

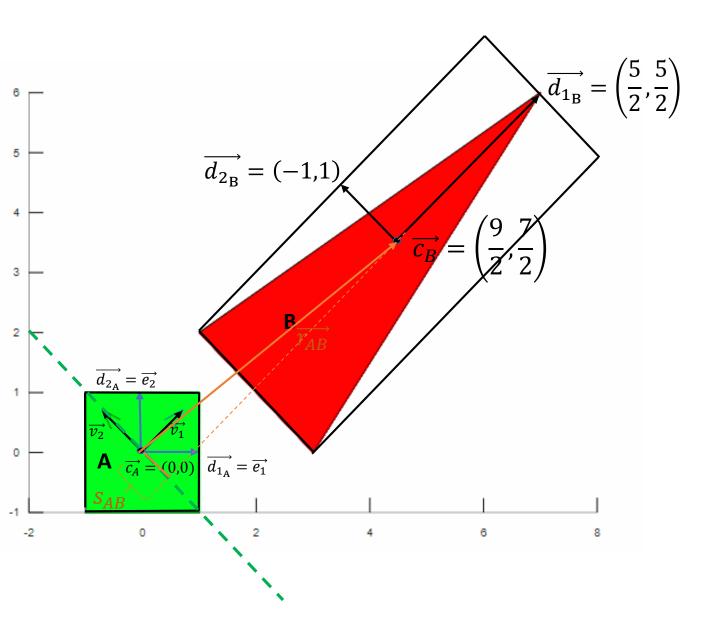
$$h_{A} + h_{B} = \frac{2+7}{2} = \frac{9}{2}$$

$$\frac{7}{2} > \frac{9}{2}$$

not true  $\Rightarrow$  can't say that they are not in a collision

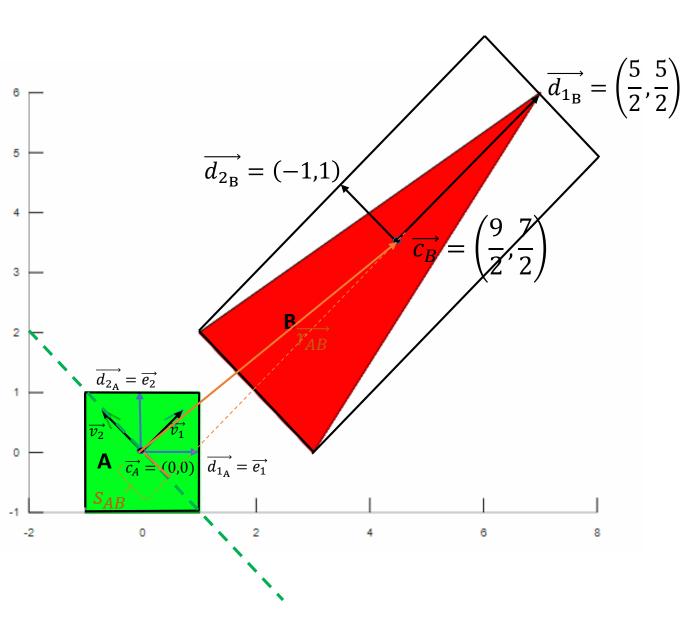


Test: 
$$\vec{v} = \vec{v_2} = \left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$



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 $\vec{r_{AB}} = \vec{c_B} - \vec{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$ 

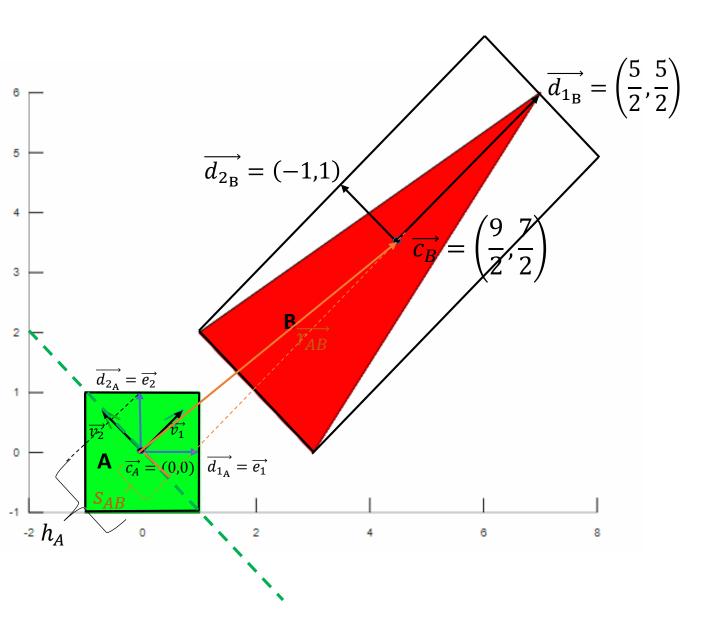
$$\begin{aligned} \mathbf{S}_{AB} &= |\vec{v} \cdot \overrightarrow{\mathbf{r}_{AB}}| = \left| \left( \frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right) \cdot \left( \frac{9}{2}, \frac{7}{2} \right) \right| = \\ &= \left| \frac{-9}{2\sqrt{2}} + \frac{7}{2\sqrt{2}} \right| = \left| \frac{-2}{2\sqrt{2}} \right| = \frac{1}{\sqrt{2}} \end{aligned}$$



