
Computer Graphics

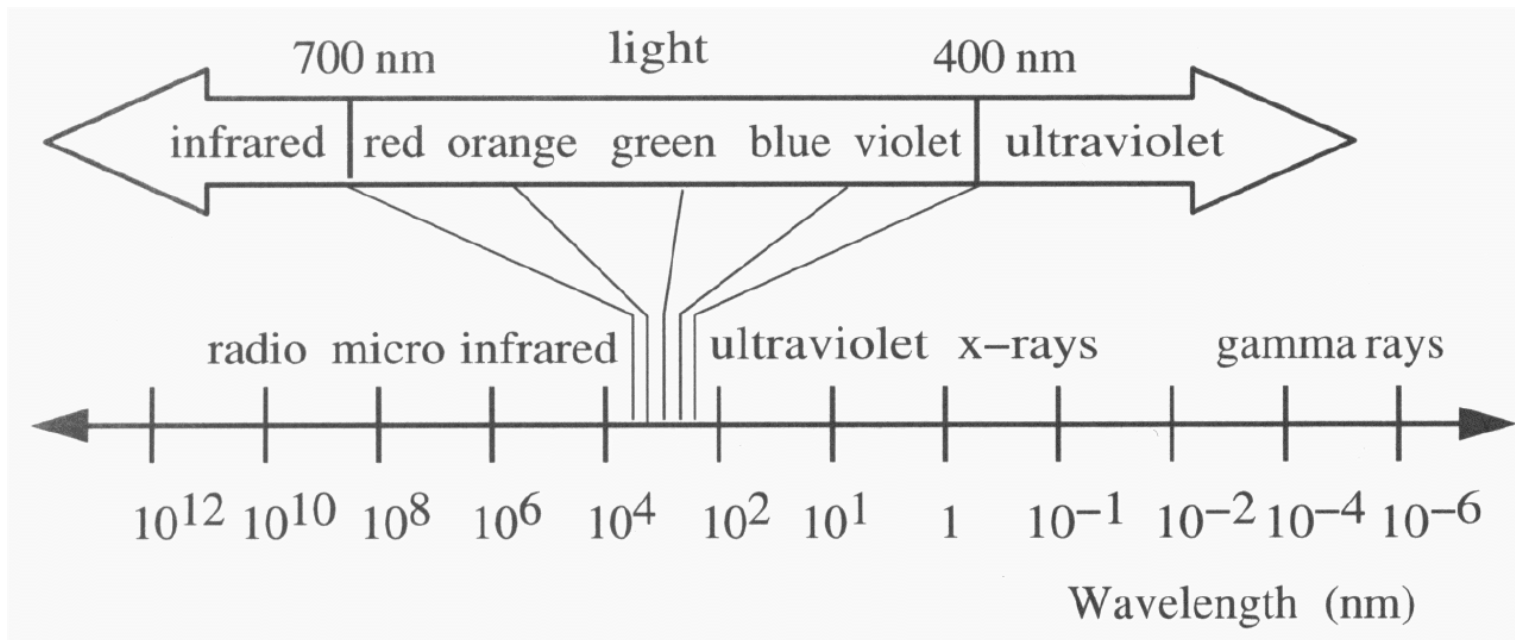
- The Human Visual System -

Overview

- **Last time**
 - Antialiasing
 - Super-Sampling
- **Today**
 - The Human Visual System
 - The eye
 - Early vision
 - High-level analysis
 - Color perception
- **Next lecture**
 - Color spaces

Light

- **Electromagnetic radiation**
- **Visible spectrum: ~ 400 to 700 nm**



Radiation Law

- **Physical model for light**

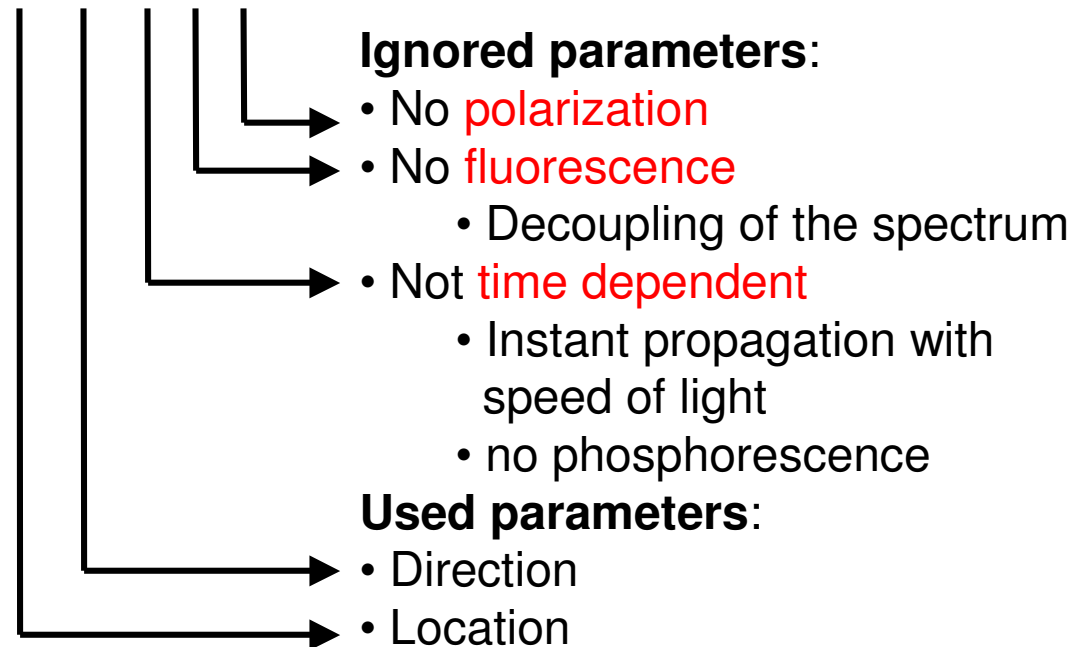
- Wave/particle-dualism

- Electromagnetic radiation wave model

- Photons: $E_{ph}=h\nu$ particle model & ray optics

- Plenoptic function

- $L = L(x, \omega, t, v, \gamma)$, 5 dimensional,



Photometry

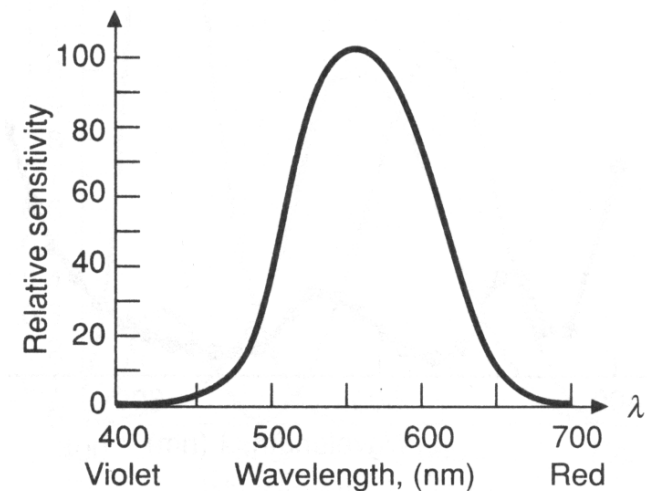
- **Equivalent units to radiometry**

- Weight with **luminous efficiency function** $V(\lambda)$
(luminous efficiency function)
- Spectral or “total” units

$$\Phi_v = K_m \int V(\lambda) \Phi_e(\lambda) d\lambda$$

$$K_m = 680 \text{ lm} / \text{W}$$

- Distinction in English simple:
 - “rad”: radiometric unit
 - “lum”: photometric unit



Radiometric Units

Specification	Definition	Symbol	Unit	Notation
Energie energy		Q_e	[J= Ws] Joule	Strahlungsenergie radiant energy
Leistung, Fluß power, flux	dQ/dt	Φ_e	[W= J/s]	Strahlungsfluß radiant flux
Flußdichte flux density	$dQ/dA dt$	E_e	[W/m ²]	Bestrahlungsstärke Irradiance
Flußdichte flux density	$dQ/dA dt$	$M_e = B_e$	[W/m ²]	Radiom. Emissionsvermögen Radiosity
	$dQ/dA^\Phi d\omega dt$	L_e	[W/m²/sr]	Strahlungsdichte Radiance
Intensität intensity	$dQ/d\omega dt$	I_e	[W/sr]	Strahlungsstärke radiant intensity

Photometric Units

With luminous efficiency function weighted units

Specification	Definition	Symbol	Units	Notation
Energie energy		Q_v	[talbot]	Lichtmenge luminous energy
Leistung, Fluß power, flux	dQ/dt	Φ_v	[lm (Lumen) = talbot/s]	Lichtstrom luminous flux
Flußdichte flux density	$dQ/dA dt$	E_v	[lux = lm/m ²]	Beleuchtungsstärke Illuminance
Flußdichte flux density	$dQ/dA dt$	[M _v =] B _v	[lux]	Photom. Emissionsvermögen Luminosity
	$dQ/dA^\Phi d\omega dt$	L_v	[lm/m ² /sr]	Leuchtdichte Luminance
Intensität intensity	$dQ/d\omega dt$	I_v	[cd (candela) = lm/sr]	Lichtstärke radiant intensity

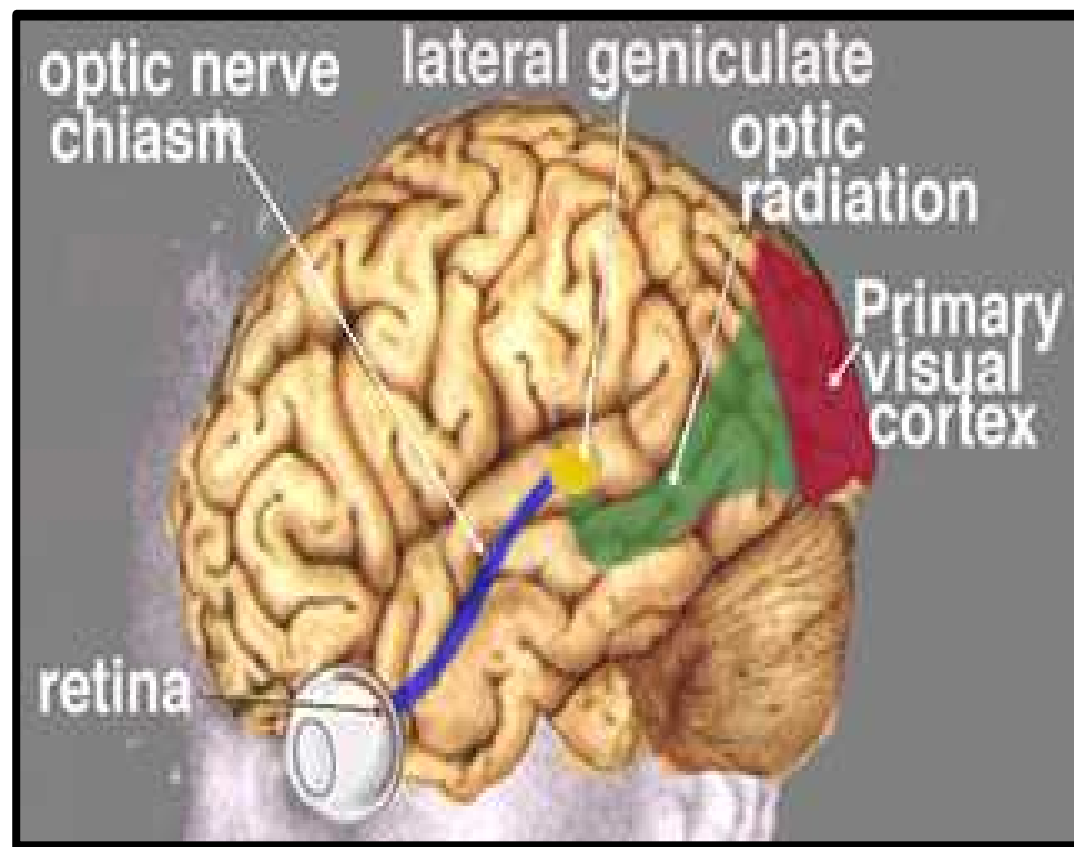
Illumination: samples

- **Typical illumination intensities**

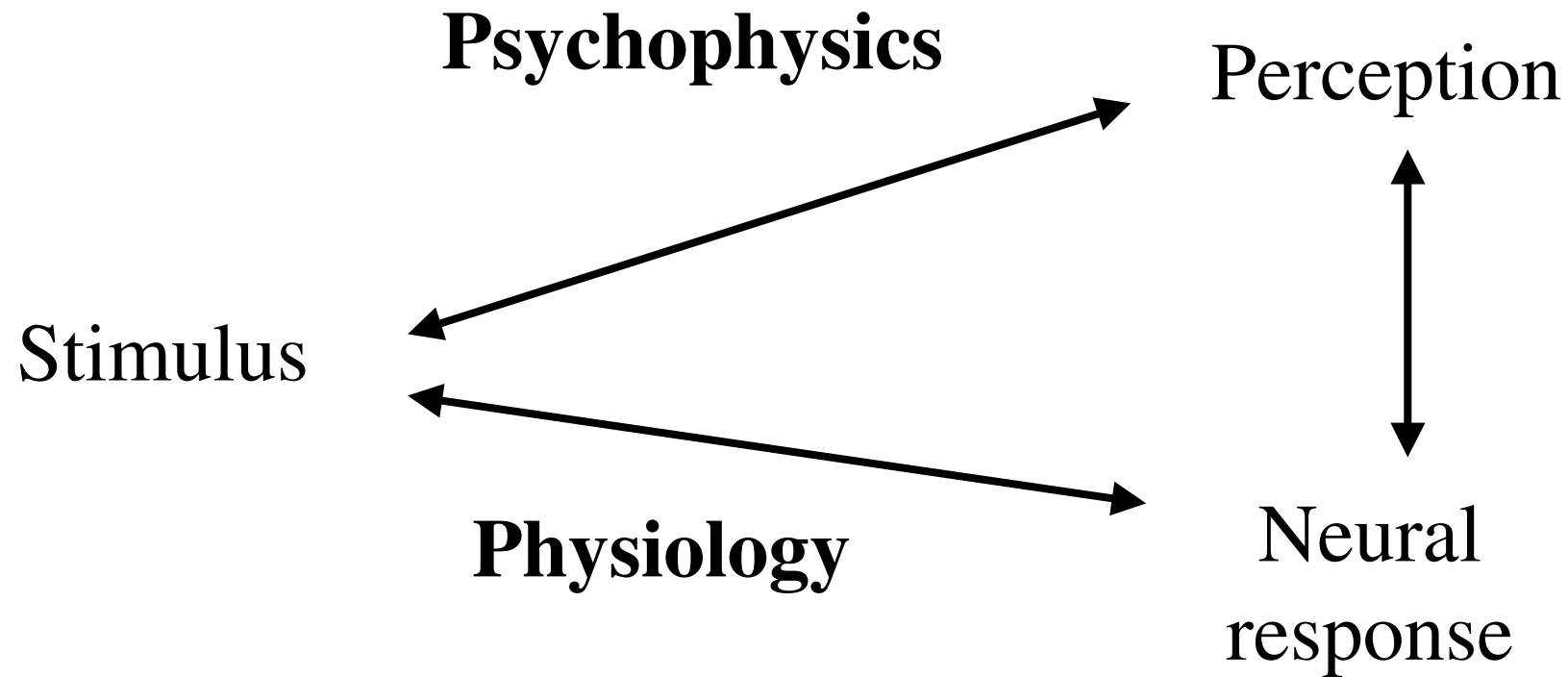
Light source	Illumination intensity [lux]
Direct solar radiation	25.000 – 110.000
Day light	2.000 – 27.000
Sunset	1 – 108
Moon light	0.01 – 0.1
Starry night	0.0001 – 0.001
TV studio	5.000 – 10.000
Shop lighting	1.000 – 5.500
Office lighting	200 – 550
Home lighting	50 – 220
Street lighting	0.1 – 20