Test: 
$$\vec{v} = \vec{v}_2 = \left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$
  
 $\vec{r}_{AB} = \vec{c}_B - \vec{c}_A = \left(\frac{9}{2}, \frac{7}{2}\right)$ 

 $S_{AB} = |\vec{v} \cdot \overrightarrow{r_{AB}}| = \frac{1}{\sqrt{2}}$ 

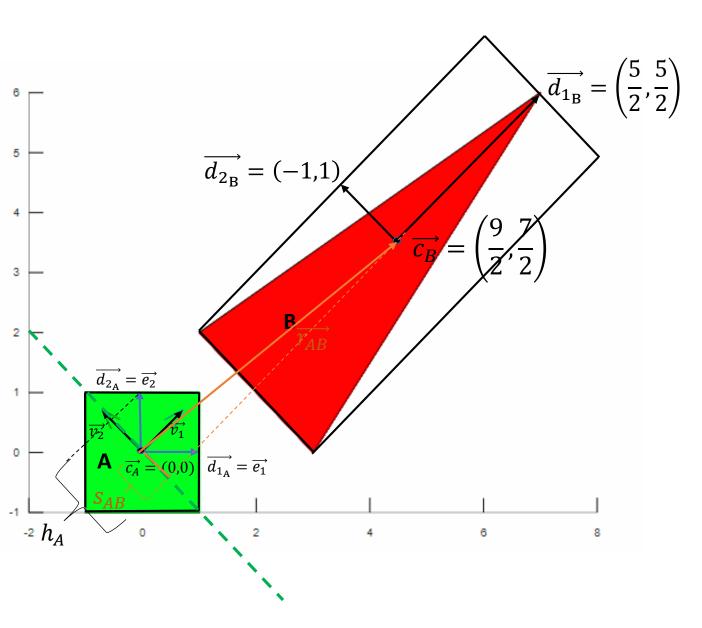
$$h_A = \left| \vec{v} \cdot \overrightarrow{d_{1_A}} \right| + \left| \vec{v} \cdot \overrightarrow{d_{2_A}} \right|$$



Test: 
$$\vec{v} = \vec{v}_2 = \left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$
  
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 $S_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = \frac{1}{\sqrt{2}}$ 

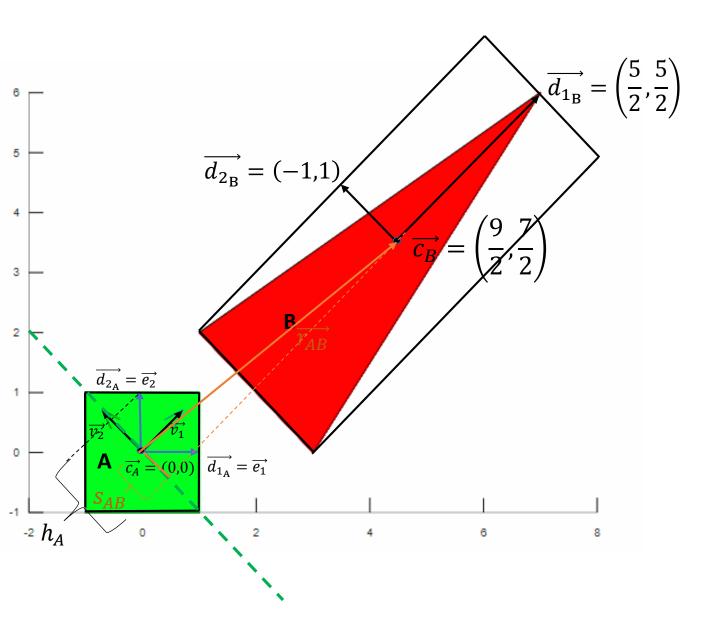
 $h_{A} = \left| \left( \frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right) \cdot (1,0) \right| + \left| \left( \frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right) \cdot (0,1) \right|$ 



Test: 
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 $S_{AB} = |\vec{v} \cdot \overrightarrow{r_{AB}}| = \frac{1}{\sqrt{2}}$ 

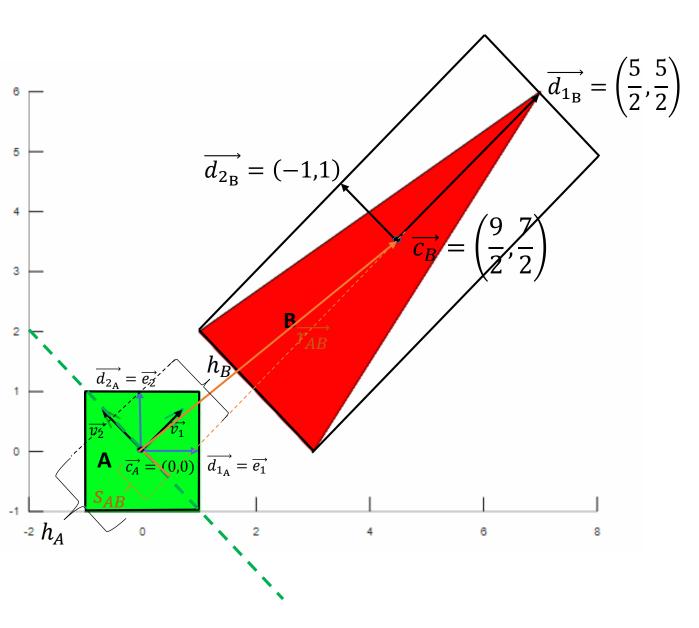
 $h_A = \left| \frac{-1}{\sqrt{2}} \right| + \left| \frac{1}{\sqrt{2}} \right|$ 



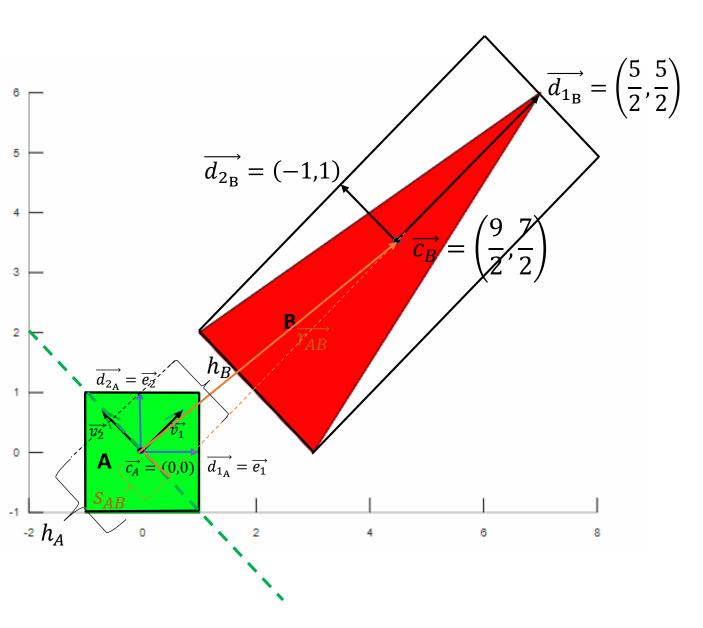
Test: 
$$\vec{v} = \vec{v}_2 = \left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$
  
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 $S_{AB} = |\vec{v} \cdot \overrightarrow{r_{AB}}| = \frac{1}{\sqrt{2}}$ 

$$h_A = \frac{2}{\sqrt{2}}$$



Test: 
$$\vec{v} = \vec{v}_2 = \left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$
  
 $\vec{r}_{AB} = \vec{c}_B - \vec{c}_A = \left(\frac{9}{2}, \frac{7}{2}\right)$   
 $s_{AB} = |\vec{v} \cdot \vec{r}_{AB}| = \frac{1}{\sqrt{2}}$   
 $h_A = \frac{2}{\sqrt{2}}$   
 $h_B = \left|\left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot \left(\frac{5}{2}, \frac{5}{2}\right)\right| + \left|\left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot (-1, 1)\right|$ 



Test: 
$$\vec{v} = \vec{v}_2 = \left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$
  
 $\vec{r}_{AB} = \vec{c}_B - \vec{c}_A = \left(\frac{9}{2}, \frac{7}{2}\right)$   
 $s_{AB} = |\vec{v} \cdot \vec{r}_{AB}| = \frac{1}{\sqrt{2}}$ 

$$h_A = \frac{2}{\sqrt{2}}$$
$$h_B = 0 + \frac{1+1}{\sqrt{2}}$$

Test:  $\vec{v} = \vec{v_2} = \left(\frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$ 