Human Visual System

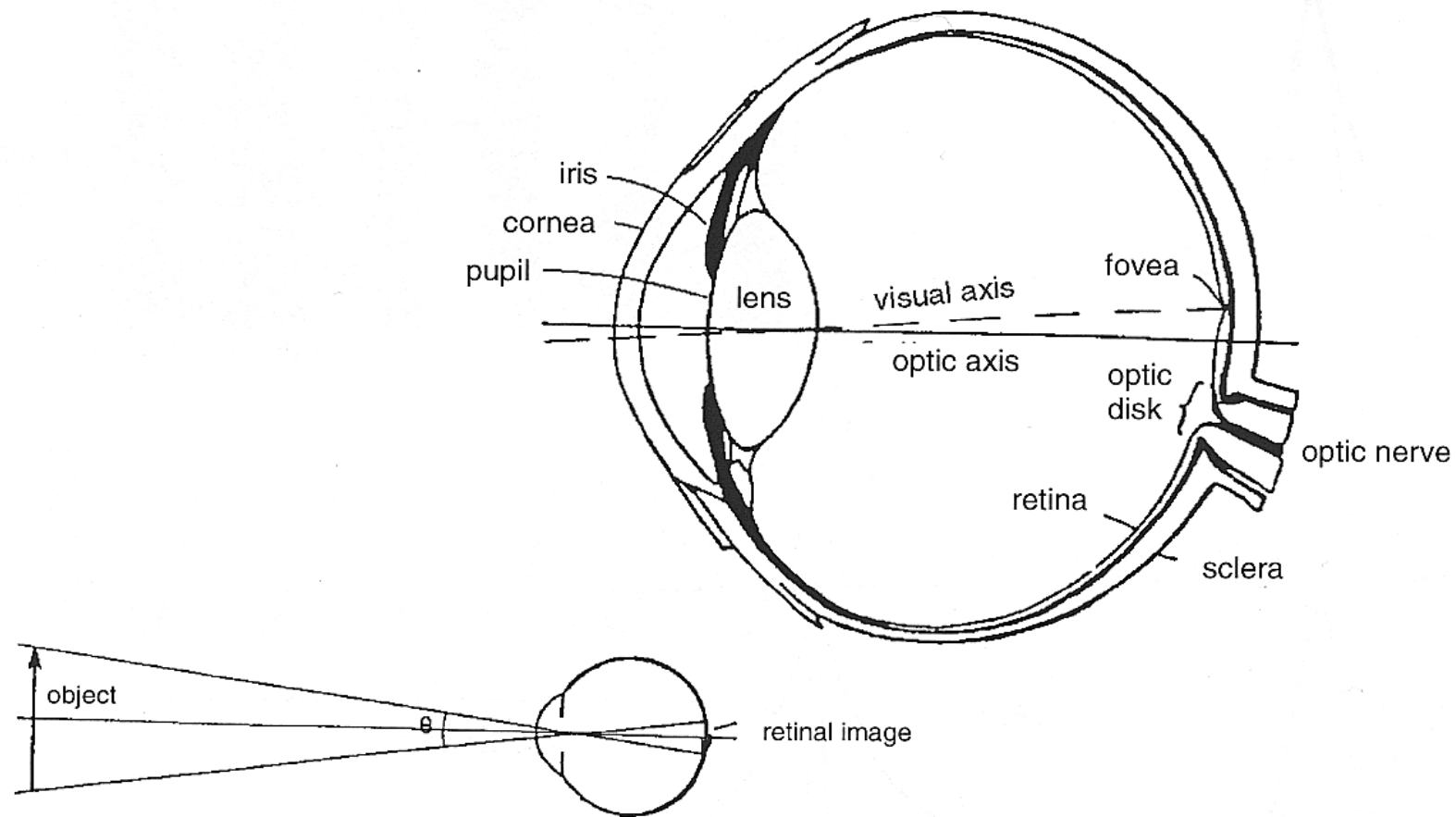
- Physical structure well established
- Perceptual behaviour is a complex process



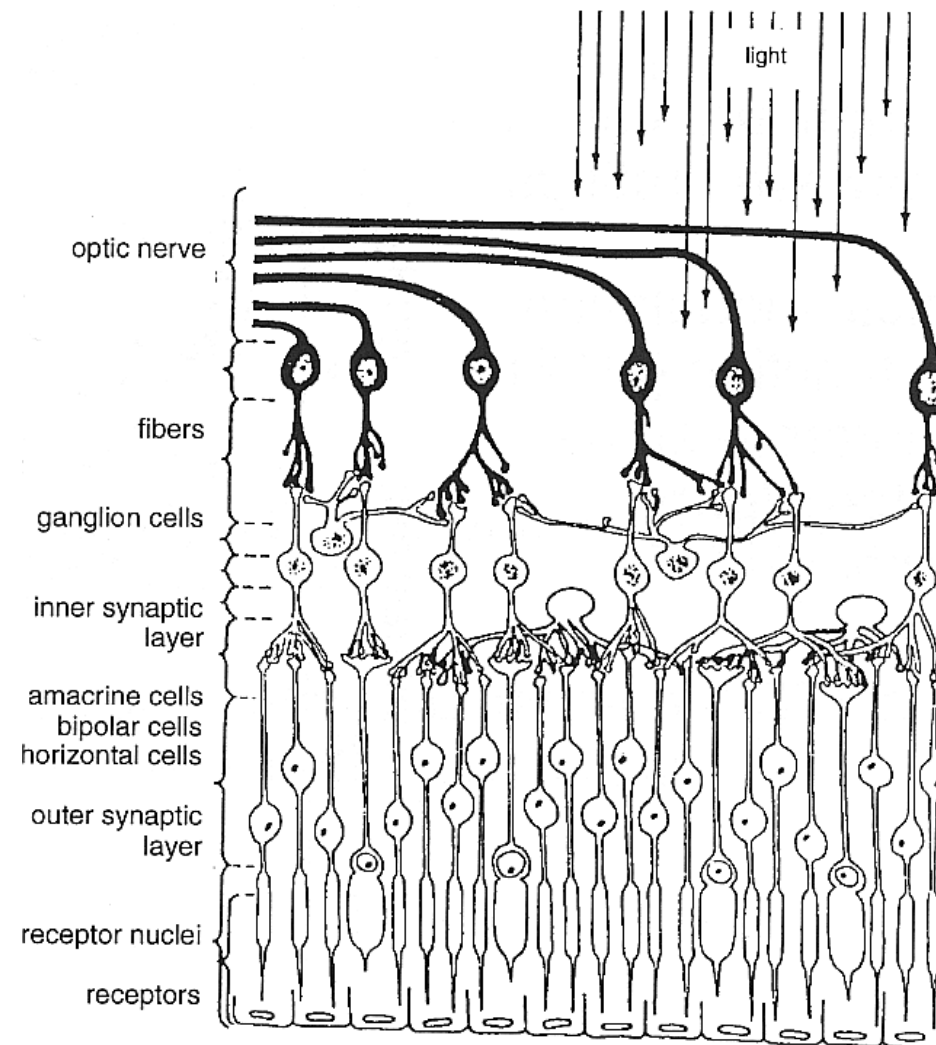
HVS - Relationships



Perception and Eye



Retina



Eye

- **Eye:**
 - Fovea: Ø 1-2 visual degrees
 - 6-7 Mio. **cones**, circa 0.4 arc seconds sized
 - No rods
 - Three different cone types: L(ong), M(edium), S(hort wavelength)
 - Linked directly with optical nerves
 - Resolution: 10 arc minutes (S, blue), 0.5 arc minutes (L, M)
 - Adaptation of light intensity only through cones
 - Periphery:
 - 75-150 Mio. **rods**, night vision, S/W
 - Response to stimulation of approx. 5 photons/sec. (@ 500 nm)
 - Many thousands of cells are linked with nerves
 - Bad resolution
 - Good flickering sensitivity

Resolution of the Eye

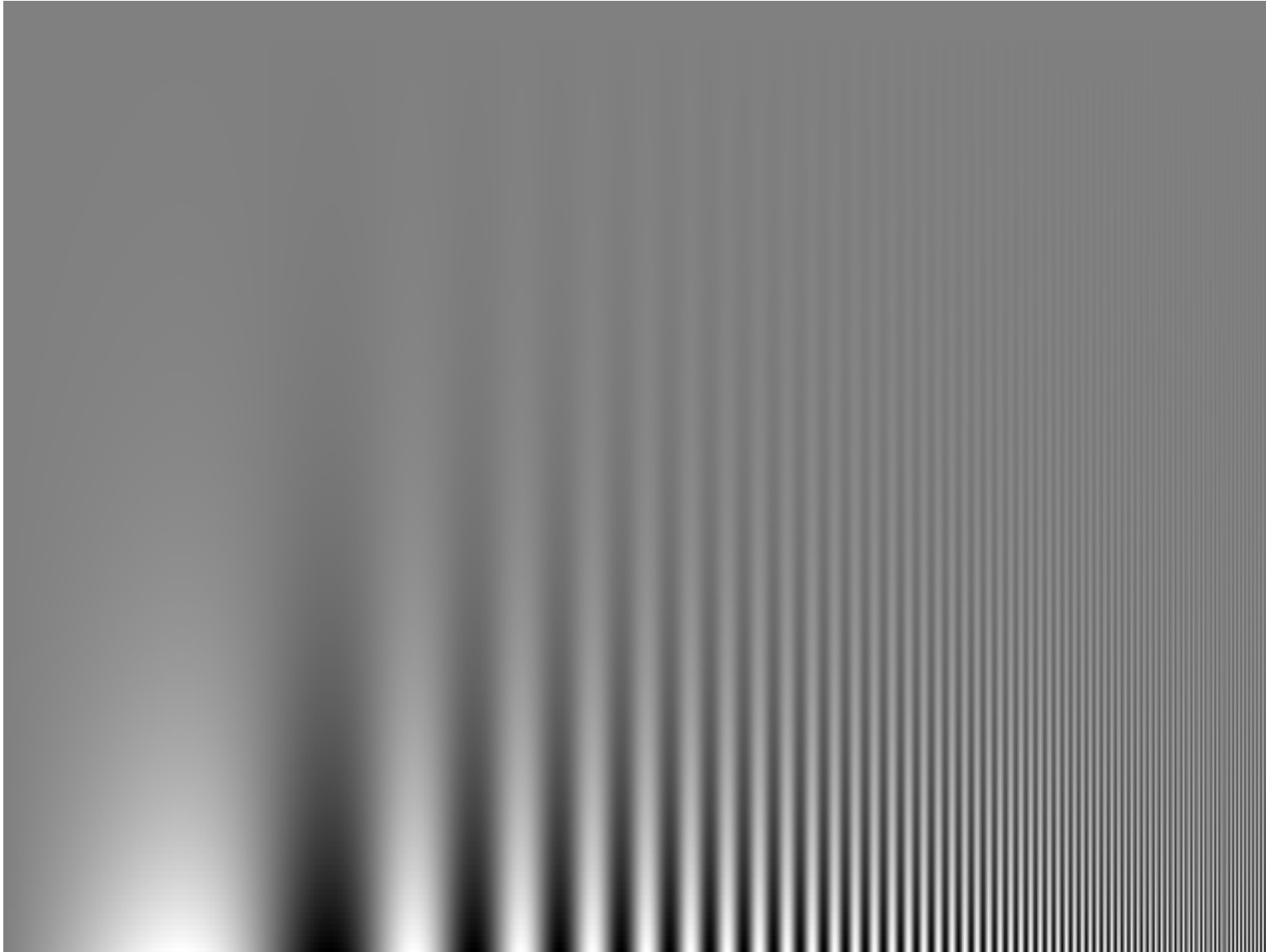
- **Resolution-experiments**

- Line pairs: 50-60/degree → resolution .5 arc minutes
- Line offset: 5 arc seconds = 1/6 !! (hyperacuity)



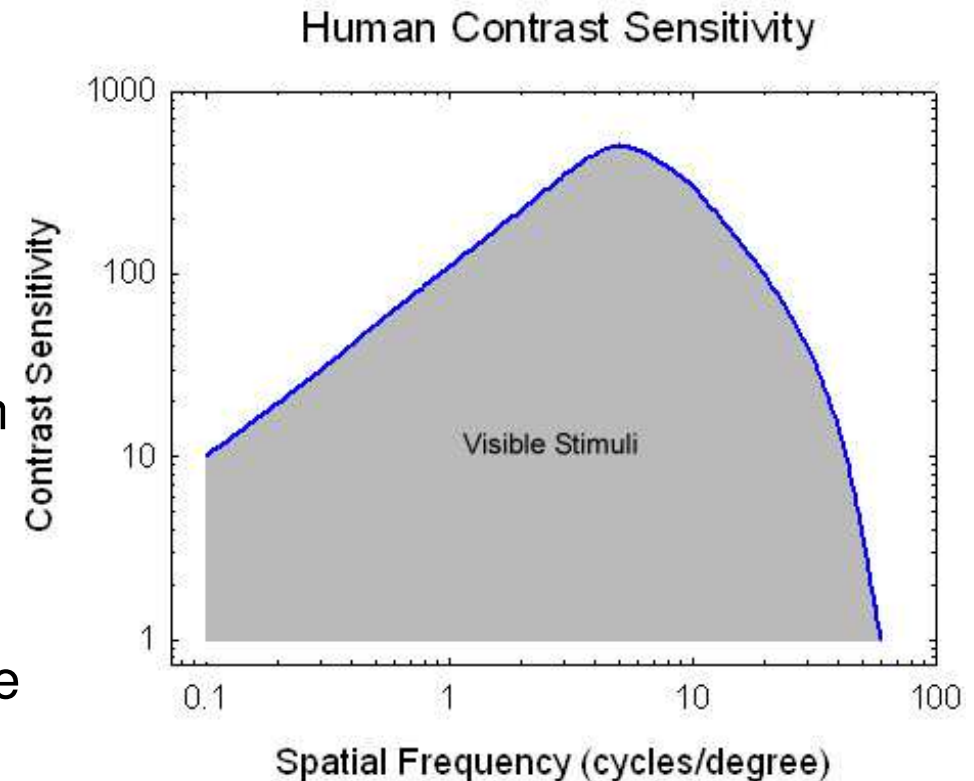
- Eye micro-tremor: 60-100 Hz, 5 μ m (2-3 photoreceptor spacings)
 - Super-resolution
 - 19" display at 60 cm: 18.000 x 18.000 (3000 x 3000) Pixel
- **Eye fixates itself**
 - Automatic gaze tracking
 - Overall high resolution
 - **Visual acuity increased by**
 - Brighter objects
 - High contrast