 $s_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = \frac{1}{\sqrt{2}}$ 

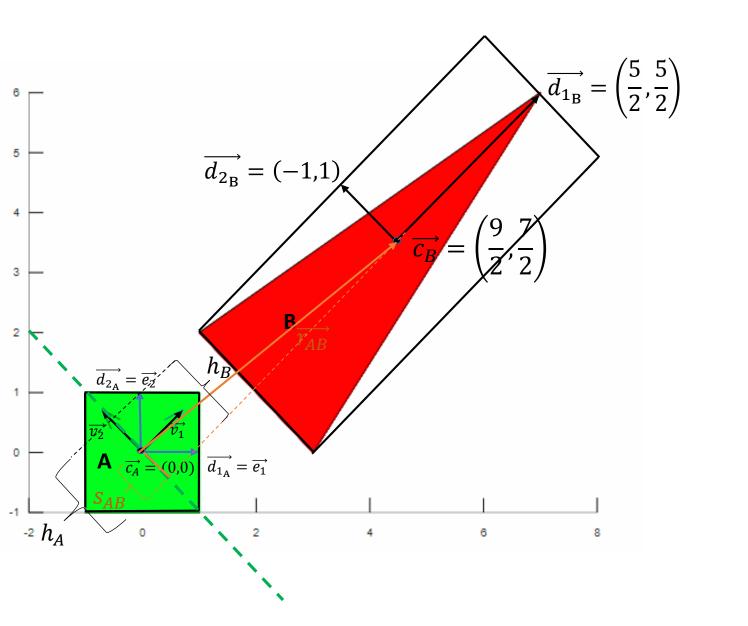
 $h_A + h_B = \frac{2+2}{\sqrt{2}} = \frac{4}{\sqrt{2}}$ 

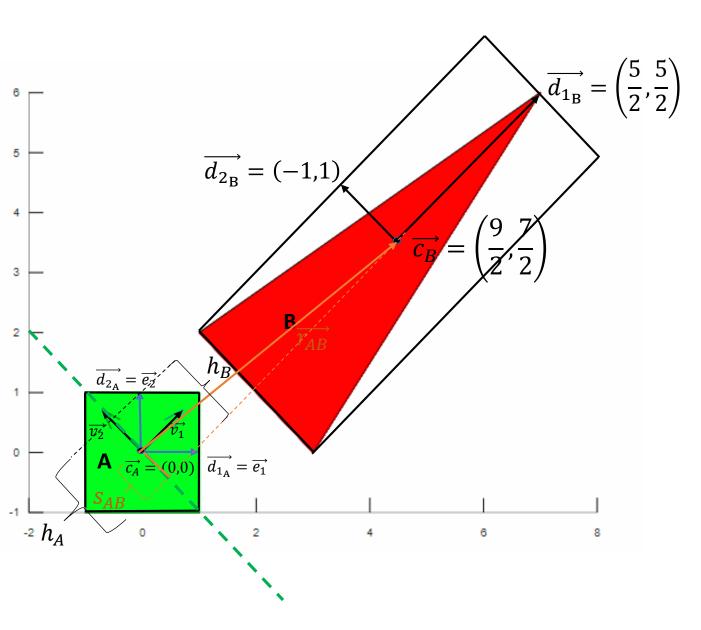
 $\frac{?}{s_{AB}} > h_A + h_B$ 

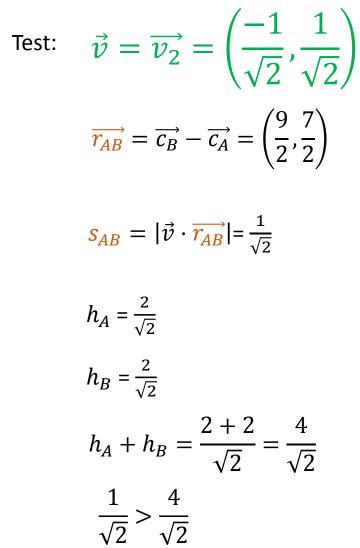
 $h_A = \frac{2}{\sqrt{2}}$ 

 $h_B = \frac{2}{\sqrt{2}}$ 

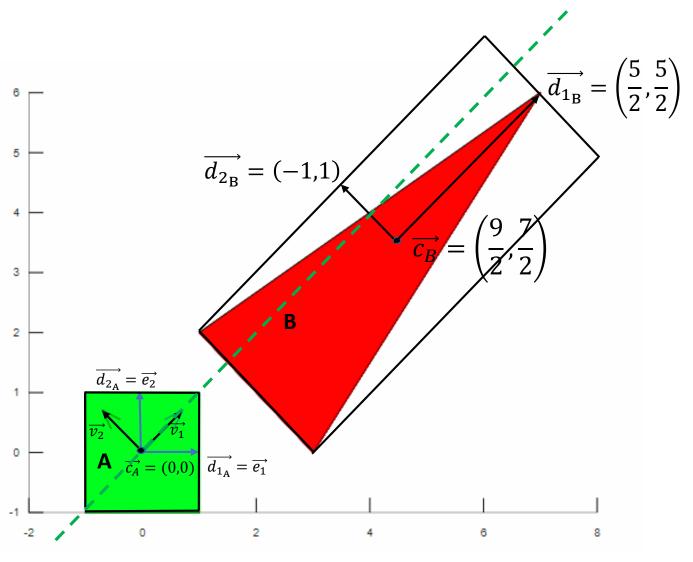
 $\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$ 



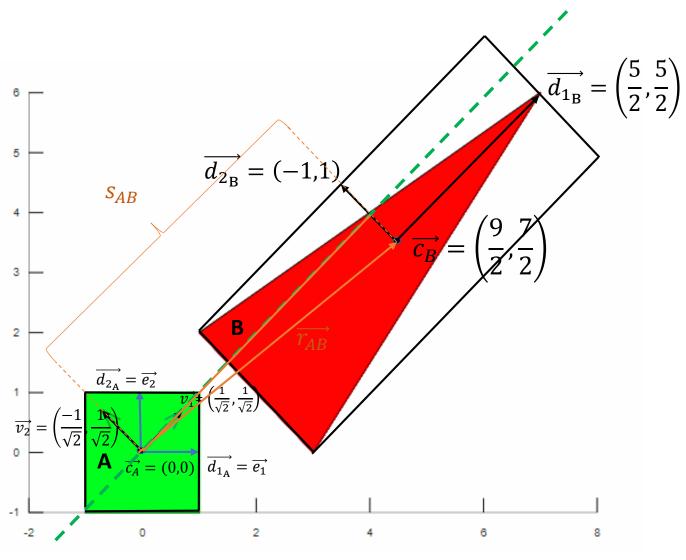




not true  $\Rightarrow$  can't say that they are not in a collision

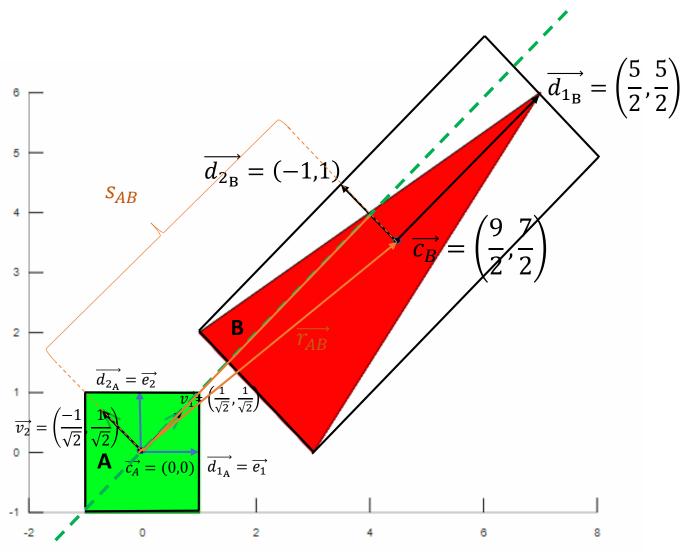


Test: 
$$\vec{v} = \vec{v_1} = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$



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 $\vec{r_{AB}} = \vec{c_B} - \vec{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$ 

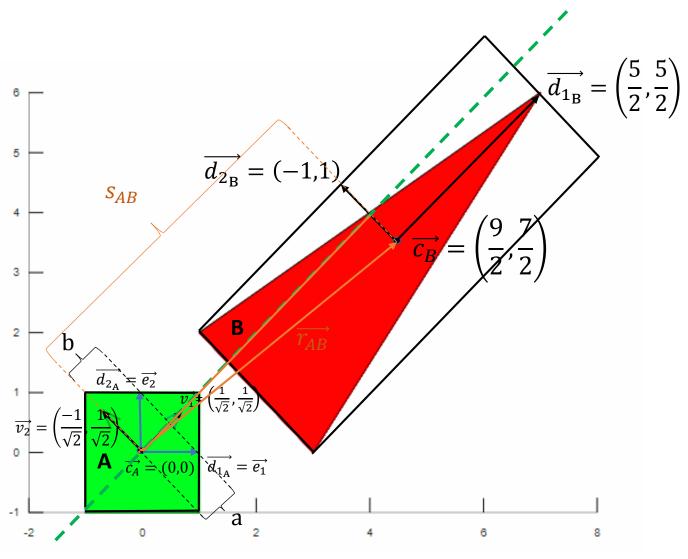
$$\begin{aligned} \mathbf{S}_{AB} &= |\vec{v} \cdot \vec{r_{AB}}| = \left| \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right) \cdot \left(\frac{9}{2}, \frac{7}{2}\right) \right| = \\ &= \left| \frac{9}{2\sqrt{2}} + \frac{7}{2\sqrt{2}} \right| = \frac{16}{2\sqrt{2}} = \frac{8}{\sqrt{2}} \end{aligned}$$