Luminance Contrast Sensitivity

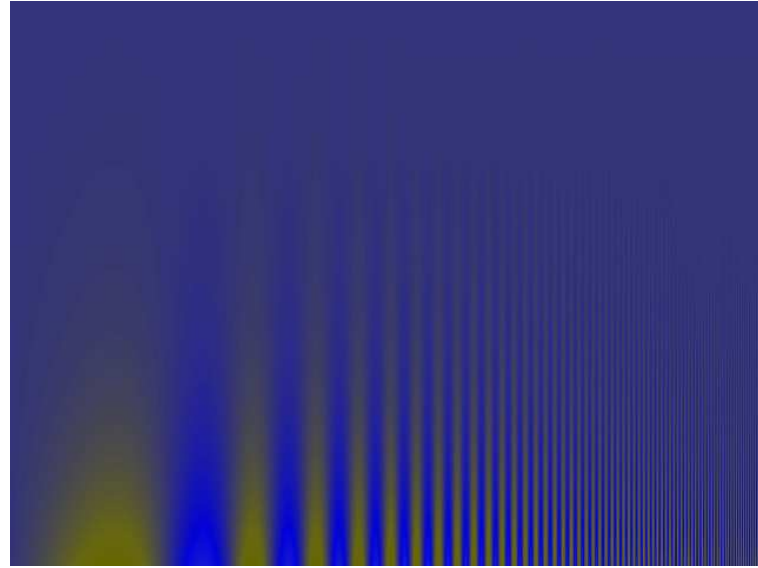
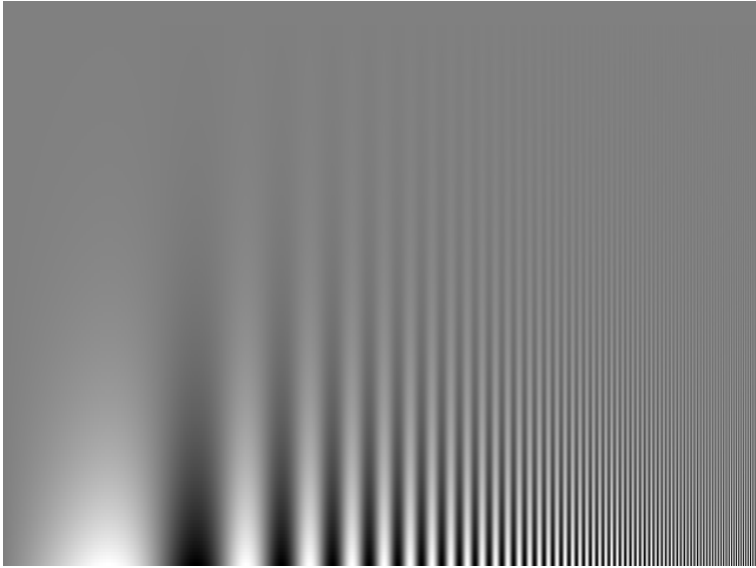


Contrast Sensitivity

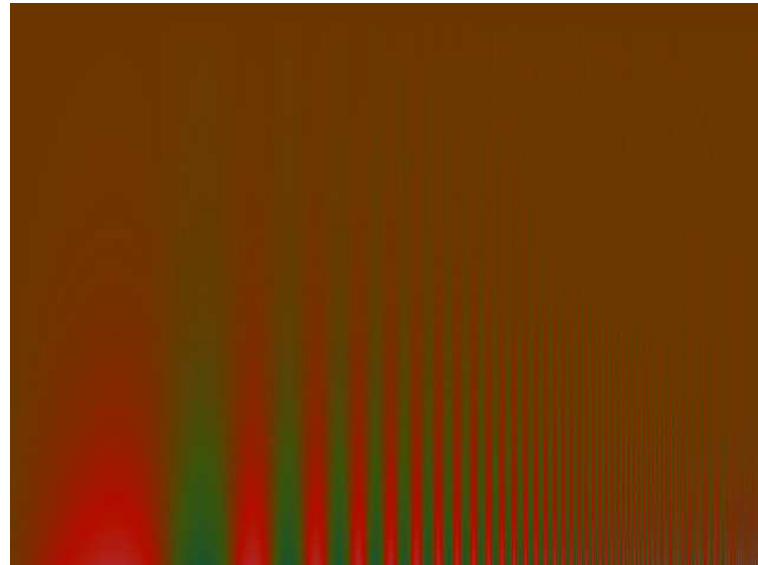
- **Sensitivity:**
1 / threshold contrast
- **Maximum acuity:**
5 cycles/degree (0.2 %)
 - Decrease toward low frequencies: lateral inhibition
 - Decrease toward high frequencies: sampling rate (Poisson disk)
 - Upper limit: 60 cycles/degree
- **Medical diagnosis**
 - Glaucoma (affects peripheral vision: low frequencies)
 - Multiple sclerosis (affects optical nerve: notches in contrast sensitivity)



Color Contrast Sensitivity



- **Color vs. luminance vision system**
 - Higher sensitivity at lower frequencies
 - High frequencies less visible
- **Image compression**



Threshold Sensitivity Function

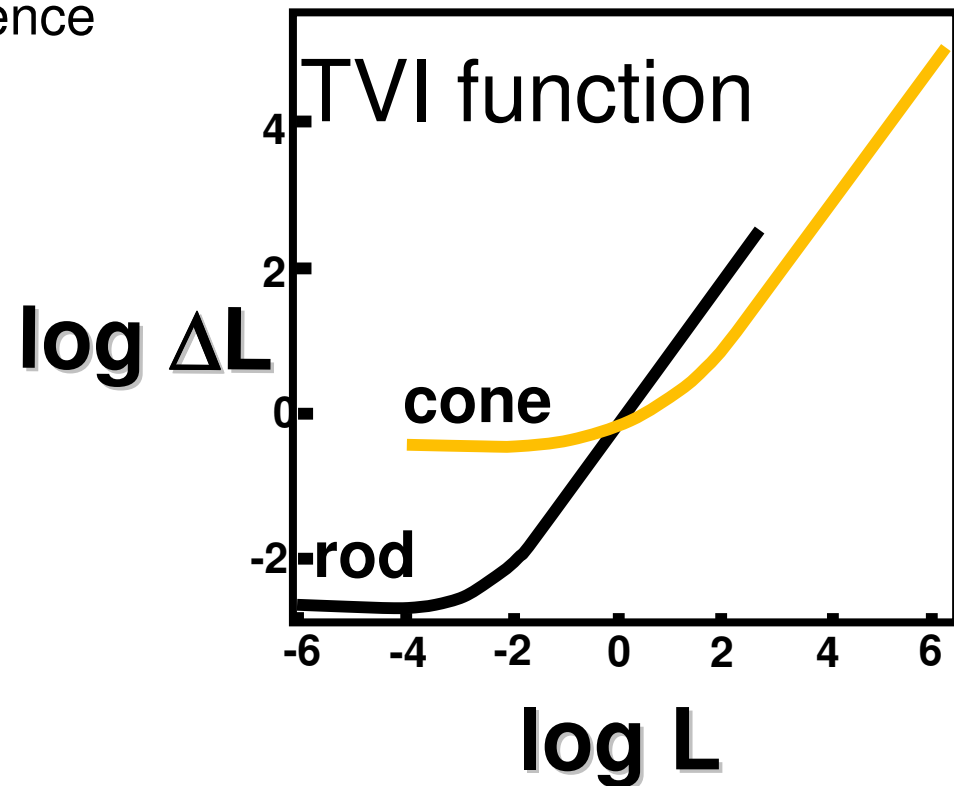
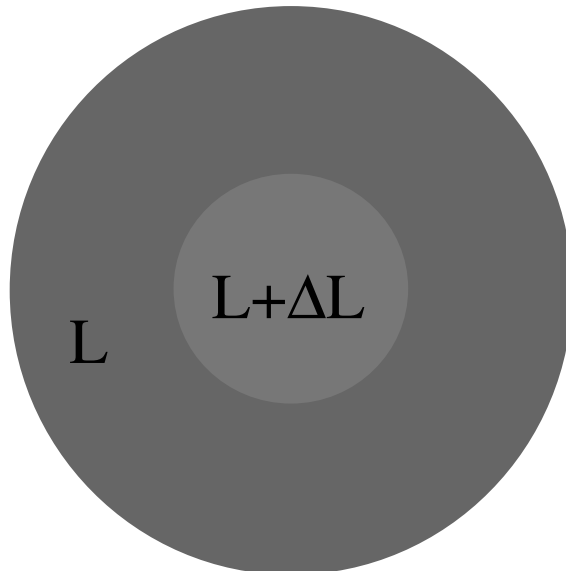
- **Weber-Fechner Law**

- Perceived brightness = \log (radiant intensity)

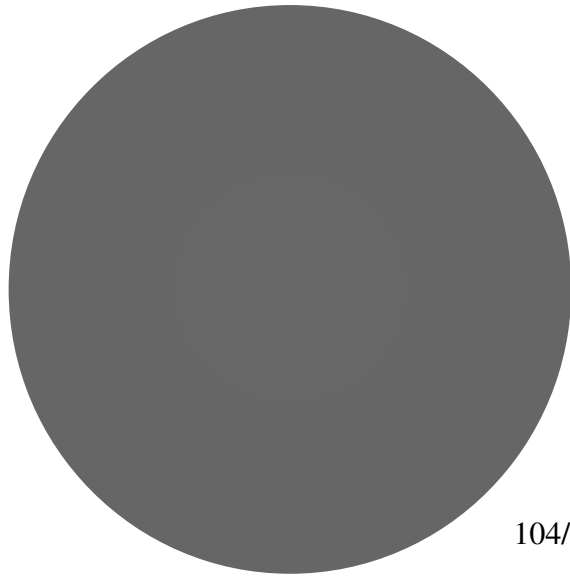
$$E = K + c \log I_v$$

- Perceivable intensity difference

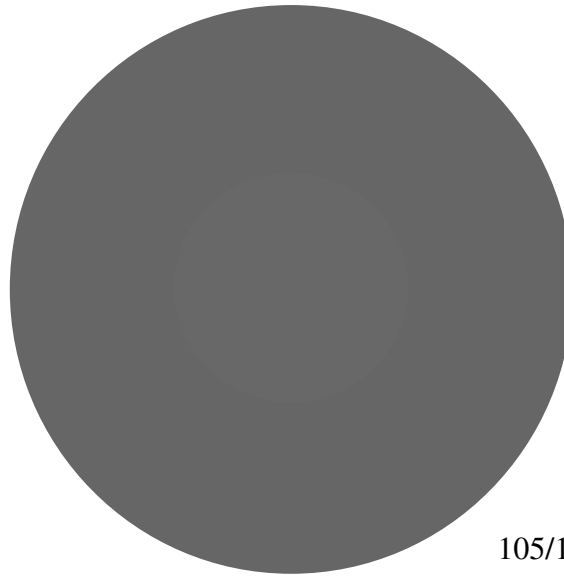
- 10 cd vs. 12 cd: $\Delta L = 2\text{cd}$
 - 20 cd vs. 24 cd: $\Delta L = 4\text{cd}$
 - 30 cd vs. 36 cd: $\Delta L = 6\text{cd}$