Test: 
$$\vec{v} = \vec{v_1} = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$
  
 $\vec{r_{AB}} = \vec{c_B} - \vec{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$ 

 $S_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = \frac{8}{\sqrt{2}}$ 

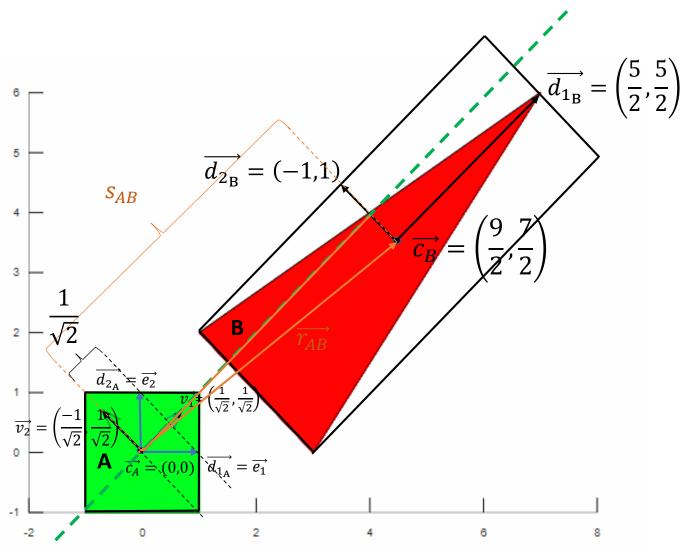
$$h_A = \left| \vec{v} \cdot \overrightarrow{d_{1_A}} \right| + \left| \vec{v} \cdot \overrightarrow{d_{2_A}} \right|$$



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$$\vec{v} = \vec{v_1} = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$
  
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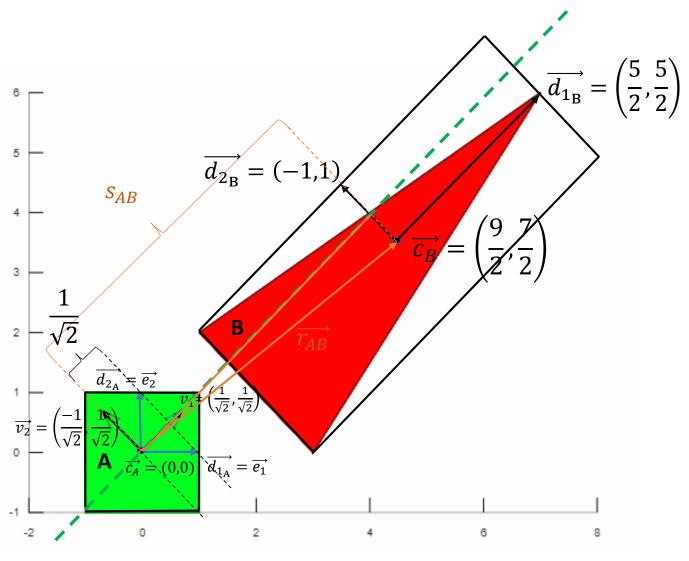
 $h_{A} = \left| \left( \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right) \cdot (1,0) \right| + \left| \left( \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right) \cdot (0,1) \right|$ a b



Test: 
$$\vec{v} = \vec{v_1} = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$
  