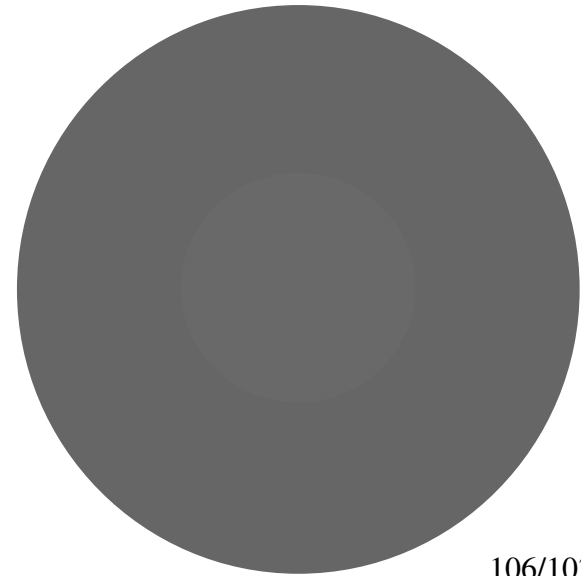
Weber-Fechner Examples



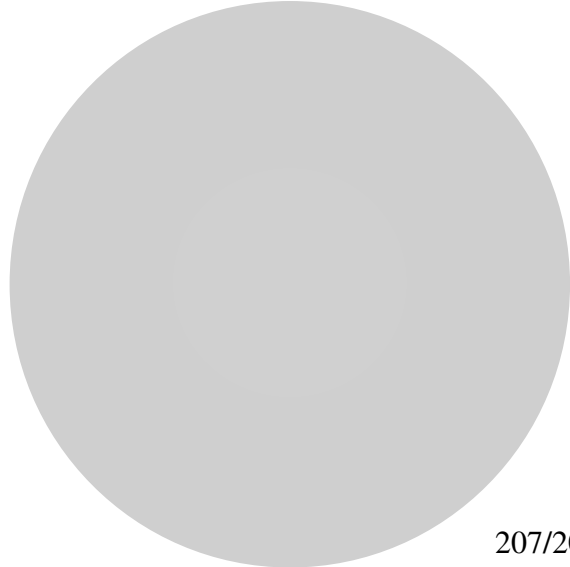
104/103



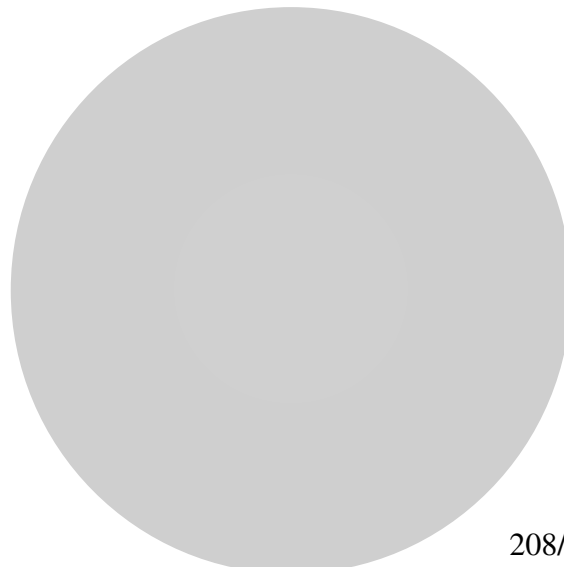
105/103



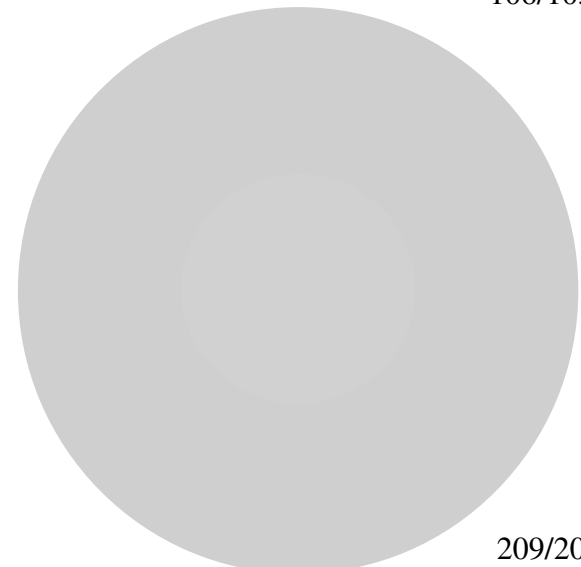
106/103



207/206

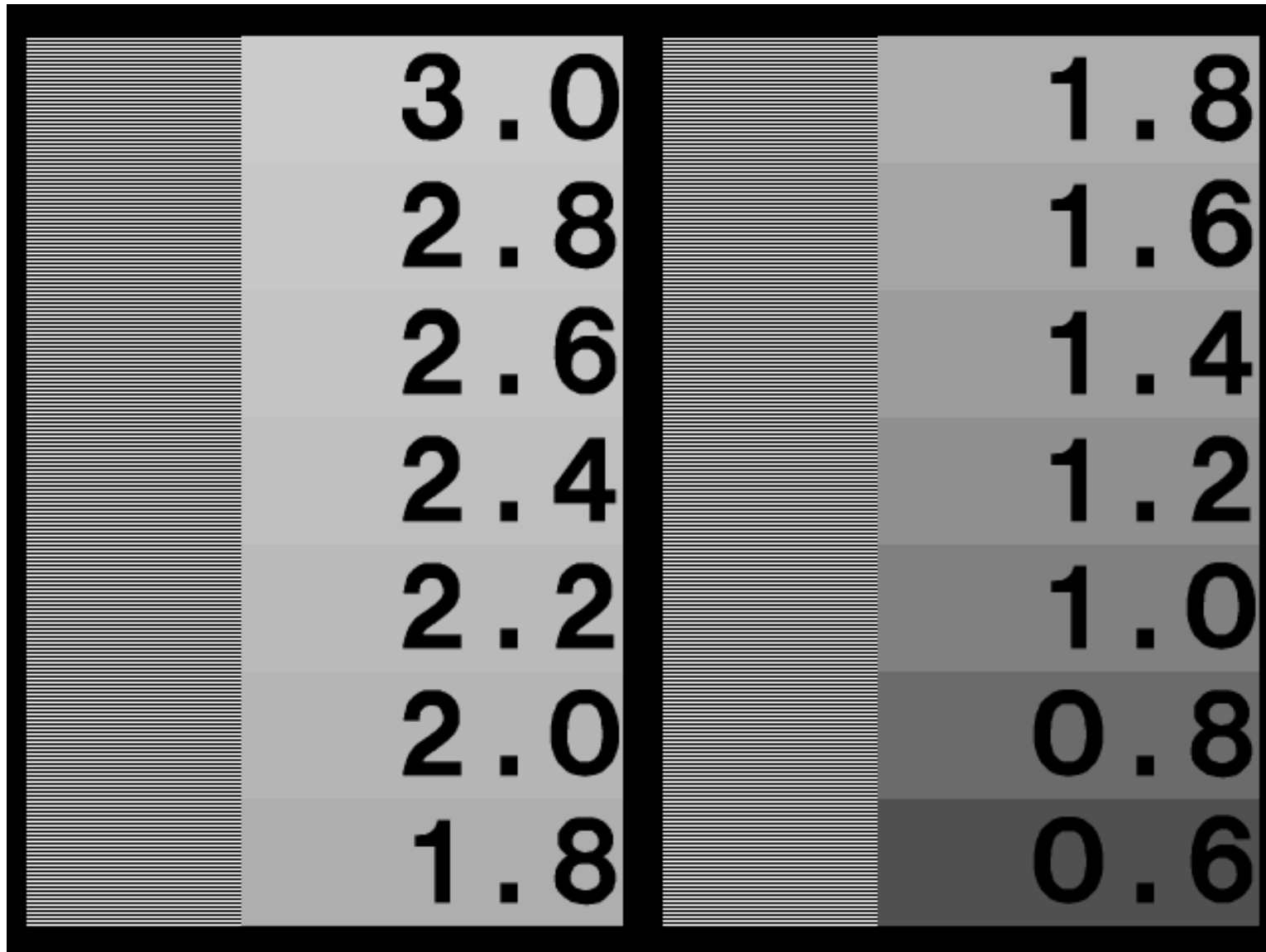


208/206



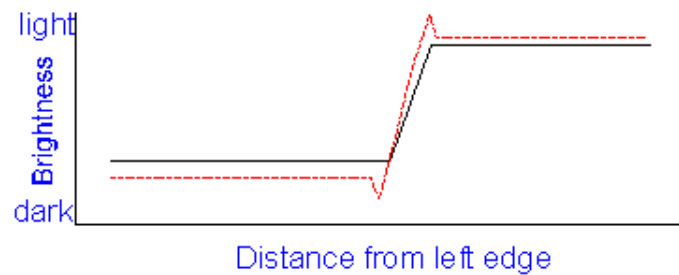
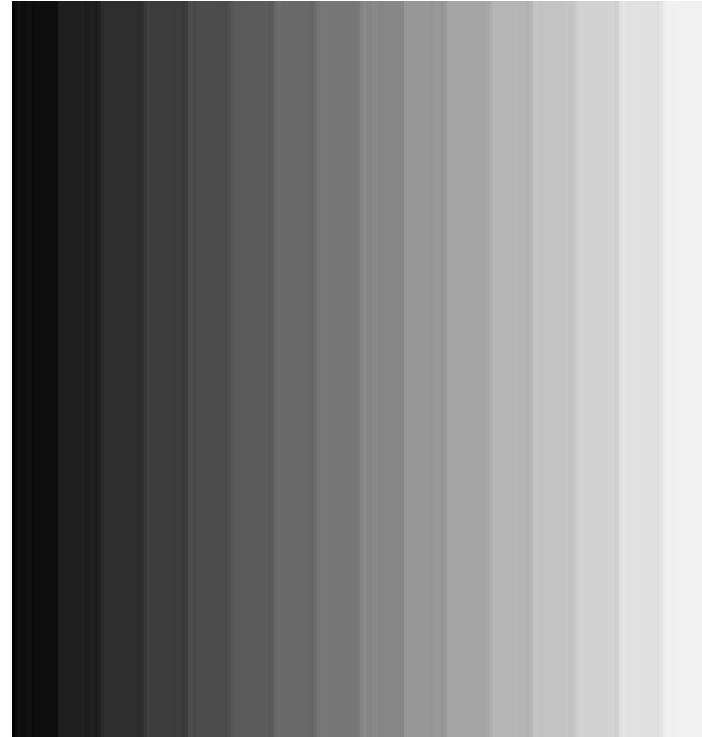
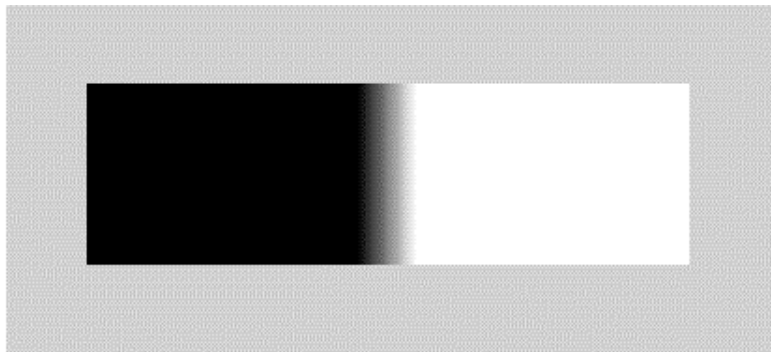
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Intermediate: Gamma Test



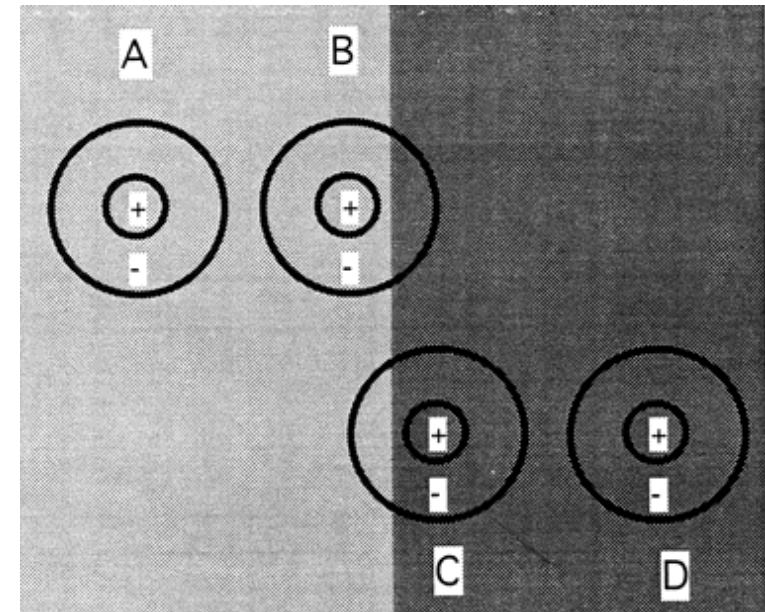
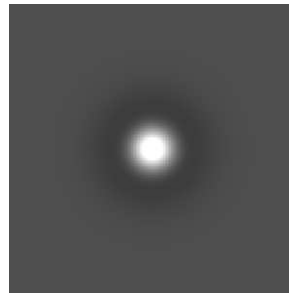
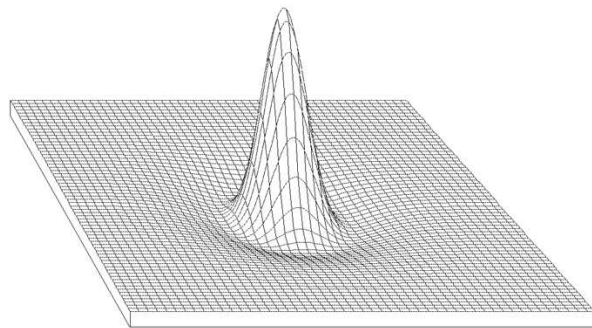
Mach Bands

- **“Overshooting” along edges**
 - Extra-bright rims on bright sides
 - Extra-dark rims on dark sides
- **Lateral Inhibition**



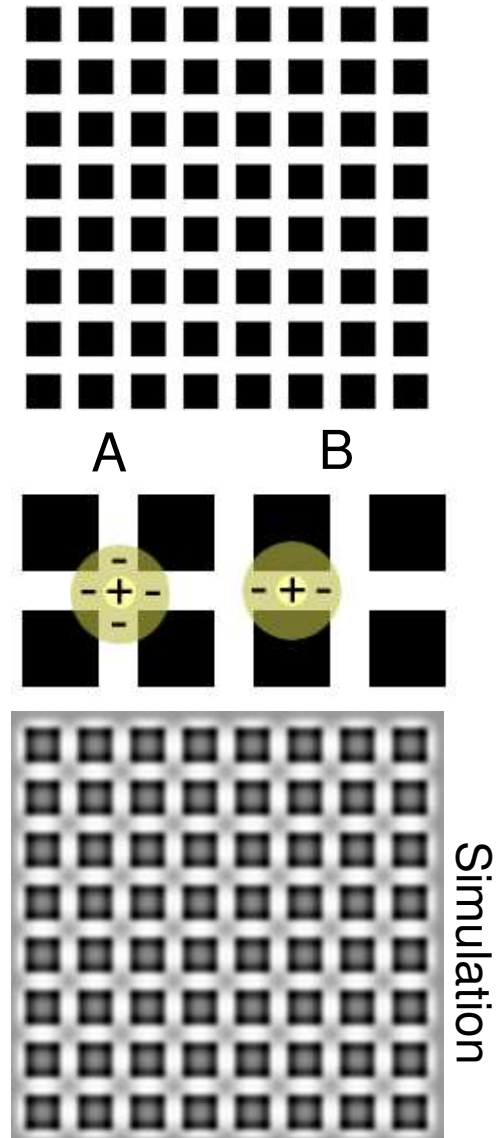
Lateral Inhibition

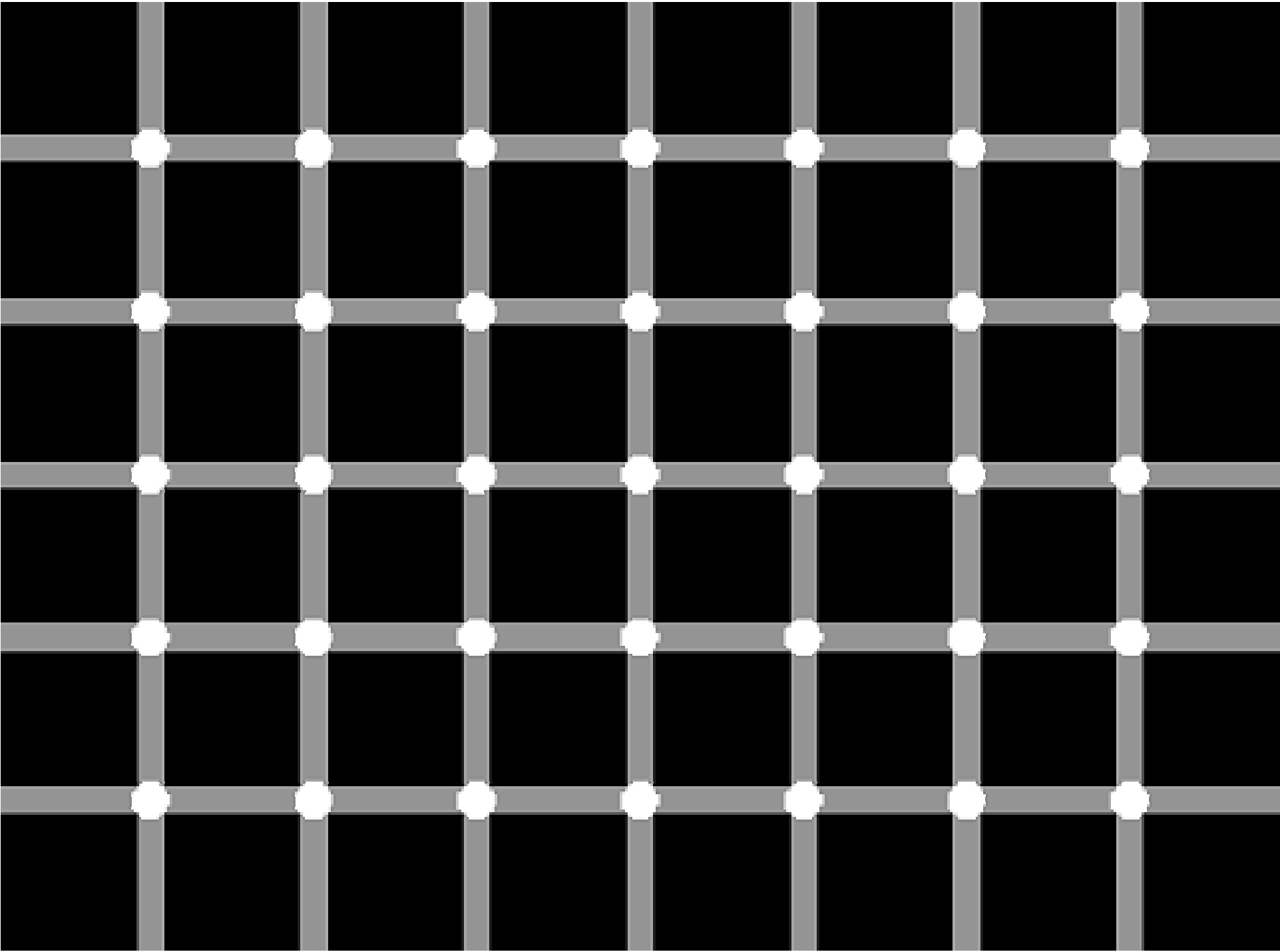
- **Pre-processing step within retina**
 - Surrounding brightness level weighted negatively
 - A: bright stimulus, maximal bright inhibition
 - B: bright stimulus, partial bright inhibition => stronger response
 - C: dark stimulus, partial dark inhibition => weaker response
 - D: dark stimulus, maximal dark inhibition
- **High-pass filter**
 - Enhances contrast along edges
 - Difference-of-Gaussians (DOG) function