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 $S_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = \frac{8}{\sqrt{2}}$ 

$$h_A = \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}}$$

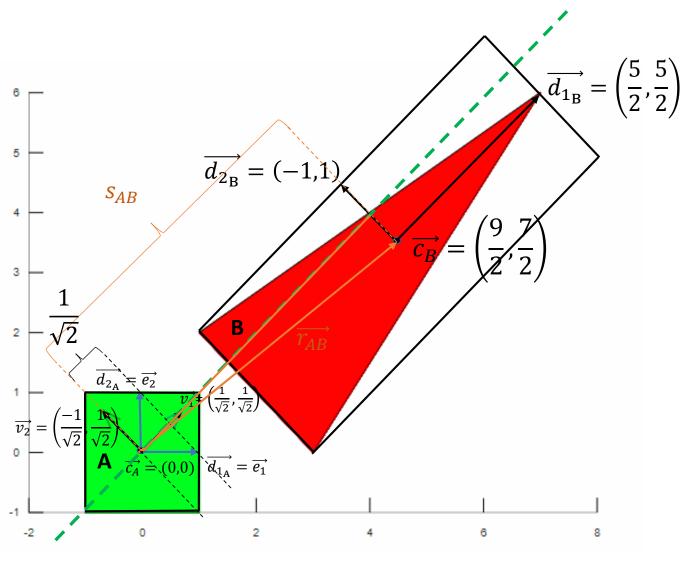


$$\vec{v} = \overrightarrow{v_1} = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$
  
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 $S_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = \frac{8}{\sqrt{2}}$ 

 $h_A = \frac{2}{\sqrt{2}}$ 

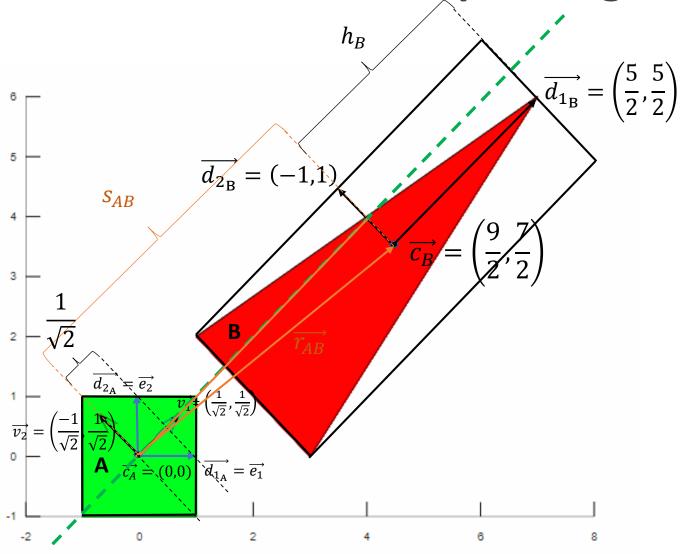
Test:



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$$\vec{v} = \vec{v_1} = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$
  
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 $s_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = \frac{8}{\sqrt{2}}$ 

$$h_A = \frac{2}{\sqrt{2}}$$
$$h_B = \left| \left( \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right) \cdot \left( \frac{5}{2}, \frac{5}{2} \right) \right| + \left| \left( \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right) \cdot (-1, 1) \right|$$

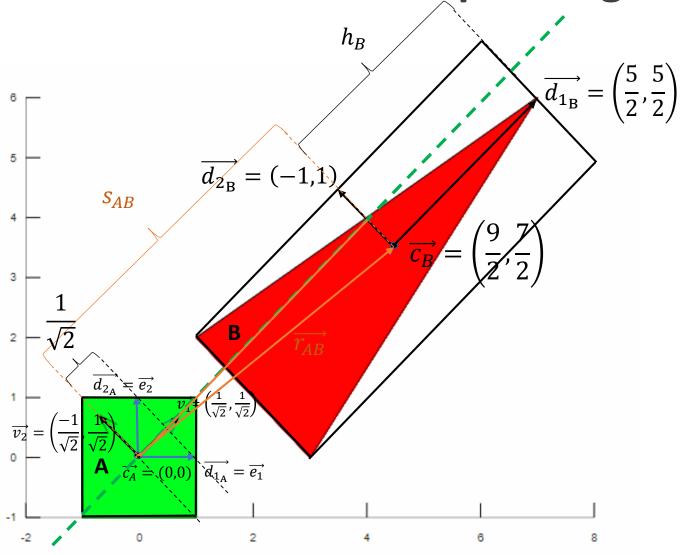
Test:



$$\vec{v} = \overrightarrow{v_1} = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$
  
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 $s_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = \frac{8}{\sqrt{2}}$ 

$$h_A = \frac{2}{\sqrt{2}}$$
$$h_B = \frac{5}{2\sqrt{2}} + \frac{5}{2\sqrt{2}} = \frac{5}{\sqrt{2}}$$