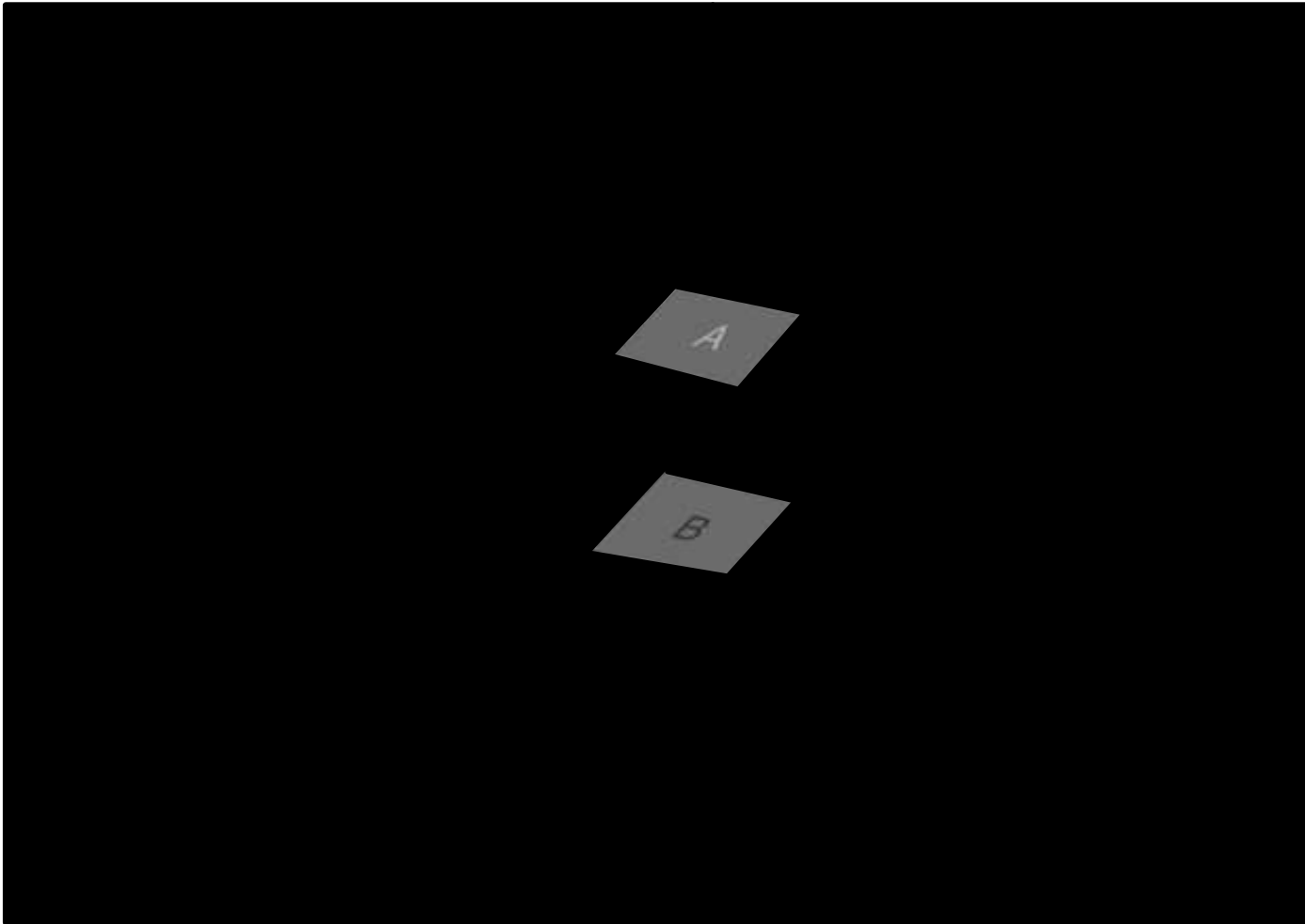
Lateral Inhibition: Hermann Grid

- **Dark dots at crossings**
- **Explanation**
 - Crossings (A)
 - More surround stimulation (more bright area)
 - ⇒ More inhibition
 - ⇒ Weaker response
 - Streets (B)
 - Less surround stimulation
 - ⇒ Less inhibition
 - ⇒ Greater response
- **Filtered with DOG function**
 - Darker at crossings, brighter in streets
 - Appears more steady
 - What if reversed ?

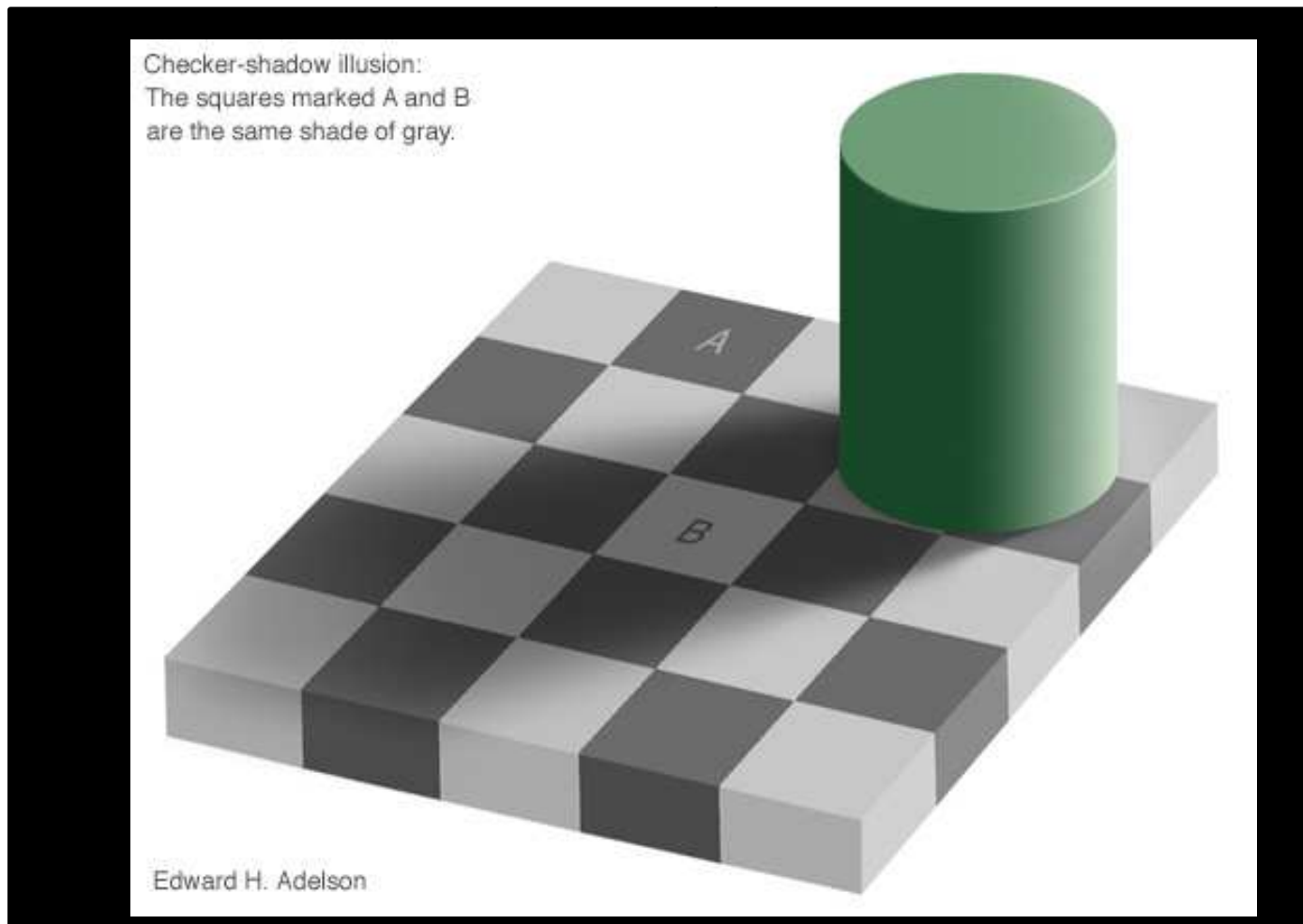




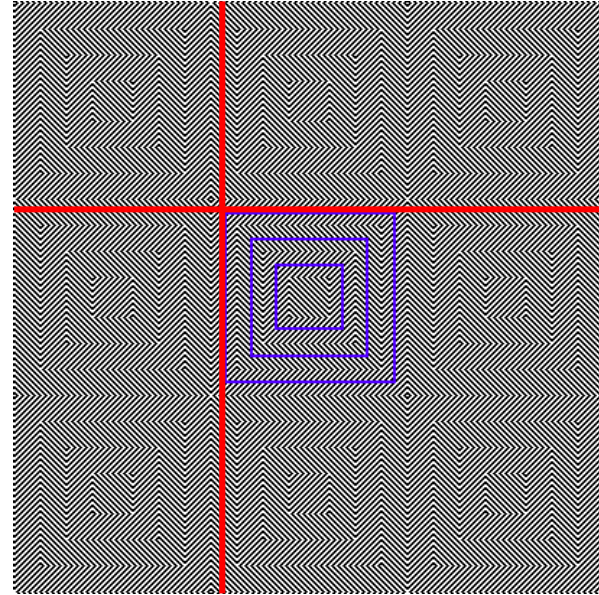
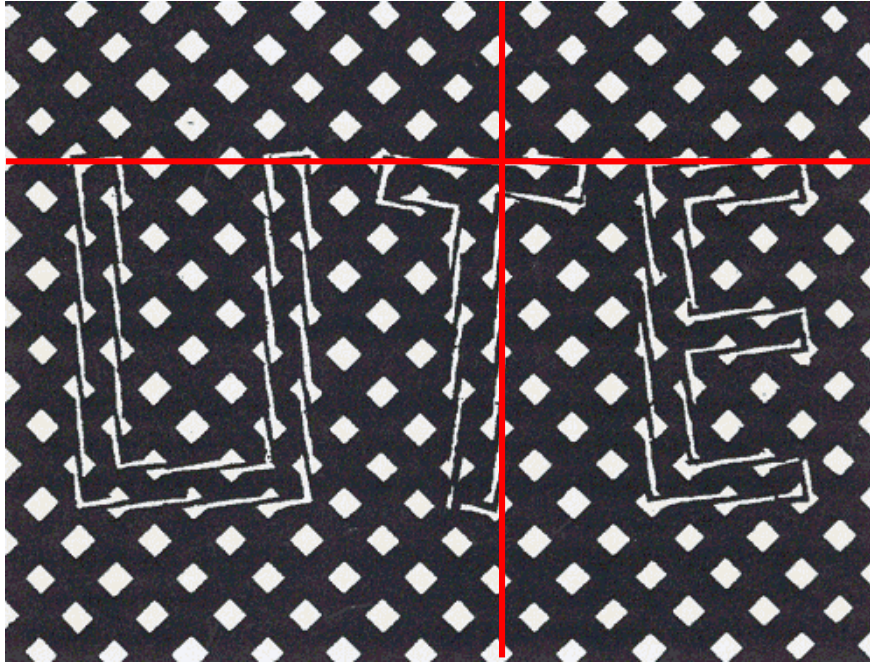
High-Level Contrast Processing



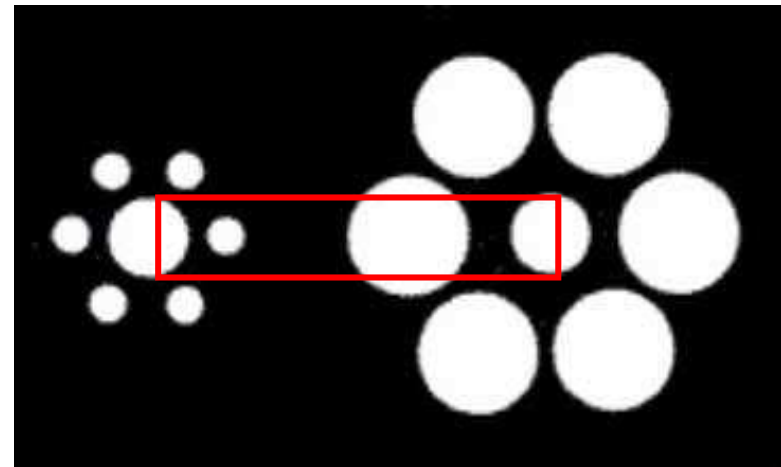
High-Level Contrast Processing



Shape Perception

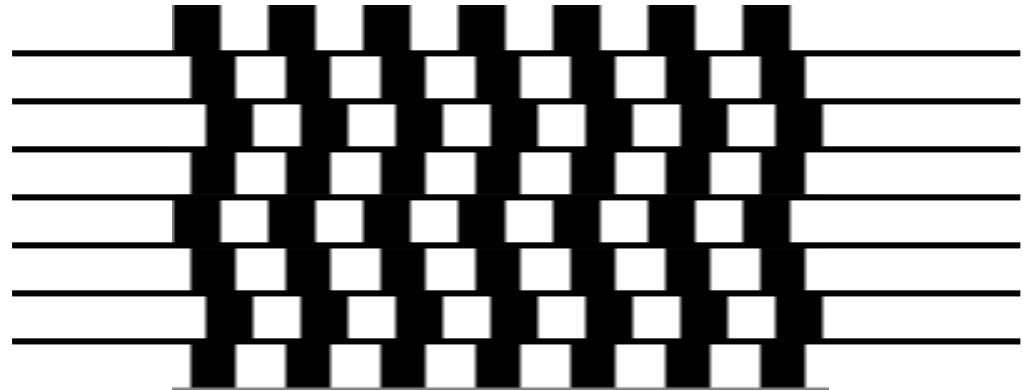
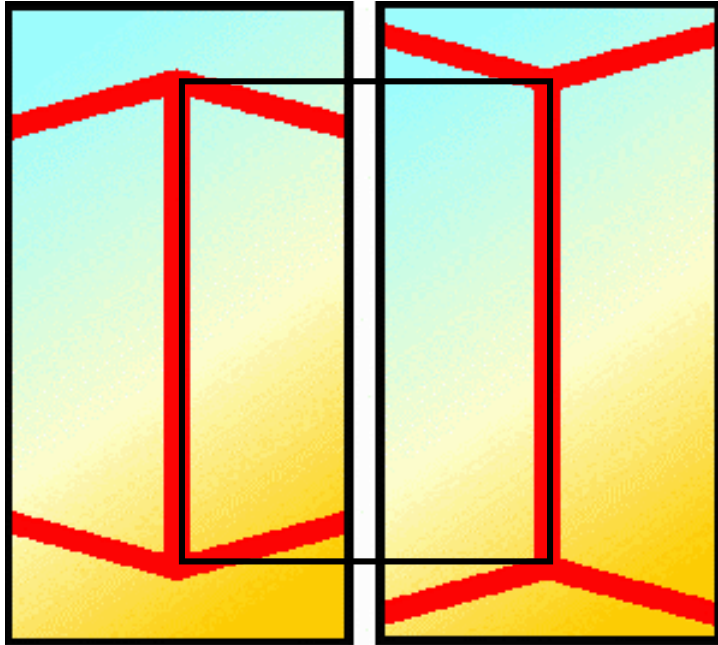


- **Depends on surrounding primitives**
 - Directional emphasis
 - Size emphasis



<http://www.panoptikum.net/optischetaeuschungen/index.html>

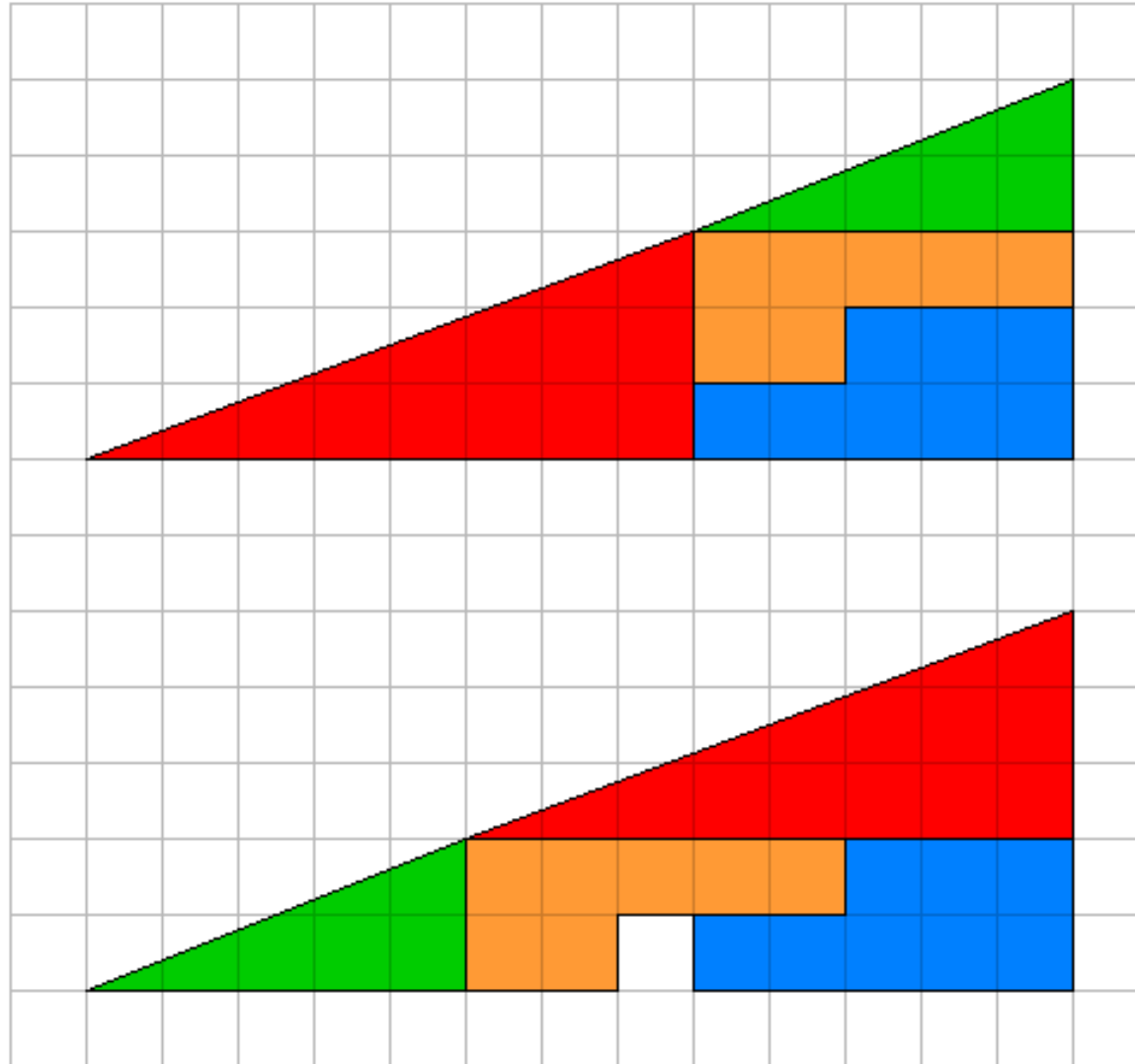
Shape Processing: Geometrical Clues



<http://www.panoptikum.net/optischetaeuschungen/index.html>

- **Automatic geometrical interpretation**
 - 3D perspective
 - Implicit scene depth

Visual “Proofs”

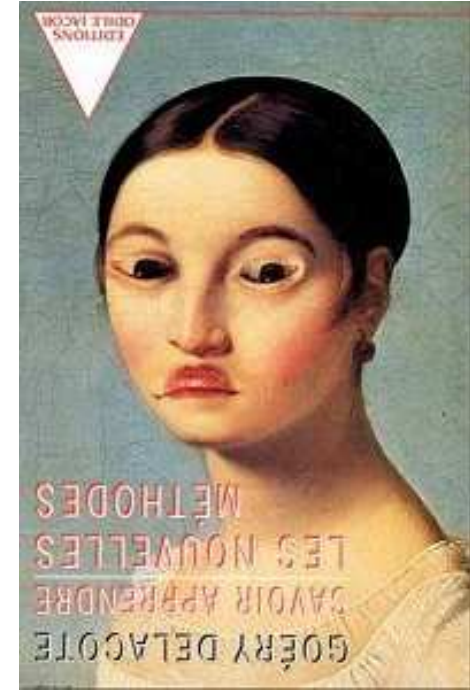


<http://www.panoptikum.net/optischetaeuschungen/index.html>

HVS: High-Level Scene Analysis



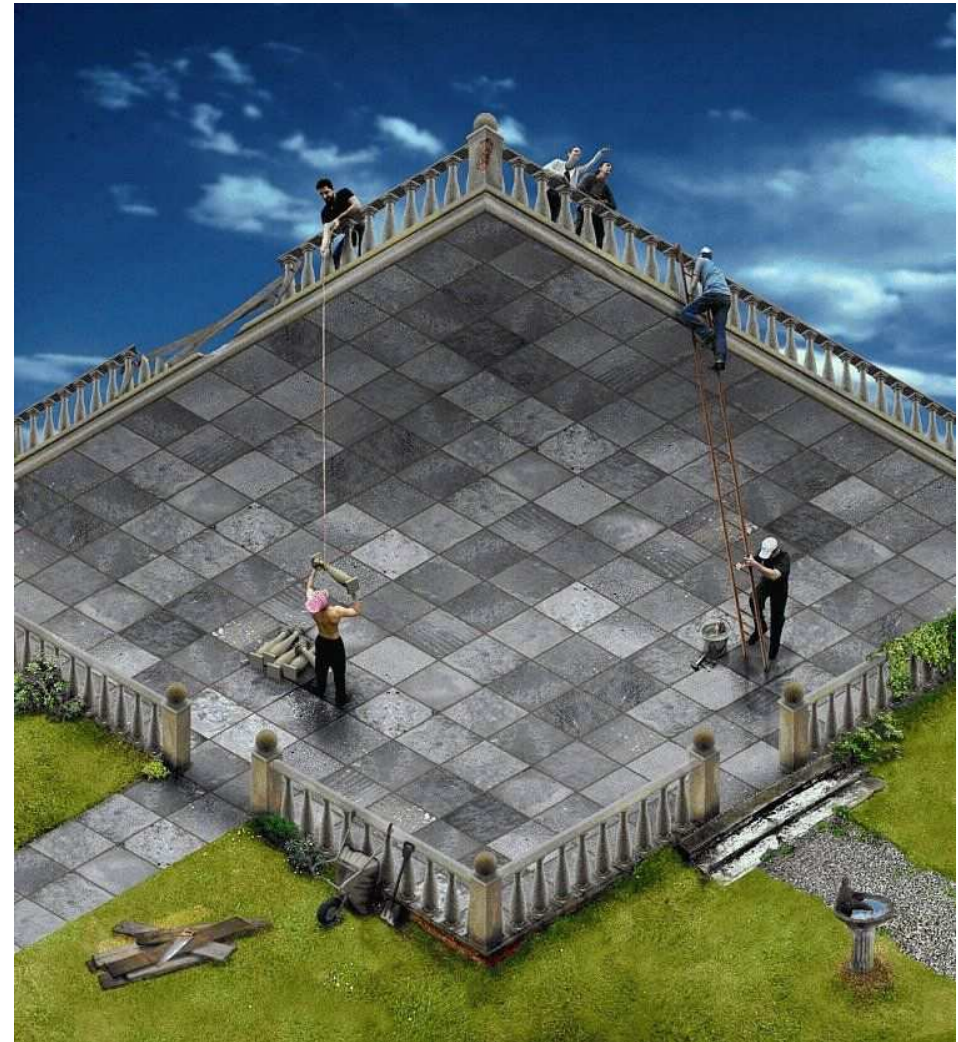
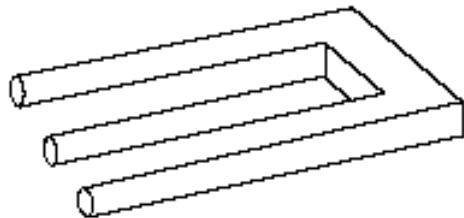
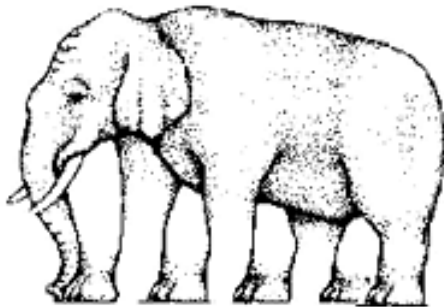
- **Experience**
- **Expectation**
- **Local clue consistency**



<http://www.panoptikum.net/optischetaeusungen/index.html>

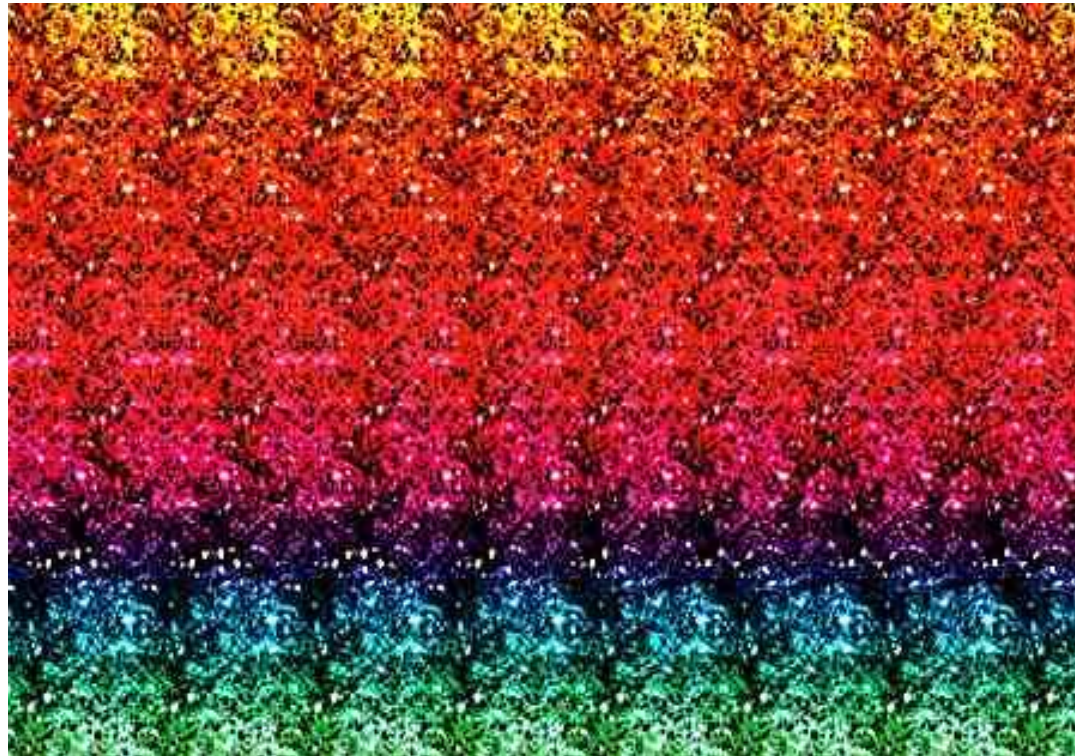
Impossible Scenes

- **Escher et.al.**
 - Confuse HVS by presenting contradicting visual clues



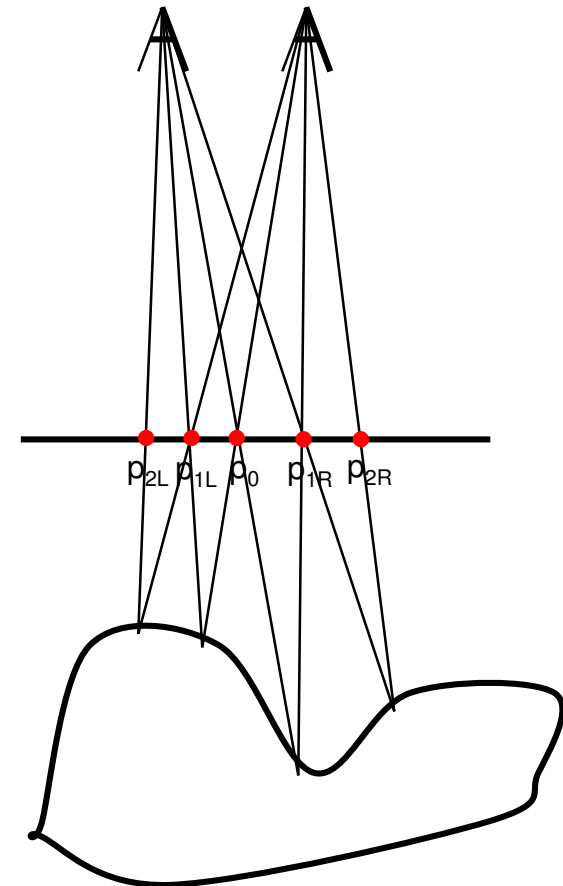
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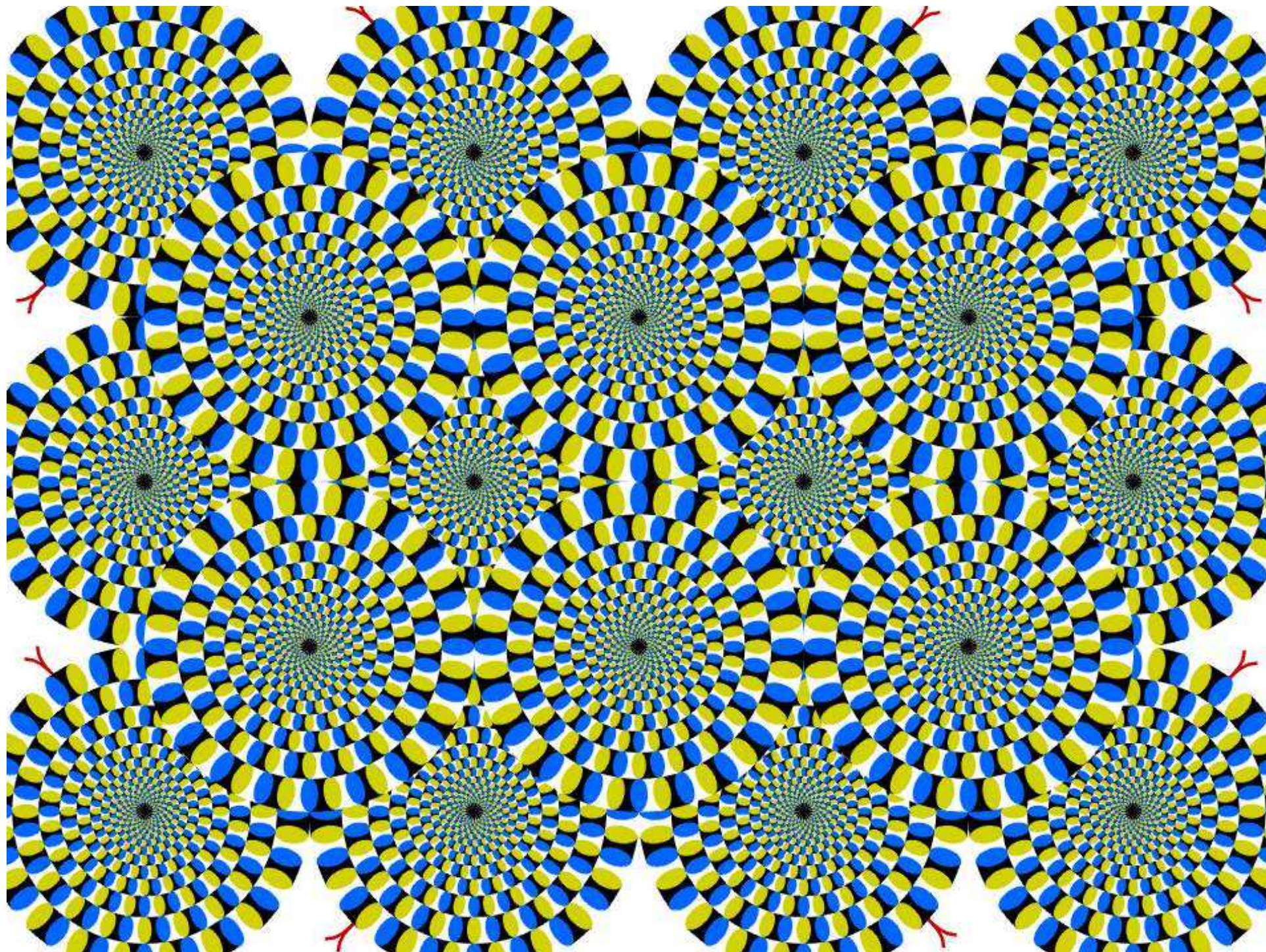
Single Image Random Dot Stereograms