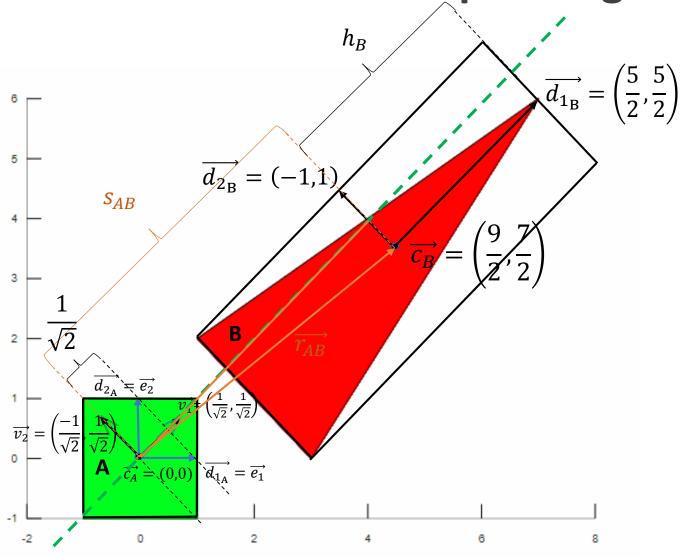
Test:  $\vec{v} = \vec{v_1} = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$  $\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$  $s_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = \frac{8}{\sqrt{2}}$ h -2

$$h_{A} - \frac{5}{\sqrt{2}}$$

$$h_{B} = \frac{5}{2\sqrt{2}} + \frac{5}{2\sqrt{2}} = \frac{5}{\sqrt{2}}$$

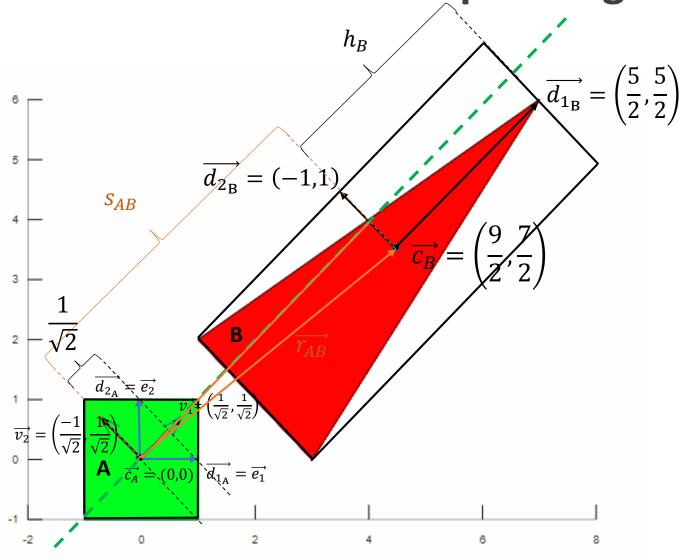
$$h_{A} + h_{B} = \frac{2+5}{\sqrt{2}} = \frac{7}{\sqrt{2}}$$

$$s_{AB} > h_{A} + h_{B}$$



Test:  $\vec{v} = \vec{v_1} = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$  $\overrightarrow{r_{AB}} = \overrightarrow{c_B} - \overrightarrow{c_A} = \left(\frac{9}{2}, \frac{7}{2}\right)$  $s_{AB} = |\vec{v} \cdot \vec{r_{AB}}| = \frac{8}{\sqrt{2}}$ 

 $h_{A} = \frac{2}{\sqrt{2}}$   $h_{B} = \frac{5}{2\sqrt{2}} + \frac{5}{2\sqrt{2}} = \frac{5}{\sqrt{2}}$   $h_{A} + h_{B} = \frac{2+5}{\sqrt{2}} = \frac{7}{\sqrt{2}}$   $s_{AB} \stackrel{?}{>} h_{A} + h_{B}$   $\frac{8}{\sqrt{2}} > \frac{7}{\sqrt{2}}$ 



Test: 
$$\vec{v} = \vec{v}_1 = \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$
  
 $\vec{r}_{AB} = \vec{c}_B - \vec{c}_A = \left(\frac{9}{2}, \frac{7}{2}\right)$   
 $s_{AB} = |\vec{v} \cdot \vec{r}_{AB}| = \frac{8}{\sqrt{2}}$   
 $h_A = \frac{2}{\sqrt{2}}$   
 $h_B = \frac{5}{2\sqrt{2}} + \frac{5}{2\sqrt{2}} = \frac{5}{\sqrt{2}}$   
 $h_A + h_B = \frac{2+5}{\sqrt{2}} = \frac{7}{\sqrt{2}}$   
 $\frac{8}{\sqrt{2}} > \frac{7}{\sqrt{2}}$ 

true  $\Rightarrow$  they are not in a collision