SIRDS Construction

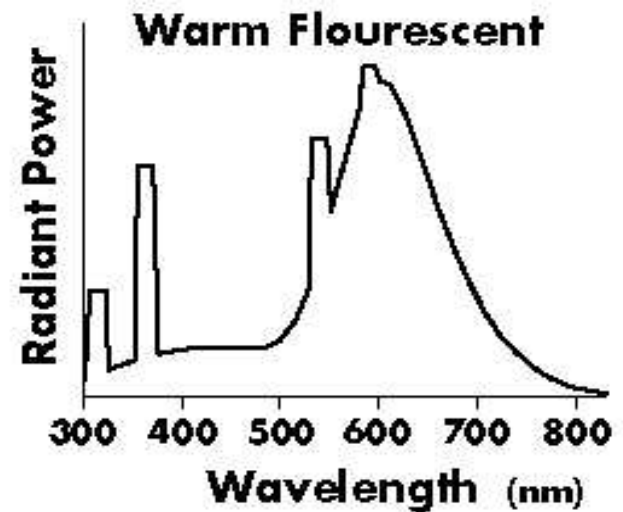
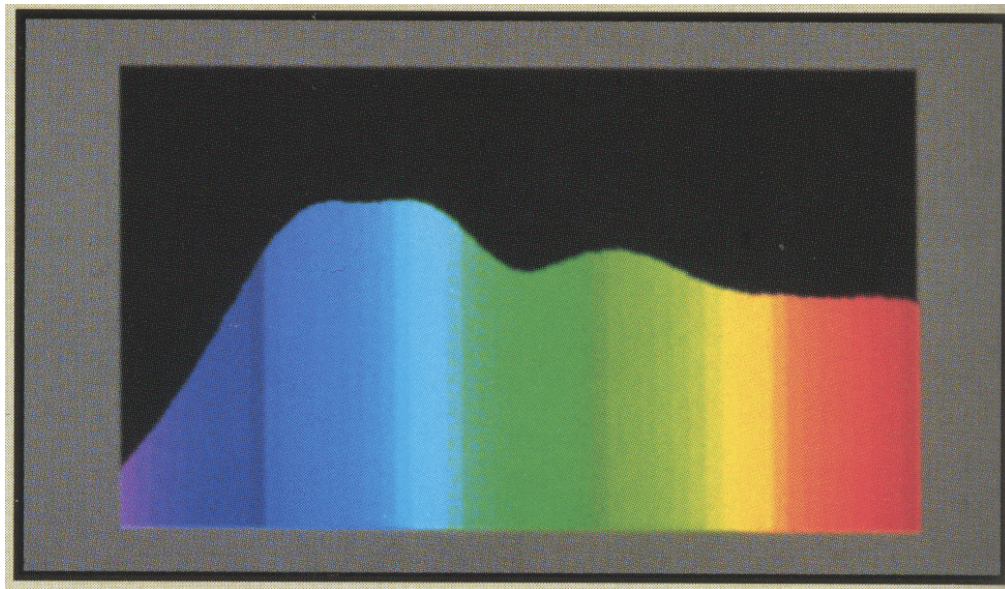
- Assign arbitrary color to p_0 in image plane
- Trace from eye points through p_0 to object surface
- Trace back from object to corresponding other eye
- Assign color at p_0 to intersection points p_{1L}, p_{1R} with image plane
- Trace from eye points through p_{1L}, p_{1R} to object surface
- Trace back to eyes
- Assign p_0 color to p_{2L}, p_{2R}
- Repeat until image plane is covered



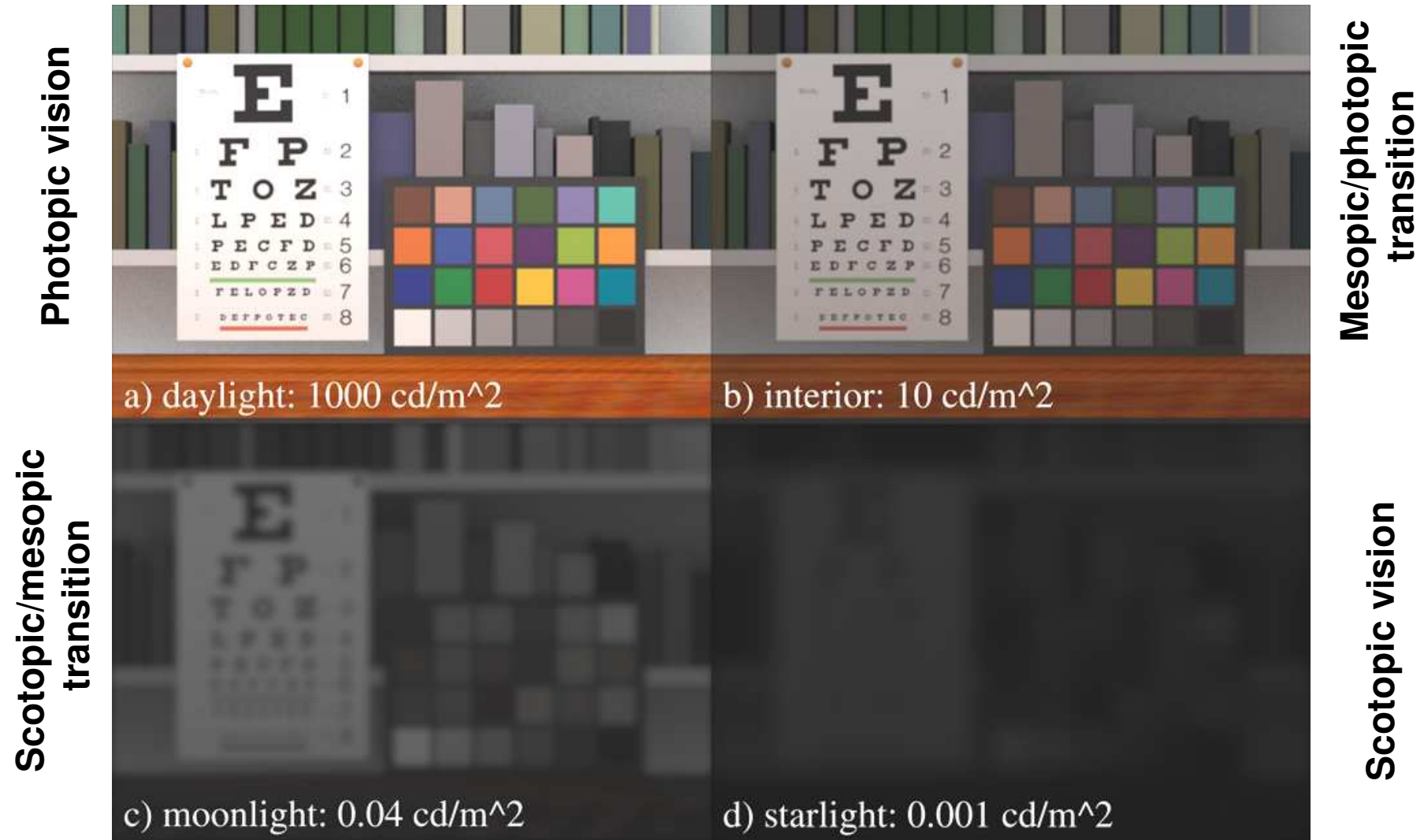


Color

- **Physics**
 - Continuous spectral energy distribution
- **Human color perception**
 - Cones in retina
 - 3 different cone types
 - Spectral mapping to 3 channels



Visual Acuity and Color Perception



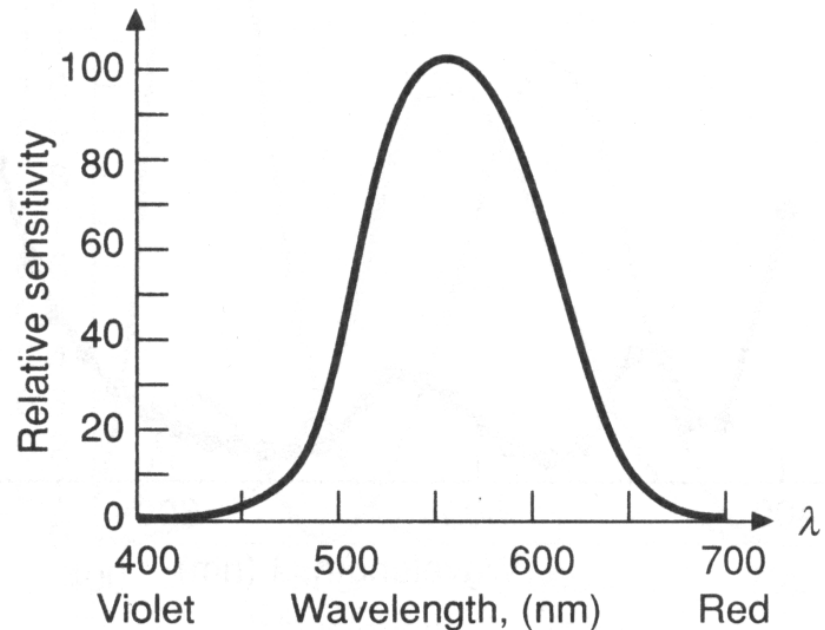
Color Comparison

- **Luminance**

- Compare a color source with a gray source
- „Luminous Efficiency Function“

$$Y = \int V(\lambda)L(\lambda)d\lambda$$

- Average value from the „spectral sensitivity“ of all receptors
- Photopic: day vision (cones)
- Scotopic: night vision (rods)
- Mesopic: mixed conditions (rods and cones)



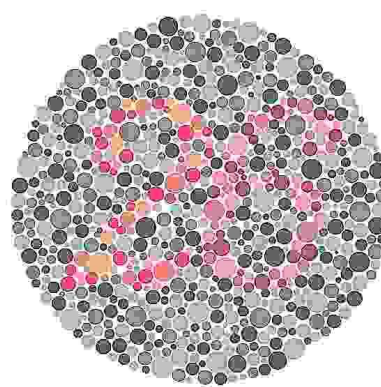
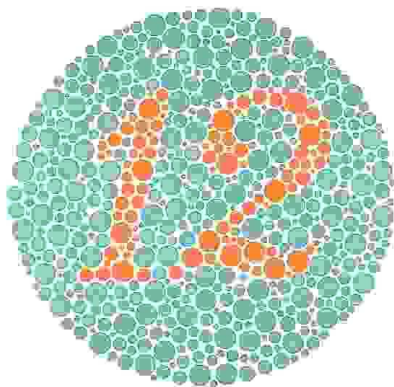
Luminous Efficiency Function (V)

Color Perception

- **Di-chromaticity (dogs, cats)**
 - Yellow & blue-violet
 - Green, orange, red indistinguishable
- **Tri-chromaticity (humans, monkeys)**
 - Red, green, blue
 - Color-blindness
 - Most often men, green color-blindness



www.lam.mus.ca.us/cats/color/



www.colorcube.com/illusions/clrblind.html

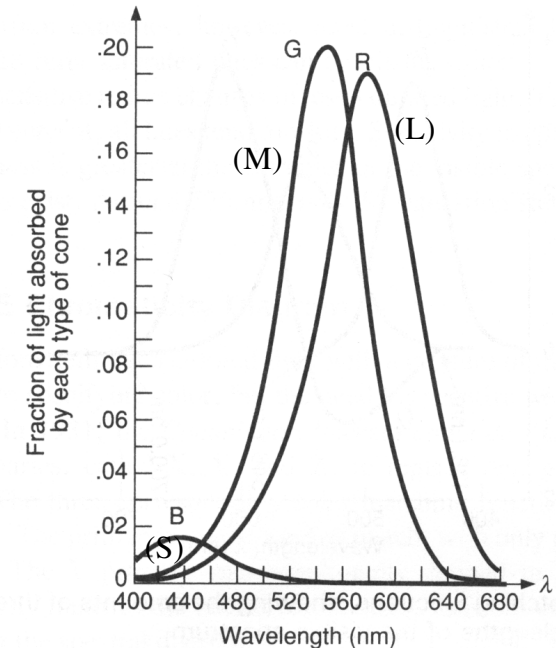
Color Mapping

- **Spectrum mapping onto perceptual color space**

- Infinitely many wavelengths
=> 3 color channels
- Cone absorption spectra (S,M,L)
- Overlap of absorption characteristics
- Metamerism
 - Same perceived color for different spectral distributions

- **Grassmann's law**

- Any perceivable color can be represented as a mixture of three primary colors
- Colors add linearly
- From tri-stimulus at every wavelength, total response can be calculated by integration
- But: Tri-stimulus response **NOT** proportional to absorption spectrum !



Standard Color Space CIE-*RGB*

- **Wide range of colors can be mixed from three monochromatic primary colors 438.1, 546.1, and 700 nm**
 - Colors in the vicinity of 500 nm can only be matched by “subtracting” certain amount of $r(\lambda)$
 - Inhibitory behavior (\Rightarrow contrast !)
 - “Negative” color values

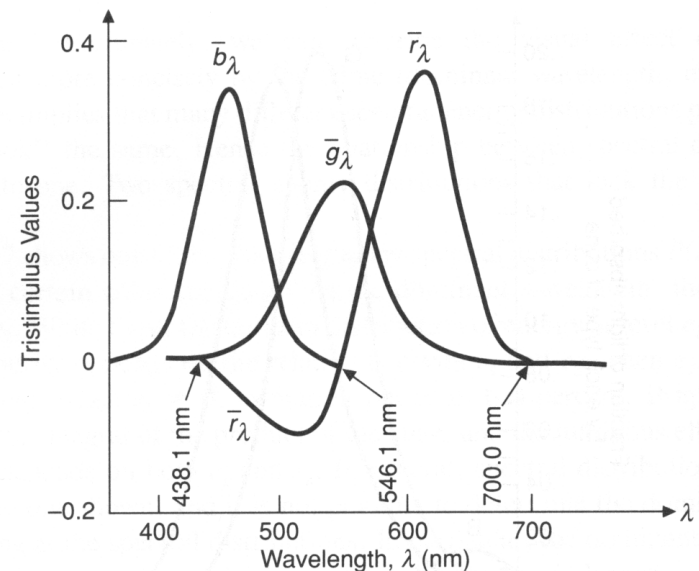
RGB are called **tristimulus values**:

$$R = K_m \int L(\lambda) \bar{r}(\lambda) d\lambda,$$

$$G = K_m \int L(\lambda) \bar{g}(\lambda) d\lambda,$$

$$B = K_m \int L(\lambda) \bar{b}(\lambda) d\lambda$$

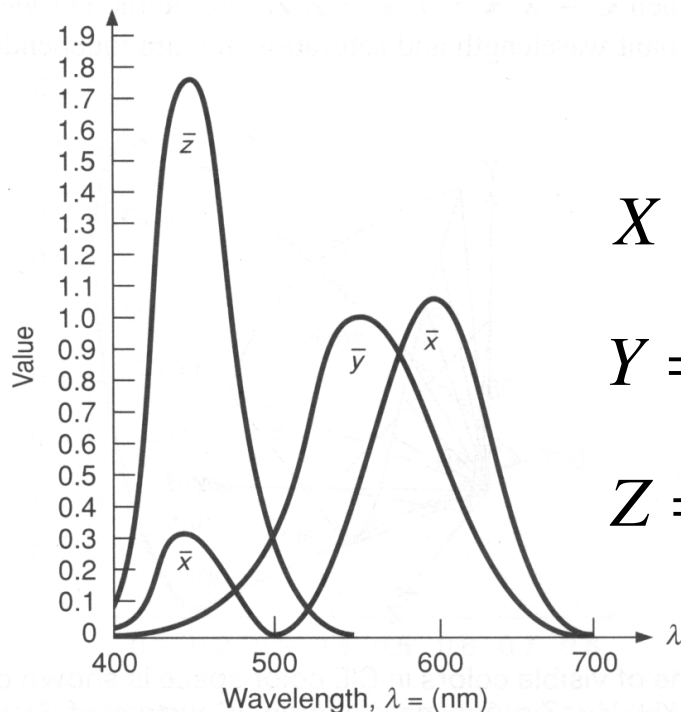
$$K_m = 680 \text{ lm} / W$$



Color-matching functions for given monochromatic primary colors

Standard Color Space CIE-*XYZ*

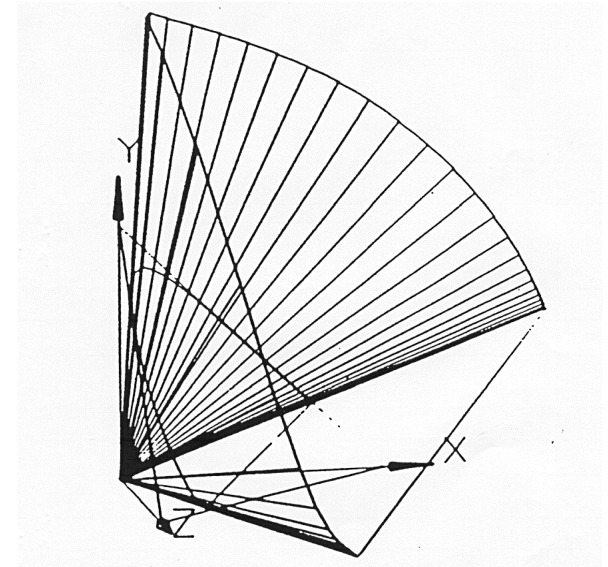
- **Standardized imaginary primaries CIE *XYZ* (1931)**
 - Non-realizable super-saturated primary colors
 - Reproduces all perceivable colors by additive mixing
 - Only positive weights
 - *Y* is equivalent to luminance
 - Perceivable colors span irregular cone in *XYZ* space



$$X = K_m \int L(\lambda) \bar{x}(\lambda) d\lambda,$$

$$Y = K_m \int L(\lambda) \bar{y}(\lambda) d\lambda,$$

$$Z = K_m \int L(\lambda) \bar{z}(\lambda) d\lambda$$



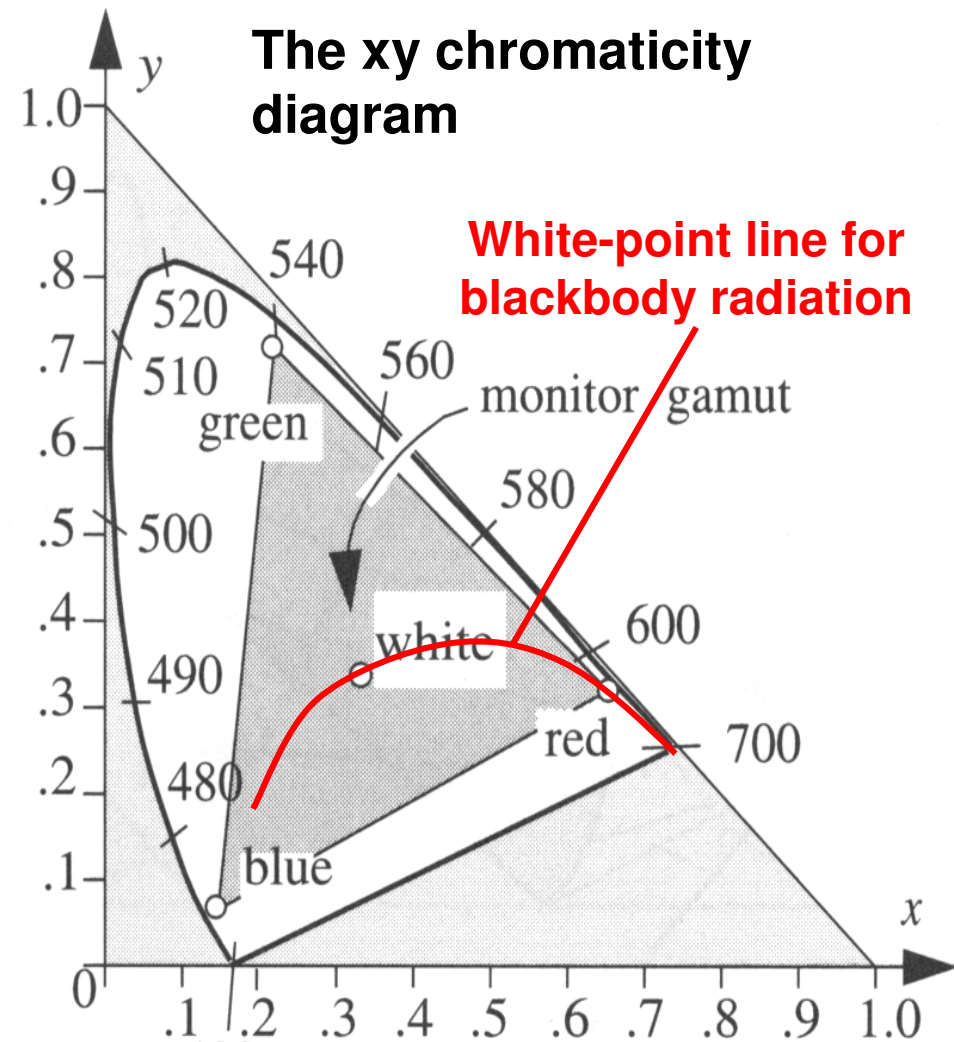
CIE Chromaticity Diagram

- **Normalization:**

- $x = \frac{X}{X+Y+Z}$ etc

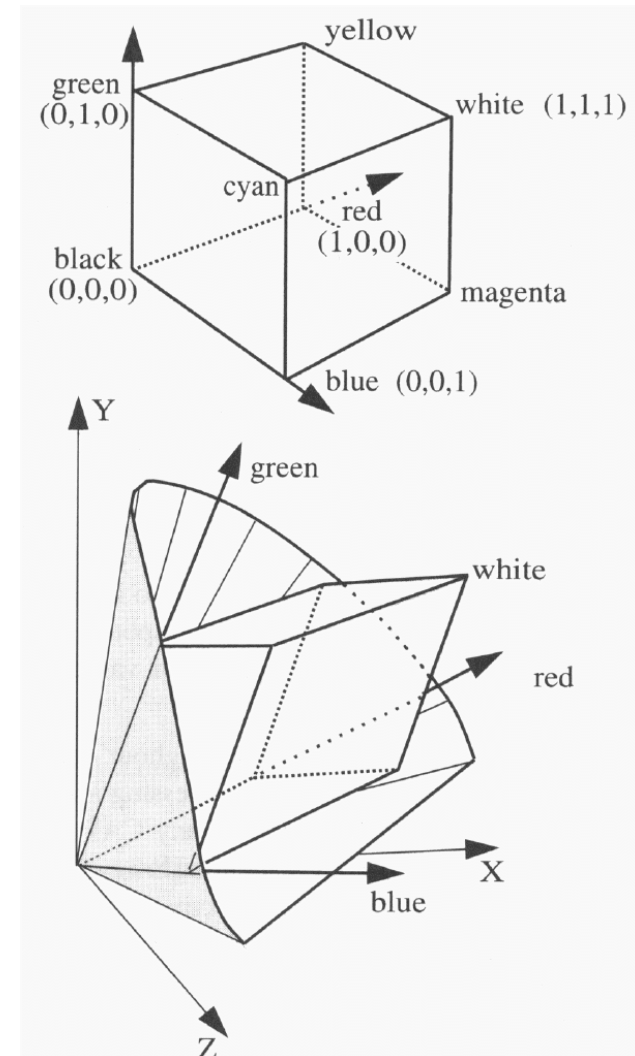
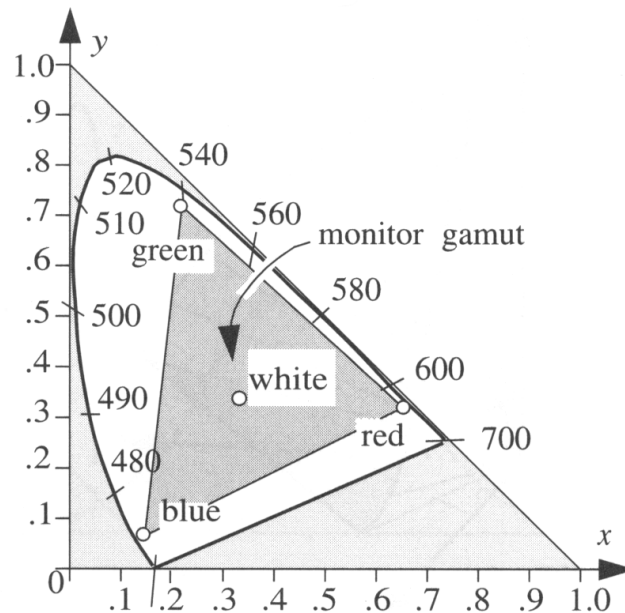
Projection on the plane
of the prime valences
 $z = 1 - x - y$

- Chromaticity diagram:
2D-Plot over x and y
 - Points called as color
locations
 - White point: $\sim(0.3, 0.3)$
 - Device dependent
 - Adaptation of the eye
 - Saturation: Distance
to the white point
 - Complementary colors



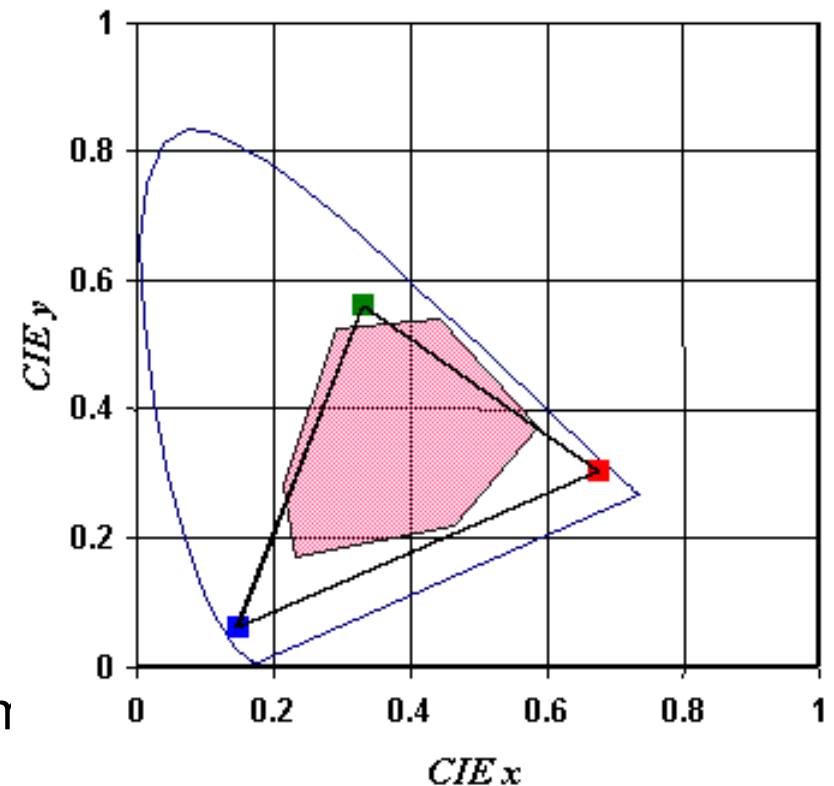
Monitor Color Gamut

- **CIE XYZ gamut**
 - Device-independent (repeatable)
- **Device color gamut**
 - Triangle inside color space, additive color blend



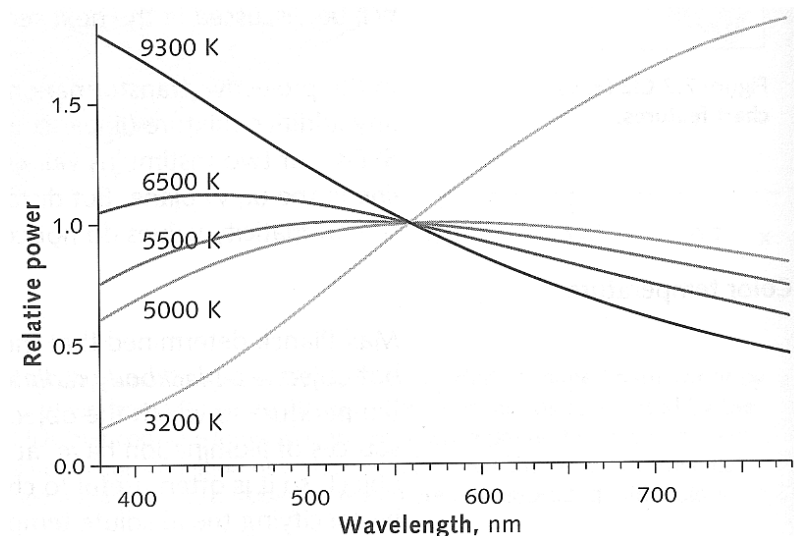
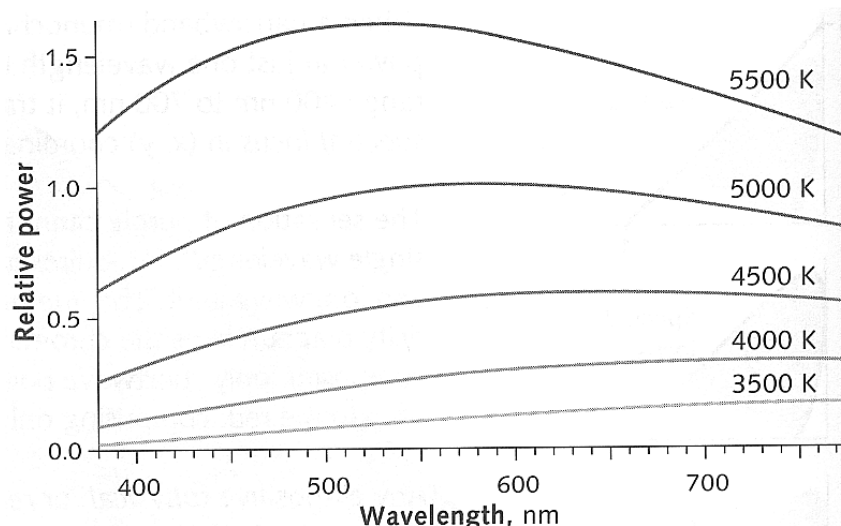
Printer Color Gamut

- **Color Gamut**
 - Complex for printer, because of subtractive color blend
 - Complex interactions between printed color points
 - Depends on printer colors and printer technique
- **Gamut compression**
 - Each device should replace of-gamut colors nearest approximate
 - Possible significant color printed → scanned → displayed in



Color Temperature

- **Theoretical light source: A black body radiator**
 - Perfect emitter of energy, the whole energy emitted due only to thermal excitation
 - Has a fixed frequency spectrum $\rho = \rho(\lambda, T)$ (Planck's law)
 - Spectrum can be converted to color
 - Energy shifts toward shorter wavelengths as the temperature of the black body increases
 - Normalizing of the spectrum (at 550 nm)
 - Color specification through temperatures



CIE Standard Illuminants

- Defining the properties of illuminant is important to describe color in many applications
 - **Illuminant A** – incandescent lighting conditions with a color temperature of about 2856 °K
 - **Illuminant B** – direct sunlight at about 4874 °K
 - **Illuminant C** – indirect sunlight at about 6774 °K
 - **Illuminants D₅₀** and **D₆₅** – different daylight conditions at color temperatures 5000 °K and 6500 °K, respectively
- The spectral data of CIE Standard Illuminants are available and often used in the CG applications